

**Texas A&M University
Department of Electrical and Computer Engineering**

ECEN 325 – Electronics

Spring 2020

Exam #2

Instructor: Sam Palermo

- Please write your name in the space provided below
- Please verify that there are 6 pages in your exam
- Good Luck!

Problem	Score	Max Score
1		30
2		35
3		35
Total		100

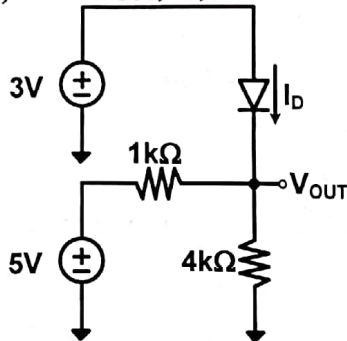
Name: SAM PALERMO

UIN: _____

Problem 1 (30 points)

For all the circuits below, use the constant-voltage-drop diode model ($V_D=0.7V$), $V_T=25.9mV$, and $n=1$.

a) Find V_{OUT} , I_D , and the small signal diode resistance, r_d . (10 points)



If diode is reverse biased

$$V_{OUT} = 4V$$

$$V_D = -1V \text{ and } I_D = 0$$

\Rightarrow Consistent w/ diode model

$$r_d = \frac{V_T}{I_D} = \frac{25.9mV}{0} = \infty$$

$$V_{OUT} = 4V$$

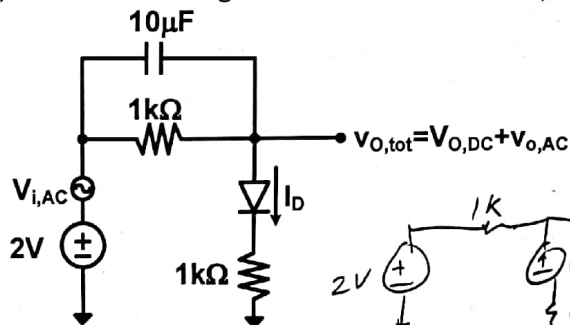
$$I_D = 0$$

$$r_d = \infty$$

The following circuit has a small-signal AC signal, $v_{i,AC}$, in series with a DC voltage.

b) Find the DC output voltage, $V_{O,DC}$, DC diode current I_D , and small-signal diode r_d (10 points)

c) Find the small-signal AC transfer function $v_{o,AC}(s)/v_{i,AC}(s)$ (10 points)



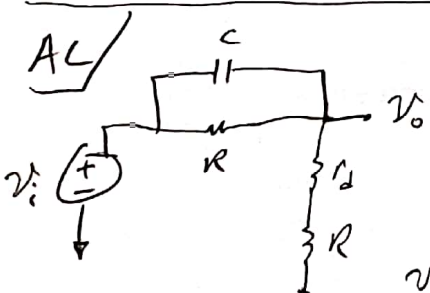
DC If diode is reverse biased,

$$V_{O,DC} = V_D = 2V \Rightarrow \text{Not consistent}$$

diode must be forward biased

$$\frac{V_{OUT} - 2V}{1k} + \frac{V_{OUT} - 0.7V}{1k} = 0 \Rightarrow V_{OUT} = 1.35V$$

$$I_D = \frac{1.35V - 0.7V}{1k} = 650\mu A, r_d = \frac{V_T}{I_D} = \frac{25.9mV}{650\mu A}$$



$$\frac{v_o}{v_i} = \frac{Z_{D1} + Z_R}{Z_C || Z_R + Z_{D1} + Z_R} = \frac{r_d + R}{\frac{1}{sC + 1/R} + r_d + R} = \frac{(sC + \frac{1}{R})(r_d + R)}{1 + sC(r_d + R) + \frac{R}{R}}$$

$$\frac{v_o}{v_i} = \frac{s + \frac{1}{RC}}{s + \frac{1}{[R || (R + r_d)]C}}$$

$$V_{O,DC} = 1.35V$$

$$I_D = 650\mu A$$

$$r_d = 39.8\Omega$$

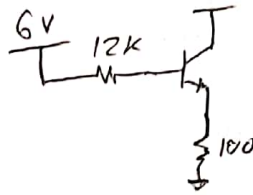
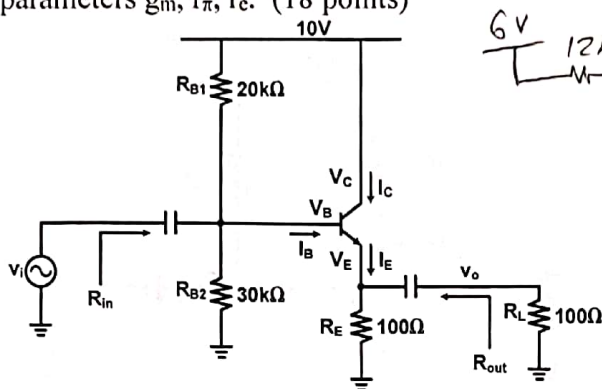
AC Transfer Function:

$$\frac{s + 100}{s + 196}$$

Problem 2 (35 points)

Assume for problem 2 that the transistor $\beta=150$, $V_{BE}=0.7V$, and $V_T=25.9mV$.

a) Calculate the DC values for V_C , V_B , V_E , I_C , I_B , and I_E . Compute the AC small signal parameters g_m , r_{π} , r_e . (18 points)



$I_C = 29.3mA$

$I_B = 196\mu A$

$I_E = 29.5mA$

$V_C = 10V$

$V_B = 3.65V$

$V_E = 2.95V$

$g_m = 1.13 A/V$

$r_{\pi} = 132\Omega$

$r_e = 0.88\Omega$

$I_E = \frac{6V - 0.7V}{100 + \frac{12k}{151}} = 29.5mA$

$I_B = \frac{I_E}{\beta + 1} = 196\mu A$

$I_C = \beta I_B = 29.3mA$

$V_E = 29.5mA (100\Omega) = 2.95V$

$V_B = V_E + 0.7V = 3.65V$

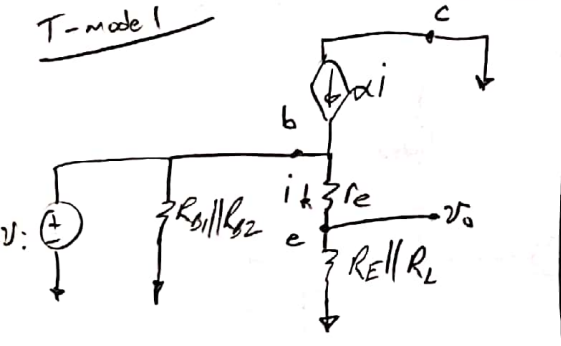
$g_m = \frac{I_C}{V_T} = \frac{29.3mA}{25.9mV} = 1.13 A/V$

$r_{\pi} = \frac{V_T}{I_B} = \frac{25.9mV}{196\mu A} = 132\Omega$

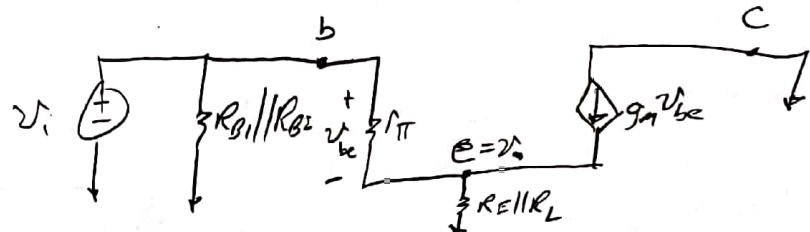
$r_e = \frac{V_T}{I_E} = \frac{25.9mV}{29.5mA} = 0.88\Omega$

b) Sketch the small-signal model of the circuit. Assume that the capacitors act as AC shorts and that the transistor's r_o is infinite (can be neglected). (11 points)

T-model



PI-model



c) Calculate the small signal gain $A_v = v_o/v_i$, the input resistance R_{in} , the output resistance R_{out} . (6 points)

$A_v = \frac{R_E || R_L}{r_e + R_E || R_L} = \frac{100 || 100}{0.88 + 100 || 100} = 0.983$

$R_{in} = R_B || [r_{\pi} + (\beta + 1)(R_E || R_L)]$
 $= 17k || [132 + 151(100 || 100)]$
 $= 4.68k\Omega$

$R_{out} = R_E || r_e + \frac{r_{\pi}}{\beta}$
 $= 100 || 0.88$
 $= 0.87\Omega$

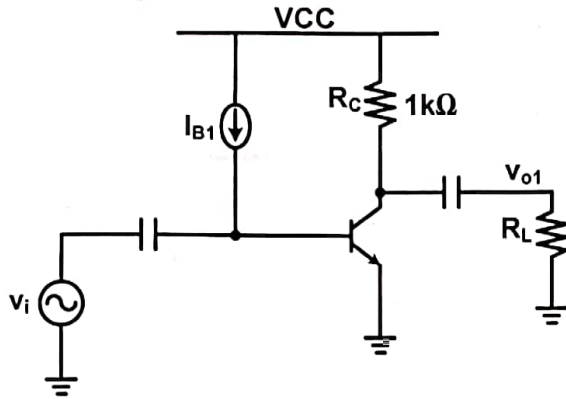
$A_v = 0.983$

$R_{in} = 4.68k\Omega$

$R_{out} = 0.87\Omega$

Problem 3 (35 points)

a) For the following amplifier, assume the transistor $\beta=150$, $r_o=\infty$, and that the transistor is biased such that $g_m=40\text{mA/V}$, $r_e=24.8\Omega$, and $r_\pi=3.8\text{k}\Omega$. Calculate the amplifier gain, $A_{v1}=v_{o1}/v_i$, for two load resistor conditions: $R_L=\infty$ and $R_L=16\Omega$. Recall that an ideal current source has infinite output resistance, ie $R_B=\infty$. Assume that the capacitors act as AC shorts. (6 points)



$$A_v = -g_m (R_C \parallel R_L)$$

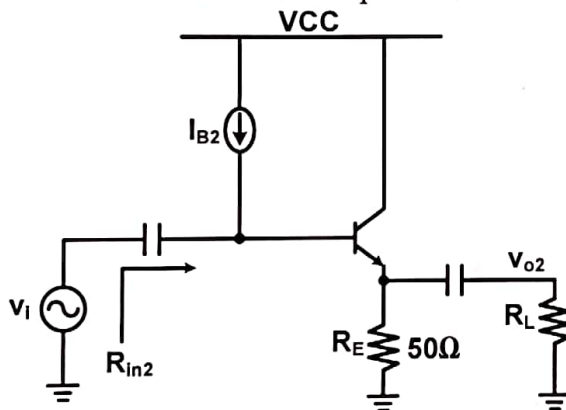
$$w/R_L = \infty \Rightarrow -40\text{mA/V}(1\text{k}) = -40\text{V/V}$$

$$w/R_L = 16 \Rightarrow -40\text{mA/V}(1\text{k} \parallel 16) = -0.63\text{V/V}$$

$$A_{v1}(R_L=\infty) = -40$$

$$A_{v1}(R_L=16\Omega) = -0.63$$

b) For the following amplifier, assume the same transistor bias conditions: $\beta=150$, $r_o=\infty$, and that the transistor is biased such that $g_m=1.93\text{A/V}$, $r_e=0.51\Omega$, and $r_\pi=78\Omega$. Calculate the amplifier gain, $A_{v2}=v_{o2}/v_i$, and the input resistance, R_{in2} , for two load resistor conditions: $R_L=\infty$ and $R_L=16\Omega$. Assume that the capacitors act as AC shorts. (14 points)



$$A_v = \frac{R_E \parallel R_L}{r_e + R_E \parallel R_L}$$

$$w/R_L = \infty \Rightarrow \frac{50\Omega}{0.51 + 50} = 0.99\text{V/V}$$

$$w/R_L = 16 \Rightarrow \frac{50 \parallel 16}{0.51 + 50 \parallel 16} = 0.96\text{V/V}$$

$$A_{v2}(R_L=\infty) = 0.99$$

$$A_{v2}(R_L=16\Omega) = 0.96$$

$$R_{in2}(R_L=\infty) = 7.63\text{k}\Omega$$

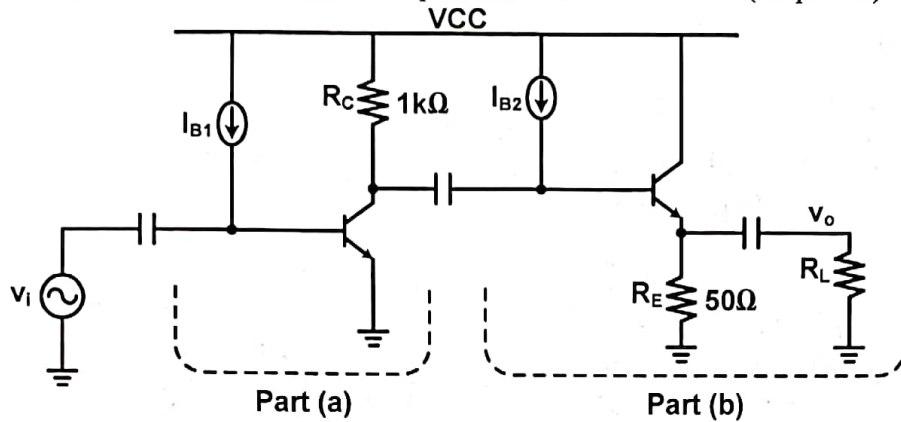
$$R_{in2}(R_L=16\Omega) = 1.91\text{k}\Omega$$

$$R_{in} = r_\pi + (\beta+1)(R_E \parallel R_L)$$

$$w/R_L = \infty \Rightarrow R_{in} = 78 + (151)(50) = 7.63\text{k}\Omega$$

$$w/R_L = 16 \Rightarrow R_{in} = 78 + (151)(50 \parallel 16) = 1.91\text{k}\Omega$$

c) The circuit below consists of the amplifier from part (a) cascaded with the amplifier from part (b). Calculate the total 2-stage amplifier gain, $A_v = v_o/v_i$, for two load resistor conditions: $R_L = \infty$ and $R_L = 16\Omega$. Assume that the capacitors act as AC shorts. (15 points)



$$A_v (R_L = \infty) = -35.0$$

$$A_v (R_L = 16\Omega) = -25.2$$

$$\text{Total } A_v = (-g_{m1}) (R_C \parallel R_{in2}) \left(\frac{R_E \parallel R_L}{r_e + R_E \parallel R_L} \right)$$

$$= -g_{m1} (R_C \parallel R_{in2}) A_{v2}$$

$$w/R_L = \infty \Rightarrow -40 \text{ mA/V} (1\text{k} \parallel 7.63\text{k}) (0.99) = -35.0 \text{ V/V}$$

$$w/R_L = 16 \Rightarrow -40 \text{ mA/V} (1\text{k} \parallel 1.91\text{k}) (0.96) = -25.2 \text{ V/V}$$