

ECEN689: Special Topics in High-Speed Links Circuits and Systems Spring 2010

Lecture 5: Interconnect Measurement Techniques



Sam Palermo

Analog & Mixed-Signal Center

Texas A&M University

Announcements

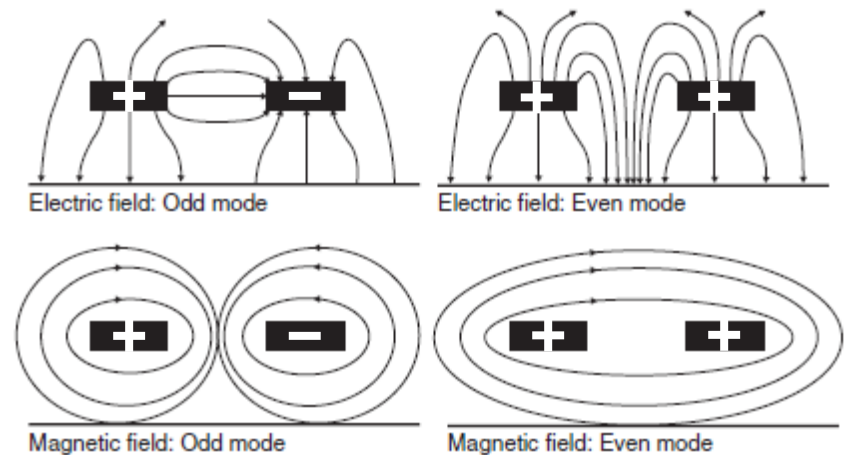
- HW1 due NOW
- HW2 posted on website and due 2/5
- Current Reading
 - Chapter 3.4, 3.6 – 3.7
- For next time
 - TBD

Agenda

- Differential transmission lines
- Interconnect measurement techniques
 - Time-domain reflectometry (TDR)
 - Network analyzer
 - S-parameters
- Majority of today's material from Dally
Chapter 3.4, 3.6 - 3.7
- Some s-parameter material from Sackinger
"Broadband Circuits" text

Differential Transmission Lines

- Differential signaling advantages
 - Self-referenced
 - Common-mode noise rejection
 - Increased signal swing
 - Reduced self-induced power-supply noise
- Requires 2x the number of signaling pins relative to single-ended signaling
 - But, smaller ratio of supply/signal (return) pins
 - Total pin overhead is typically 1.3-1.8x (vs 2x)

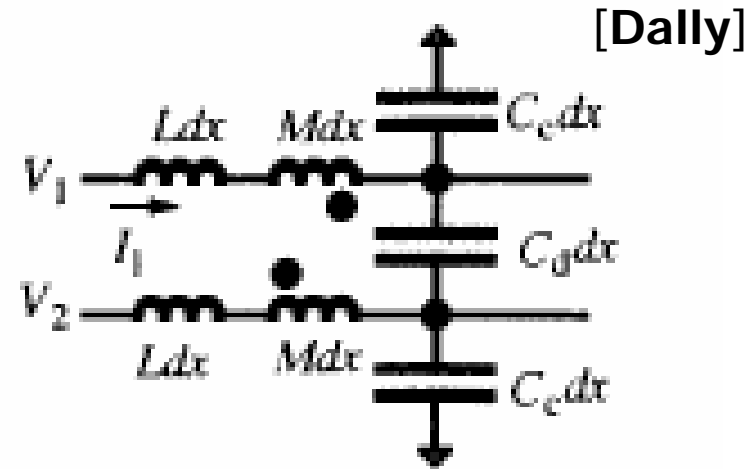


[Hall]

Balanced Transmission Lines

- Even (common) mode excitation
 - Effective $C = C_C$
 - Effective $L = L + M$
- Odd (differential) mode excitation
 - Effective $C = C_C + 2C_d$
 - Effective $L = L - M$

$$Z_{DIFF} = 2Z_{odd}, \quad Z_{CM} = \frac{Z_{even}}{2}$$

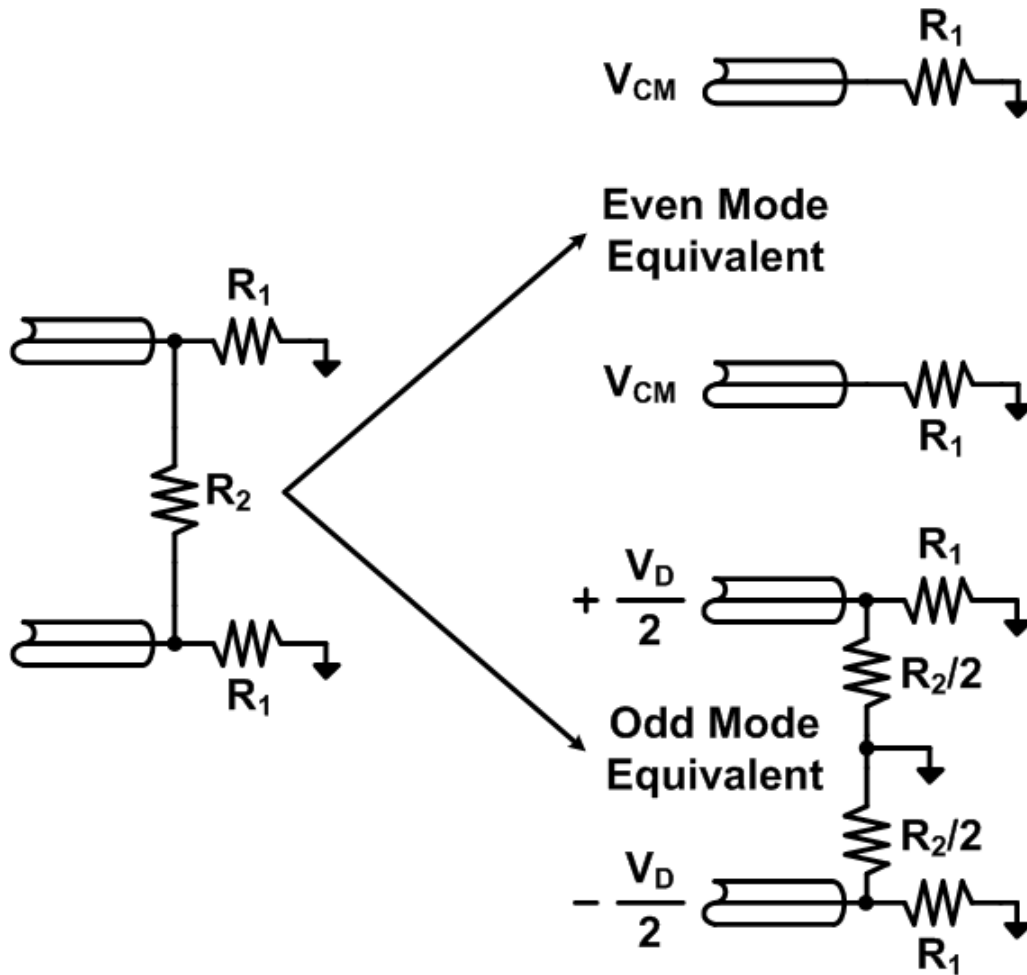


(a) Model of a Balanced Line

$$Z_{even} = \left(\frac{L + M}{C_c} \right)^{1/2}$$

$$Z_{odd} = \left(\frac{L - M}{C_c + 2C_d} \right)^{1/2}$$

PI-Termination

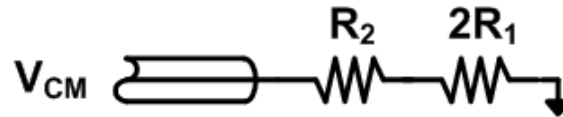


$$Z_{even} = R_1$$

$$Z_{odd} = R_1 \parallel R_2/2 = Z_{even} \parallel R_2/2$$

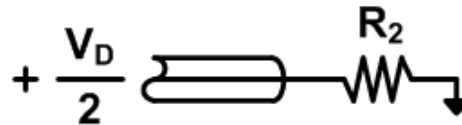
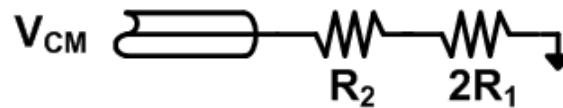
$$R_2 = 2 \left(\frac{Z_{odd} Z_{even}}{Z_{even} - Z_{odd}} \right)$$

T-Termination

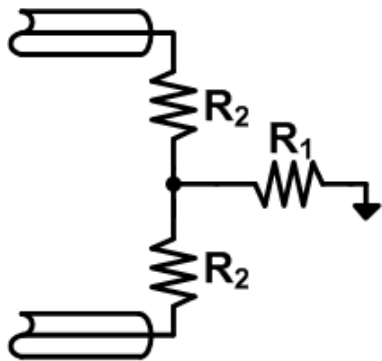


Even Mode Equivalent

$$Z_{even} = R_2 + 2R_1$$



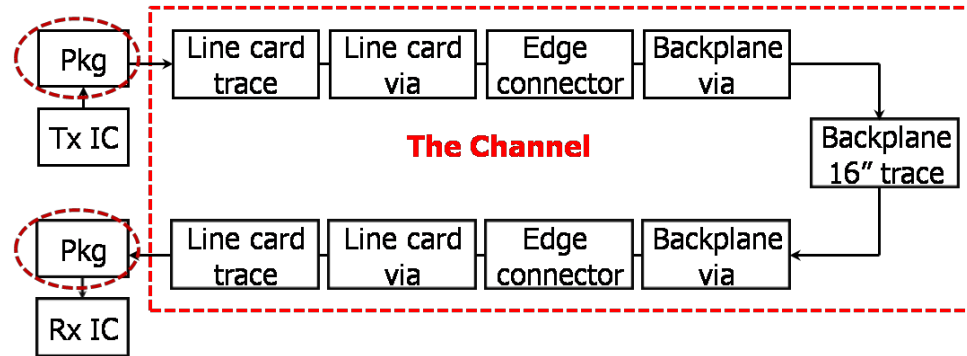
Odd Mode Equivalent



$$Z_{odd} = R_2$$

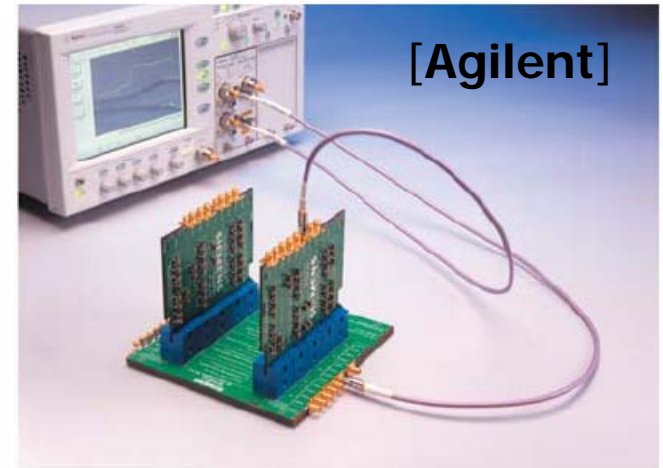
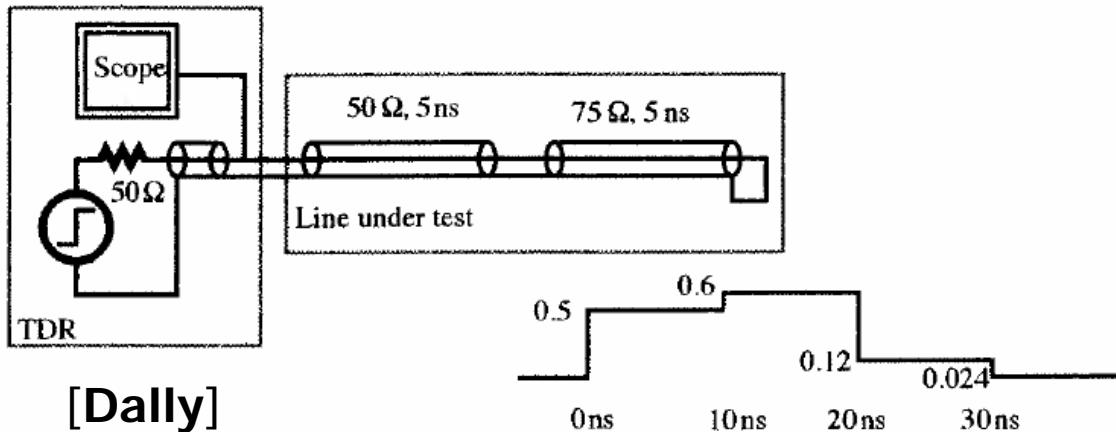
$$R_1 = \frac{1}{2}(Z_{even} - Z_{odd})$$

Interconnect Modeling



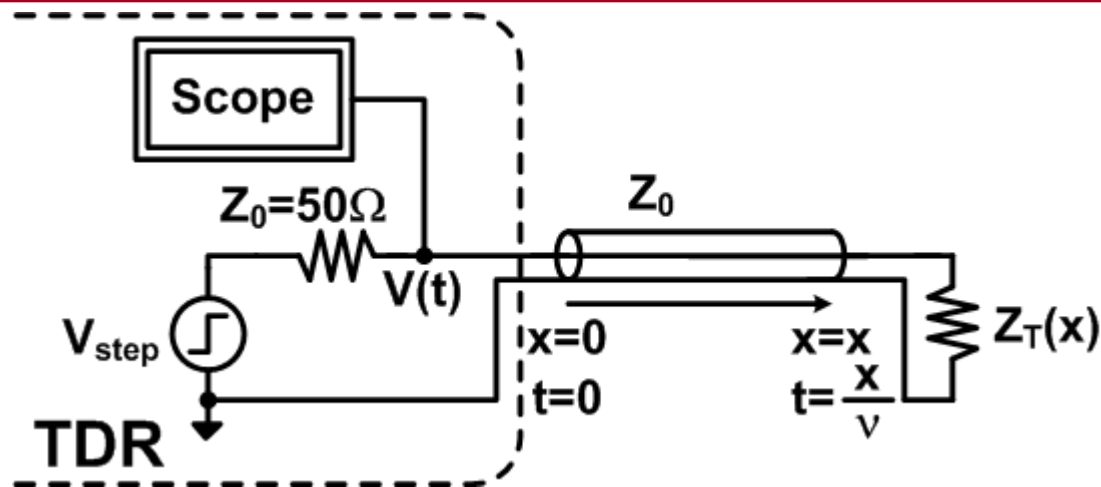
- Why do we need interconnect models?
 - Perform hand calculations and simulations (Spice, Matlab, etc...)
 - Locate performance bottlenecks and make design trade-offs
- Model generation methods
 - Electromagnetic CAD tools
 - Actual system measurements
- Measurement techniques
 - Time-Domain Reflectometer (TDR)
 - Network analyzer (frequency domain)

Time-Domain Reflectometer (TDR)



- TDR consists of a fast step generator and a high-speed oscilloscope
- TDR operation
 - Outputs fast voltage step onto channel
 - Observe voltage at source, which includes reflections
 - Voltage magnitude can be converted to impedance
 - Impedance discontinuity location can be determined by delay
- Only input port access to characterize channel

TDR Impedance Calculation



$$k_r(t) = \frac{V_r(t)}{V_i} = \frac{Z_T(t) - Z_0}{Z_T(t) + Z_0}$$

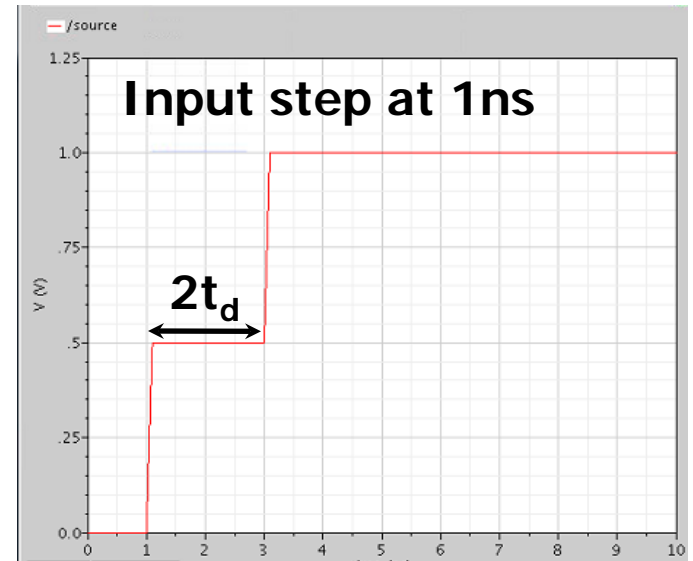
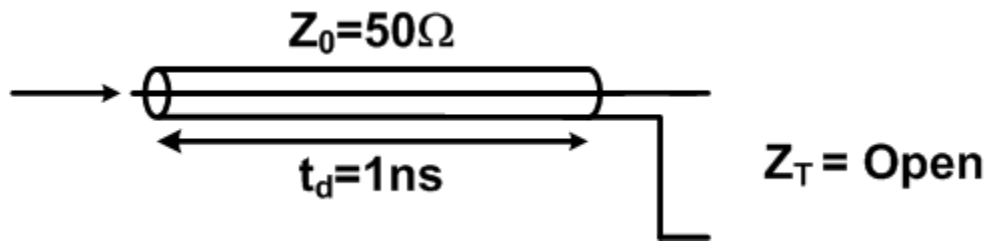
$$Z_T(t) = Z_0 \left(\frac{1 + k_r(t)}{1 - k_r(t)} \right) = Z_0 \left(\frac{V_i + V_r(t)}{V_i - V_r(t)} \right) = Z_0 \left(\frac{V(t)}{2V_i - V(t)} \right)$$

$$\text{If } V_{\text{STEP}} = 1V \Rightarrow V_i = 0.5V$$

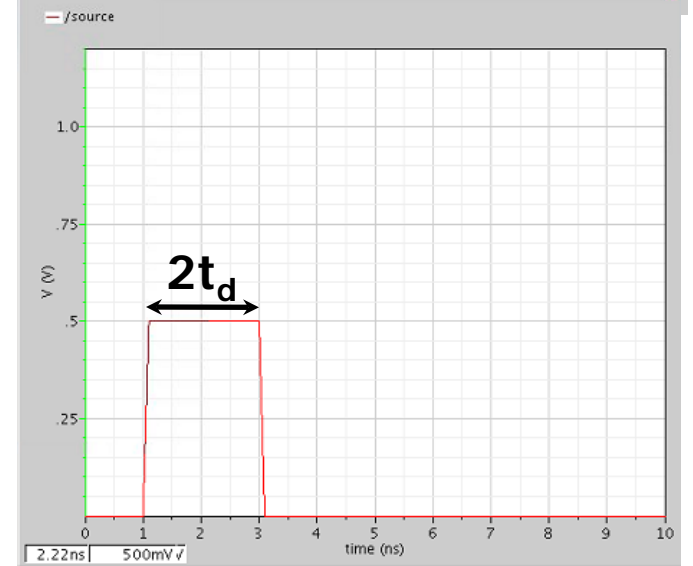
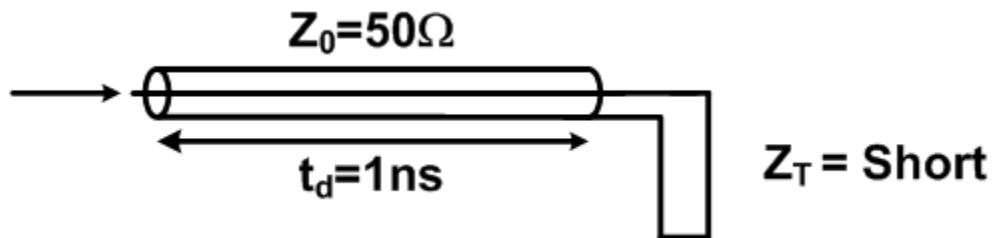
$$\boxed{Z_T(t) = Z_0 \left(\frac{V(t)}{1V - V(t)} \right) \quad Z_T(x) = Z_T \left(t = \frac{2x}{v} \right)}$$

TDR Waveforms (Open & Short)

- Open termination

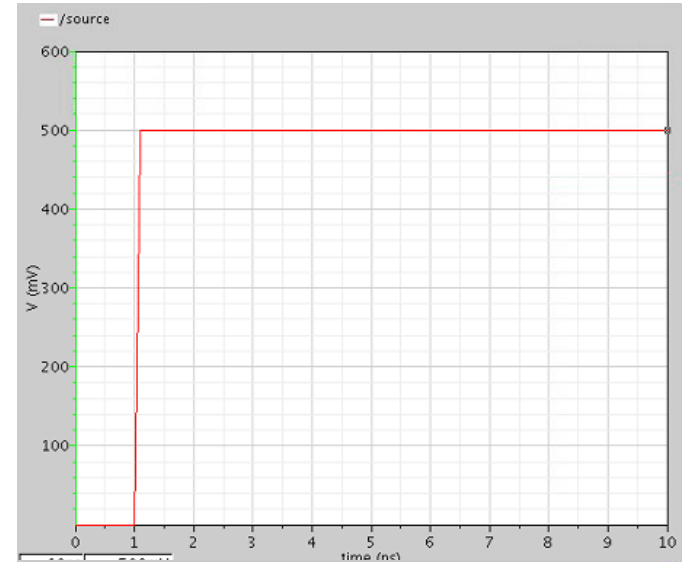
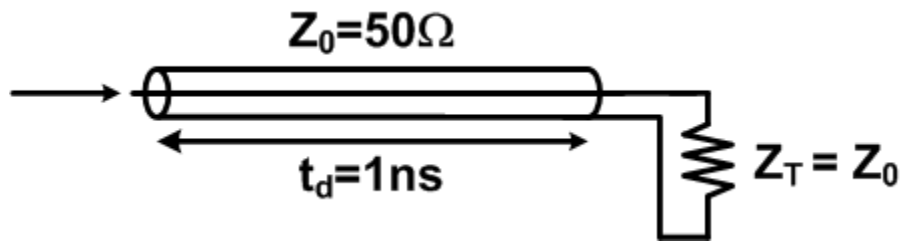


- Short termination

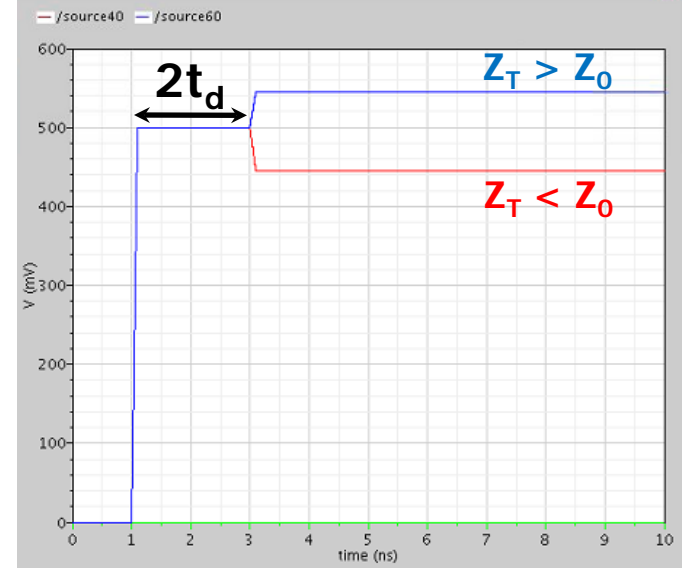
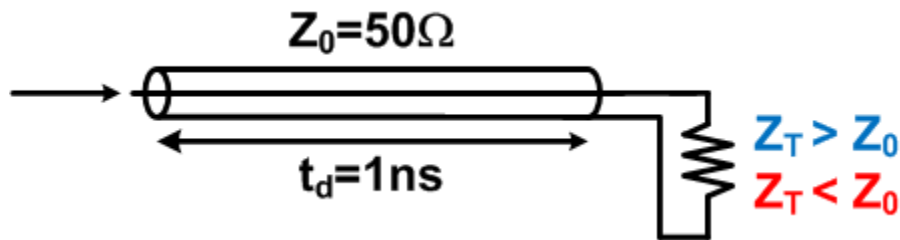


TDR Waveforms (Matched & Mismatched)

- Matched termination

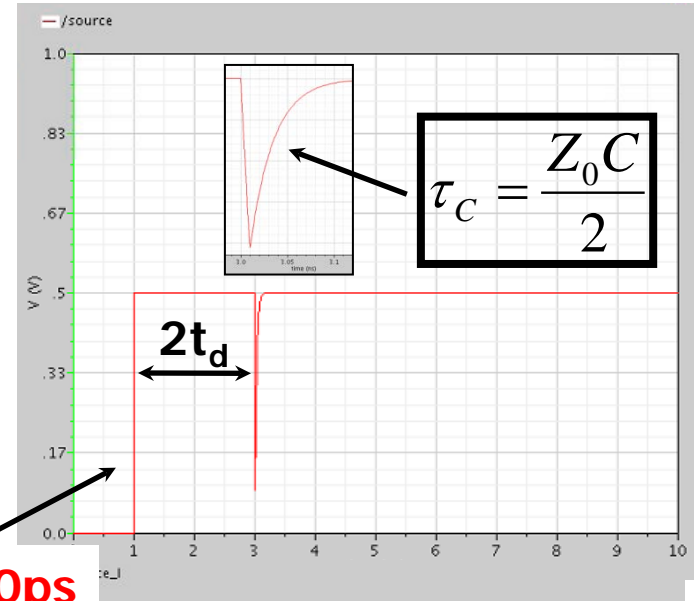
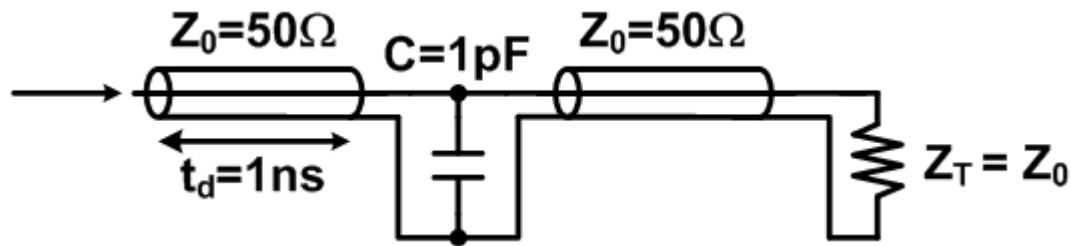


- Mismatched termination

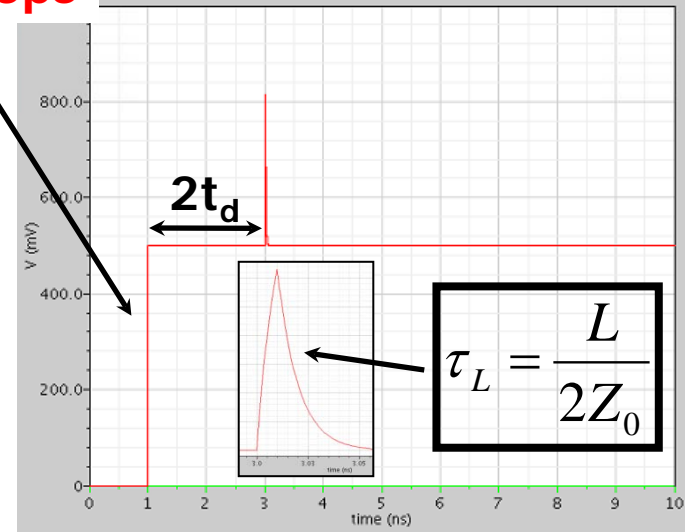
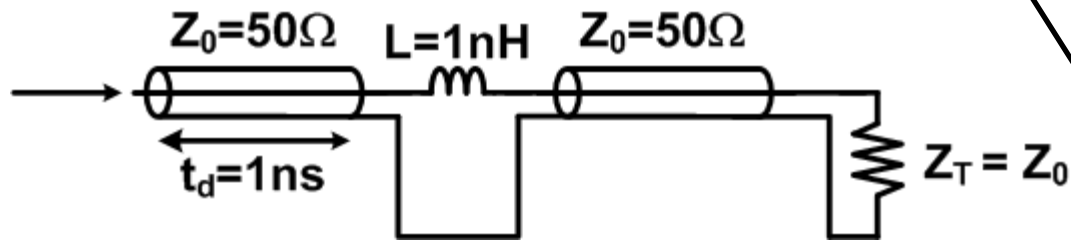


TDR Waveforms (C & L Discontinuity)

- Shunt C discontinuity



- Series L discontinuity



Peak voltage spike magnitude:

$$\frac{\Delta V}{V} = \left(\frac{\tau}{t_r} \right) \left[1 - e^{-\left(\frac{t_r}{\tau} \right)} \right]$$

$t_r = 10\text{ps}$

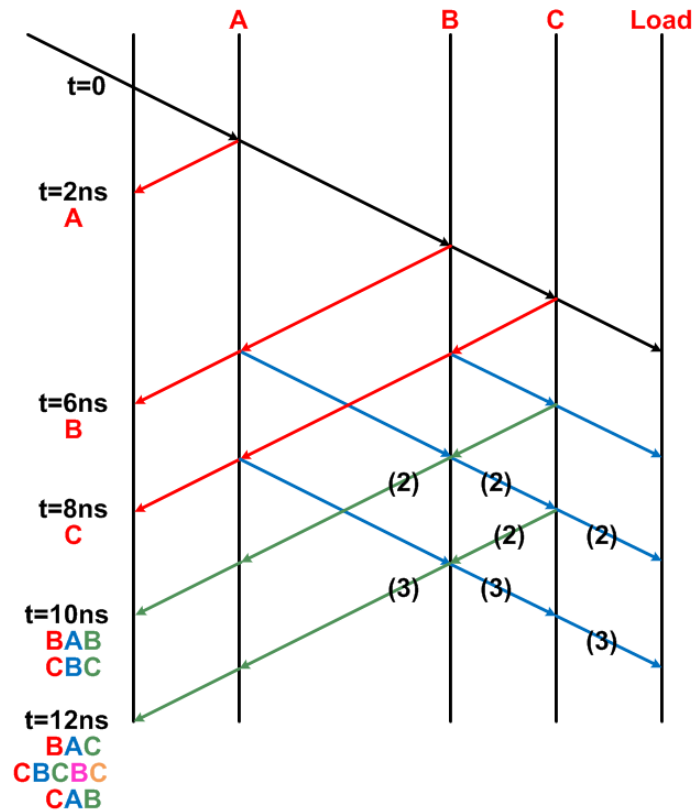
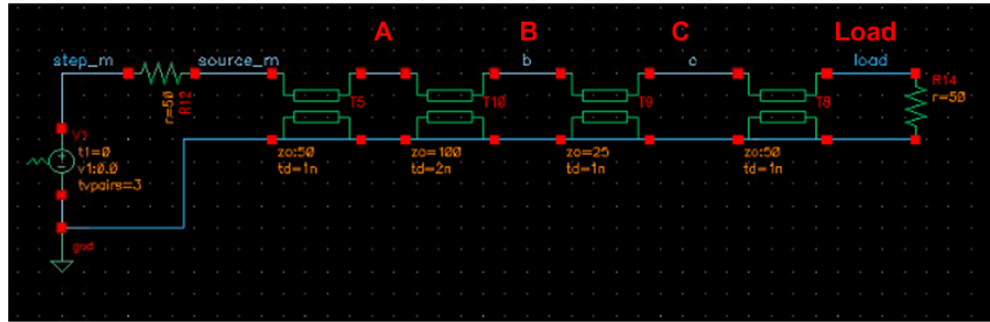
TDR Rise Time and Resolution

- TDR spatial resolution is set by step risetime

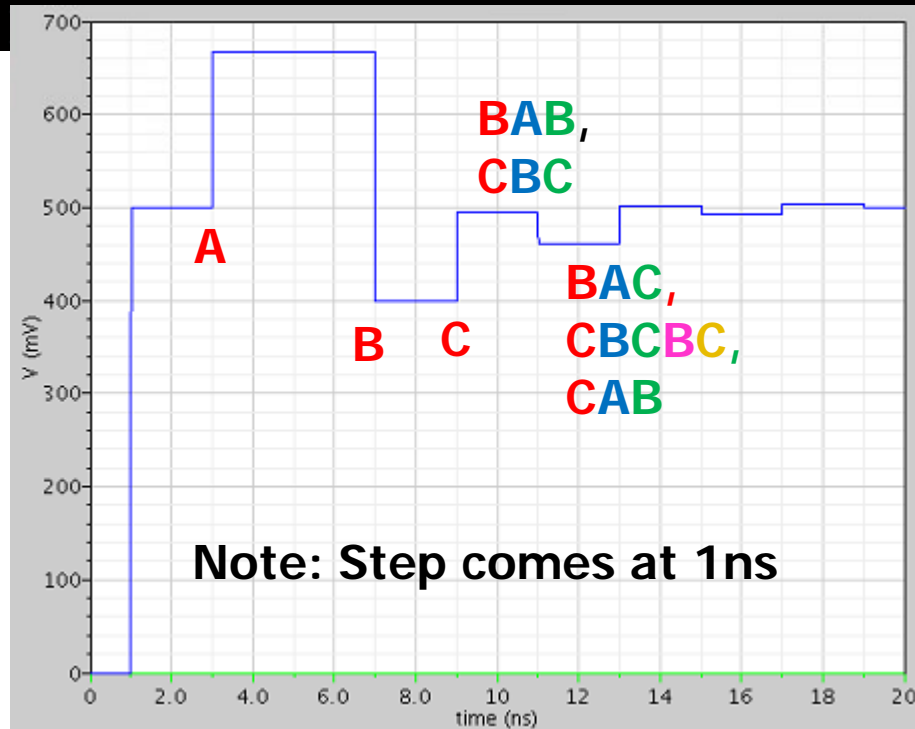
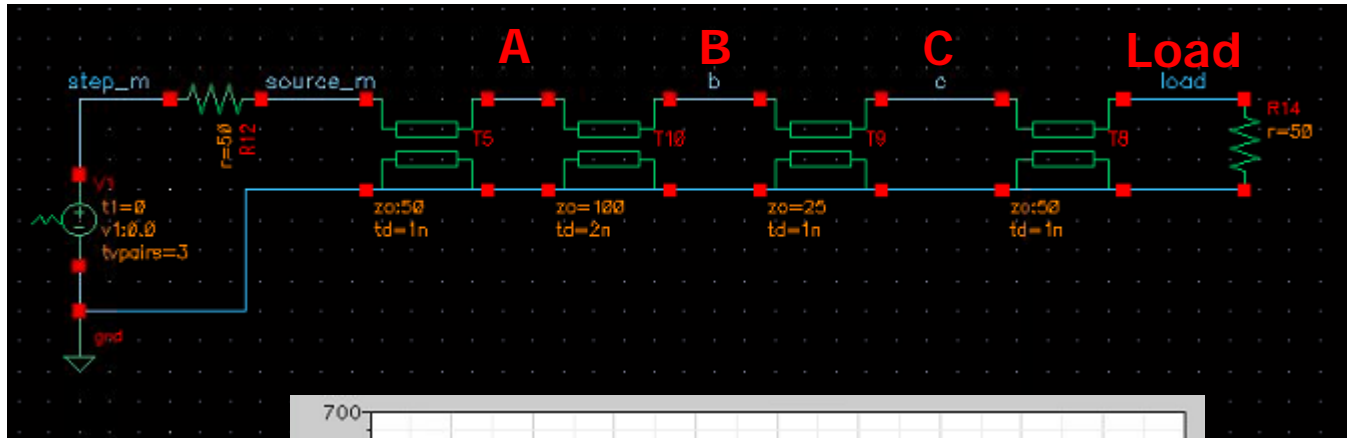
$$\Delta x > t_r v$$

- Step risetime degrades with propagation through channel
 - Dispersion from skin-effect
 - Lump discontinuities low-pass filter the step
- Causes difficulty in estimating L & C values
- Channel filtering can actually compensate for lump discontinuity spikes 😊

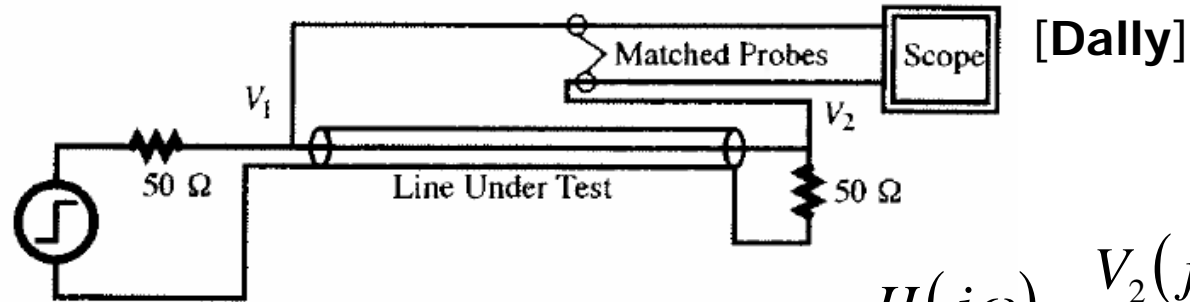
TDR Multiple Reflections



TDR Waveforms (Multiple Discontinuities)

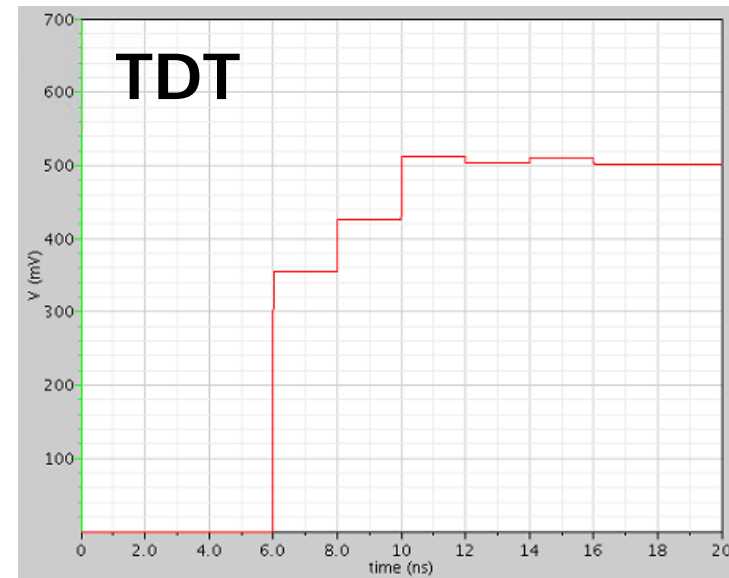
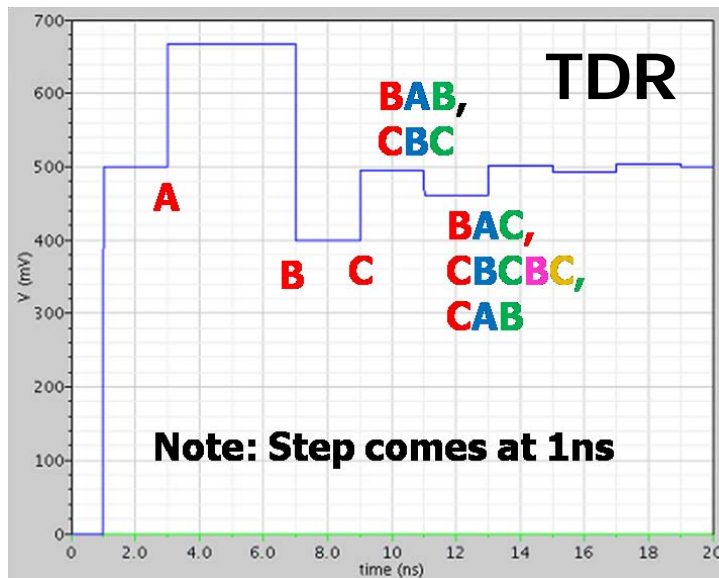


Time-Domain Transmission (TDT)



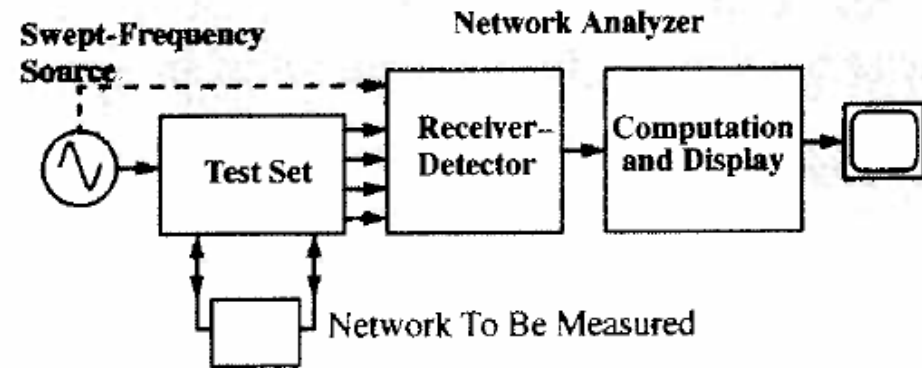
$$H(j\omega) = \frac{V_2(j\omega)}{V_1(j\omega)}$$

- Can measure channel transfer function
- Hard to isolate impedance discontinuities, as they are superimposed on a single rising edge

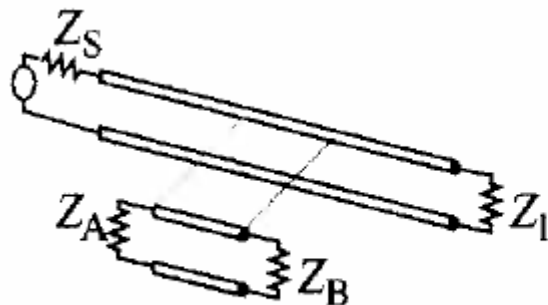


Network Analyzer

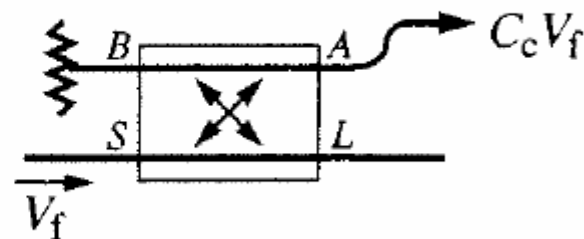
- Stimulates network with swept-frequency source
- Measures network response amplitude and phase
- Can measure transfer function, scattering matrices, impedance, ...



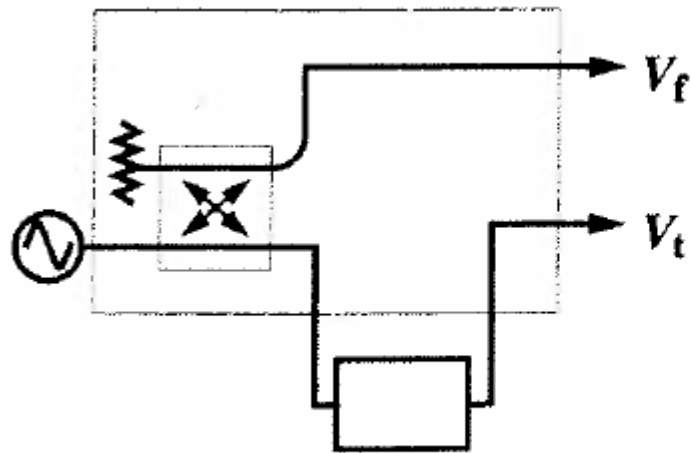
[Dally]



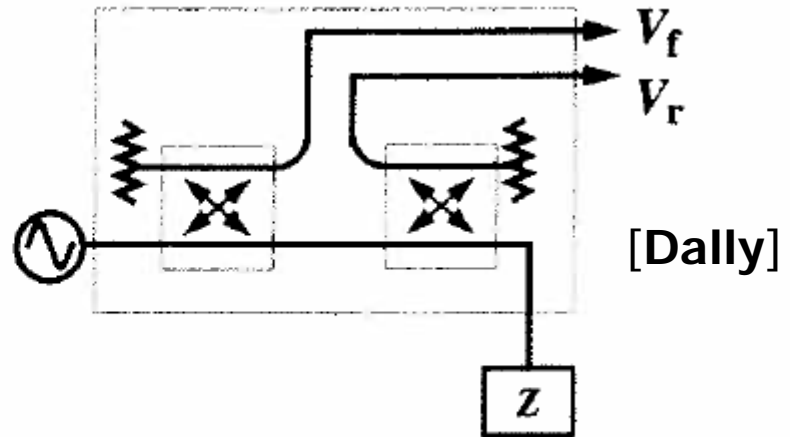
Direction Coupler



Transfer Function & Impedance Measurements



Test Set for Transfer Function

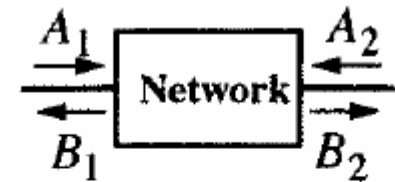


[Dally]

Test Set for Impedance Measurements

Scattering (S) Parameters

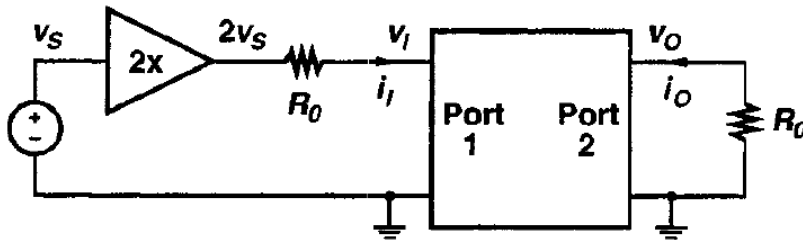
- Why S Parameters?
 - Easy to measure
 - Y, Z parameters need open and short conditions
 - S parameters are obtained with nominal termination
 - S parameters based on incident and reflected wave ratio



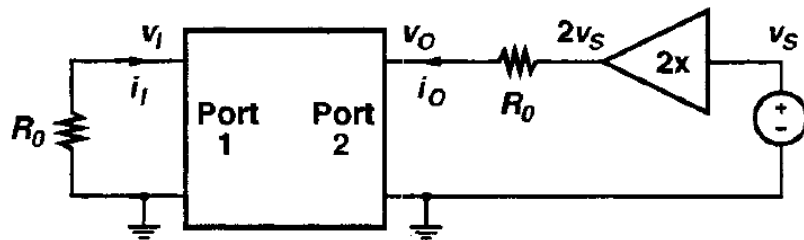
$$\begin{bmatrix} B_1 \\ B_2 \end{bmatrix} = \begin{bmatrix} S_{11} & S_{12} \\ S_{21} & S_{22} \end{bmatrix} \cdot \begin{bmatrix} A_1 \\ A_2 \end{bmatrix}$$

S-matrix [Dally]

S-Parameter Test Circuits & Meaning



[Sackinger]



$$S_{11}(s) = \frac{V_{i,reflected}}{V_{i,incident}} = \frac{V_i - R_0 I_i}{V_i + R_0 I_i} = \frac{V_i - V_s}{V_s}$$

$$S_{21}(s) = \frac{V_{o,transmitted}}{V_{i,incident}} = \frac{V_o - R_0 I_o}{V_i + R_0 I_i} = \frac{V_o}{V_s}$$

$$S_{22}(s) = \frac{V_{o,reflected}}{V_{o,incident}} = \frac{V_o - R_0 I_o}{V_o + R_0 I_o} = \frac{V_o - V_s}{V_s}$$

$$S_{12}(s) = \frac{V_{i,transmitted}}{V_{o,incident}} = \frac{V_i - R_0 I_i}{V_o + R_0 I_o} = \frac{V_i}{V_s}$$

- S_{11} = Input reflection coefficient
- S_{21} = Forward transmission coefficient
 - Gain w/ input matching dependency
- S_{22} = Output reflection coefficient
 - $1/S_{22}$ = Output return loss
- S_{12} = Reverse transmission coefficient (isolation)

$$S_{21}(s) = [1 + S_{11}(s)]A(s)$$

where $A(s)$ is voltage gain

Next Time

- S-parameter examples
- Impulse response generation
- Communication techniques
 - Eye Diagram
 - Intersymbol interference
 - Modulation techniques