

Texas A&M University
Department of Electrical and Computer Engineering

ECEN 620 – Network Theory (Broadband Circuit Design)

Fall 2025

Exam #1

Instructor: Sam Palermo

- Please write your name in the space provided below
- Please verify that there are 6 pages in your exam
- You may use one double-sided page of notes and equations for the exam
- Good Luck!

Problem	Score	Max Score
1		40
2		60
Total		100

Name: SAM PALERMO

UIN: _____

Problem 1 (40 points)

Select the proper PLL architecture to track a frequency ramp of 10^{12} rad/s^2 with a steady-state phase error of 0.01 rad. Assume that $K_{VCO} = 2\pi \cdot (1\text{GHz/V})$, there is no loop divider ($N=1$), and that the loop filter utilizes a 1nF capacitor. Additional circuitry should be added to the loop filter to achieve a $\zeta=2$. **Give the value of K_{PD} (include correct units), draw the loop filter and label the filter component values.**

A 2nd-order Type 2 PLL is required to track a frequency ramp.

$$E(s) = \frac{s^2}{s^2 + 2\zeta\omega_n s + \omega_n^2}$$

Frequency Ramp: $\Phi_{in}(s) = \frac{1}{s^3}$

$$\phi_{ess} = \lim_{s \rightarrow 0} \frac{1}{s^3} \frac{s \cdot s^2}{s^2 + 2\zeta\omega_n s + \omega_n^2} = \frac{1}{\omega_n^2} = 0.01 \text{ rad}$$

$$\Rightarrow \omega_n = \sqrt{\frac{1}{\phi_{ess}}} = \sqrt{\frac{10^{12} \text{ rad/s}^2}{0.01 \text{ rad}}} = 10^7 \text{ rad/s}$$

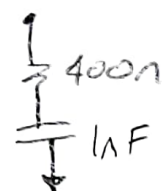
$$\omega_n = \sqrt{\frac{K_{PD} K_{VCO}}{N C}}$$

$$K_{PD} = \frac{\omega_n^2 N C}{K_{VCO}} = \frac{(10^7 \text{ rad/s})^2 (1) (1\text{nF})}{2\pi (1\text{GHz/V})} = \frac{100 \mu\text{A}}{2\pi}$$

$$R = \frac{2\zeta}{\omega_n C} = \frac{2(2)}{(10^7 \text{ rad/s})(1\text{nF})} = 400 \Omega$$

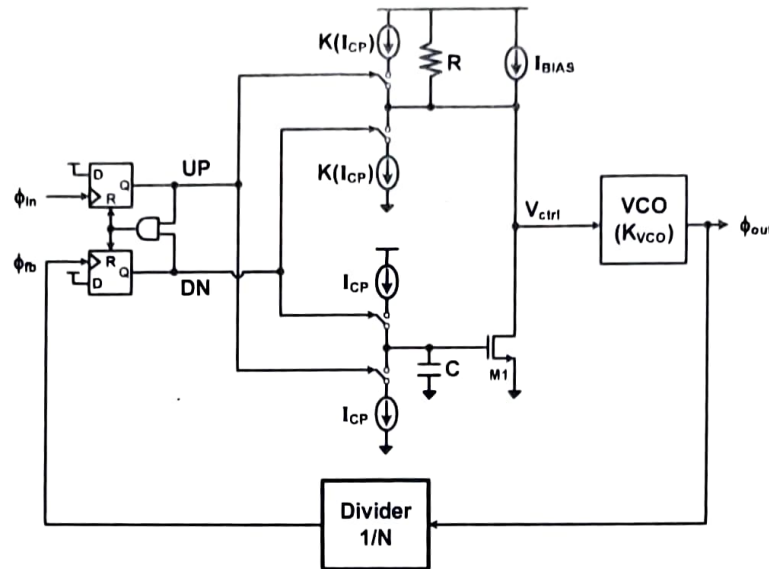
$$K_{PD} = \frac{100 \mu\text{A}}{2\pi}$$

Loop Filter



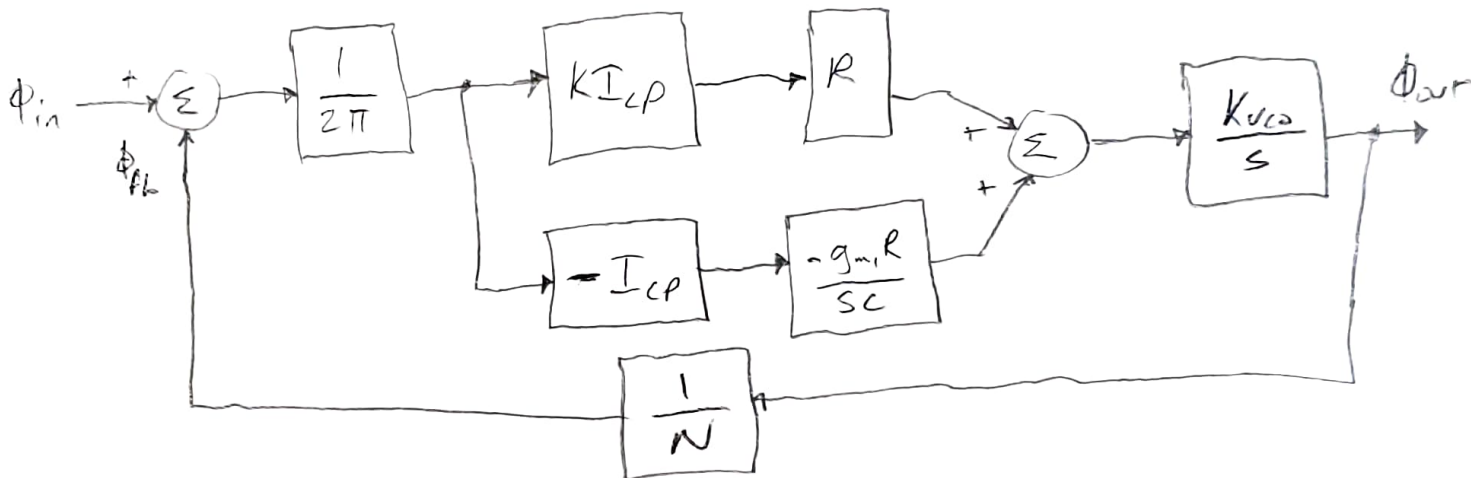
Problem 2 (60 points)

For the PLL shown below, assume that the VCO gain is K_{VCO} is positive, all transistors are operating in saturation with $r_o = \infty$ and you can ignore any transistor device capacitors.



- a) Draw the phase domain small signal model of the loop.
- b) Find the expressions for the product of the forward path gain and feedback factor, $\frac{G(s)}{N}$, and determine the pole-zero locations of $\frac{G(s)}{N}$.

a.



b.

$$\frac{G(s)}{N} = \frac{1}{2\pi} \left[KI_{CP}R + I_{CP} \frac{g_{m1}R}{sC} \right] \left(\frac{K_{VCO}}{s} \right) \left(\frac{1}{N} \right)$$

$$\frac{G(s)}{N} = \frac{KI_{CP}RK_{VCO}}{2\pi} \frac{\left[s + \frac{g_{m1}}{KC} \right]}{s^2 N}$$

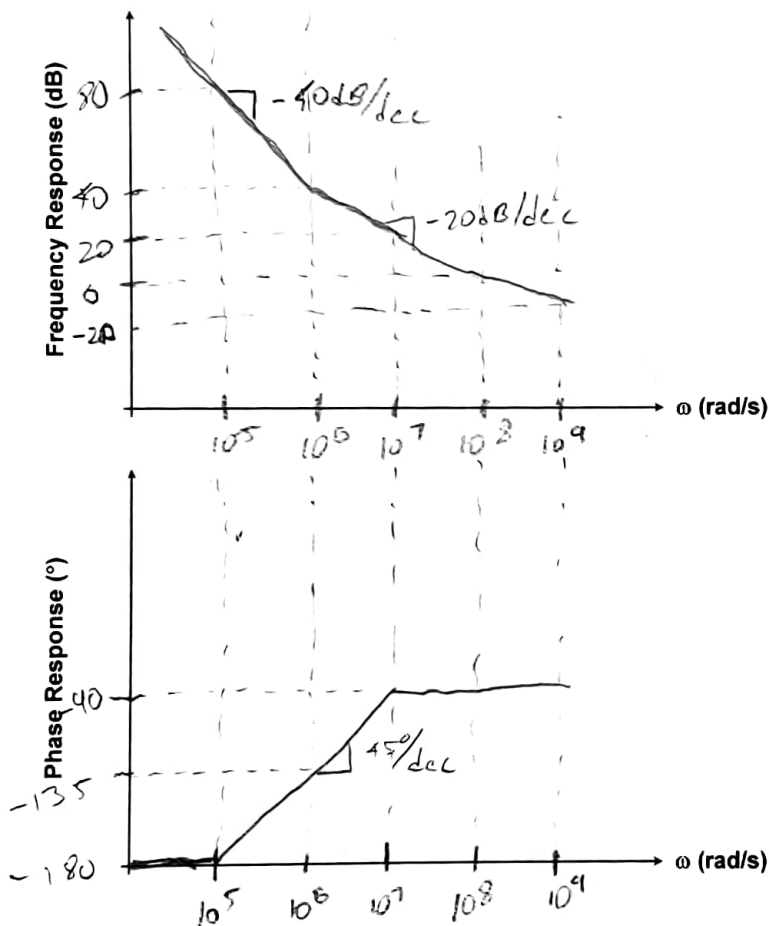
1 zero at $-\frac{g_{m1}}{KC}$
2 poles at ϕ

- c) Assume that $I_{CP}=10\mu A$, $K=10$, $R=50k\Omega$, $K_{VCO}=2\pi*(1GHz/V)$, $g_{m1}=20\mu A/V$ and $N=50$. What is the C value required for the $\frac{G(s)}{N}$ transfer function zero, ω_z , to equal $1Mrad/s$? Sketch the $\frac{G(s)}{N}$ Bode Plot (magnitude and phase). What is the phase margin?

$$|\omega_z| = \frac{g_{m1}}{KC} \Rightarrow C = \frac{g_{m1}}{K|\omega_z|} = \frac{20\mu A/V}{10(1Mrad/s)} = 2pF$$

$$\frac{G(s)}{N} = \frac{10(10\mu A/50k\Omega)(2\pi \cdot 1GHz/V)}{2\pi} \frac{[s + 10^6]}{s^2 50} = \frac{10^8 [s + 10^6]}{s^2}$$

$$At \omega = 10^5 rad/s \quad \left| \frac{G(j\omega)}{N} \right| \approx \frac{10^8 (10^6)}{10^{10}} = 10^4 = 80dB$$



$$C = 2pF$$

$$\text{Phase Margin} = 90^\circ$$

d) What is the phase relationship between ϕ_{in} and ϕ_{fb} when is PLL locked?

The PFD will cause the PLL to lock with a 0° phase difference

$$\phi_{in} - \phi_{fb} = 0^\circ$$