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# OP AMP CHARACTERISTICS

## Static op amp limitations

REFERENCE: Chapter 5 textbook

## ERRORS CAUSED BY THE INPUT BIAS CURRENT AND THE INPUT OFFSET CURRENT

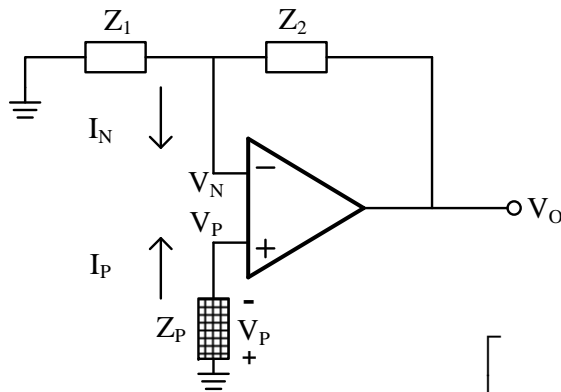
- Op Amp to function should have for the input terminals a DC path through which current can flow.

$$I_B = \frac{I_P + I_N}{2} \quad \text{Input bias current}$$

$$I_{OS} = I_P - I_N \quad \text{Input offset voltage, Ideally } I_{OS} = 0 \text{ but due to mismatch } |I_{OS}| \neq 0$$

i.e., for 741C

$$80\text{nA} \leq I_B \leq 500\text{nA} \quad \text{and} \quad 20\text{nA} \leq |I_{OS}| \leq 200\text{nA}$$



$$V_o = V_P \left( 1 + \frac{Z_2}{Z_1} \right) + Z_2 I_N$$

also since  $V_P = -Z_P I_P$

$$V_o = Z_2 I_N - \left( 1 + \frac{Z_2}{Z_1} \right) Z_P I_P$$

$$E_o = \left( 1 + \frac{Z_2}{Z_1} \right) \left[ \frac{Z_2}{1 + \frac{Z_2}{Z_1}} I_N - Z_P I_P \right] = \left( 1 + \frac{Z_2}{Z_1} \right) \left[ \frac{Z_1 Z_2}{Z_1 + Z_2} I_N - Z_P I_P \right]$$

Note that  $I_N$  and  $I_P$  can be expressed as

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$$I_P = \frac{2I_B + I_{OS}}{2}$$

$$I_N = \frac{2I_B - I_{OS}}{2}$$

Then the output offset voltage can be expressed as

$$E_O = \left(1 + \frac{Z_2}{Z_1}\right) \left[ \left( \frac{Z_1 Z_2}{Z_1 + Z_2} - Z_P \right) I_B - \left( \frac{Z_1 Z_2}{Z_1 + Z_2} + Z_P \right) \frac{I_{OS}}{2} \right]$$

Note that if

$$Z_P = Z_1 // Z_2 = \frac{Z_1 Z_2}{Z_1 + Z_2}$$

Then  $E_O$  becomes

$$E_O \cong - \left(1 + \frac{Z_2}{Z_1}\right) \frac{Z_1 Z_2}{Z_1 + Z_2} I_{OS}$$

- Notice that one can keep the ratio  $Z_2/Z_1$  constant but can reduce the values of  $Z_1$  and  $Z_2$  to minimize  $E_O$ .

Let us discuss another technique to reduce the input offset error.

For any configuration (inverting or non-inverting) one can write

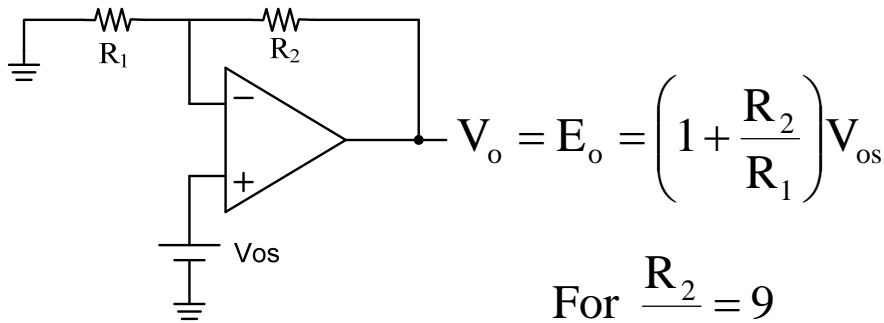
$$v_o = A_s V_i + E_o$$

$$\text{where } A_s = \begin{cases} -R_2/R_1 \\ 1 + R_2/R_1 \end{cases}$$

$$E_o = \left(1 + \frac{R_2}{R_1}\right) [V_{os} - (R_1 // R_2) I_{os}]$$

$$E_o \cong \frac{1}{\beta} E_I \quad \text{where } \frac{1}{\beta} = 1 + \frac{R_2}{R_1}$$

The input offset voltage  $V_{os}$  can be modeled as shown next.

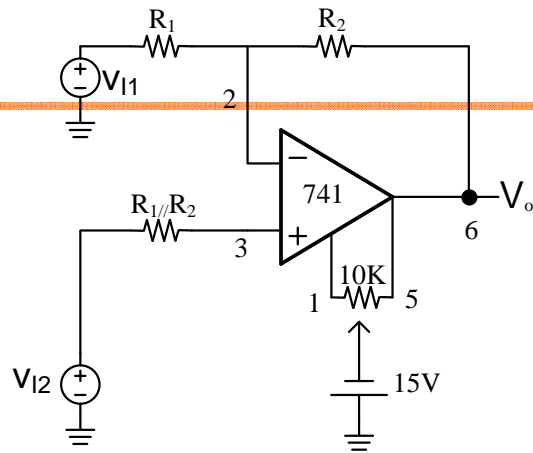


$$\begin{aligned} \text{i.e. } \min V_{os} &= \pm 2\text{mV for a 741} \\ \max V_{os} &= \pm 6\text{mV} \end{aligned}$$

$$\text{For } \frac{R_2}{R_1} = 9$$

Worst case is

$$E_o = 10 \times (\pm 6\text{mV}) = \pm 60\text{mV}.$$



Practical Internal Offset-Error-Nulling.

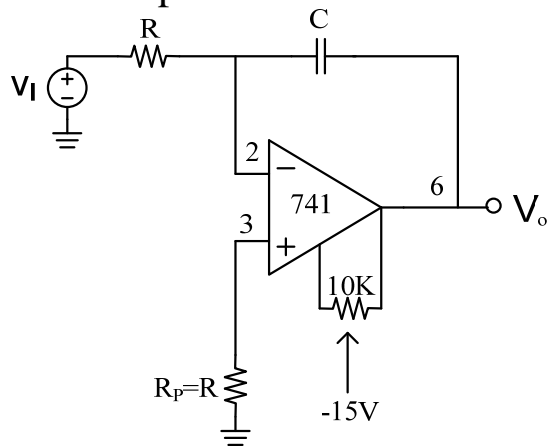
- $E_I$  is the total offset error referred to the output/

$$v_o = -\frac{R_2}{R_1} v_{I1} + \left(1 + \frac{R_2}{R_1}\right) v_{I2} + E_o$$

$$E_o = \left(1 + \frac{R_2}{R_1}\right) (V_{os} - (R_1 // R_2) I_{os})$$

$$E_o = \frac{1}{\beta} E_I$$

Example



$$v_o(t) = -\frac{1}{R_C} \int_0^t [V_I(\xi) + E_I] d\xi + V_o(0)$$

$$E_I = R I_{os} - V_{os}$$

Integrator with Internal Offset-Error Nulling.

# Static op amp limitations

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## Low input bias current op amps

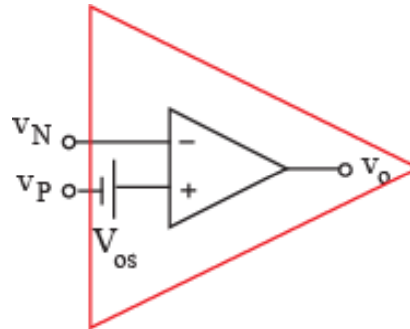
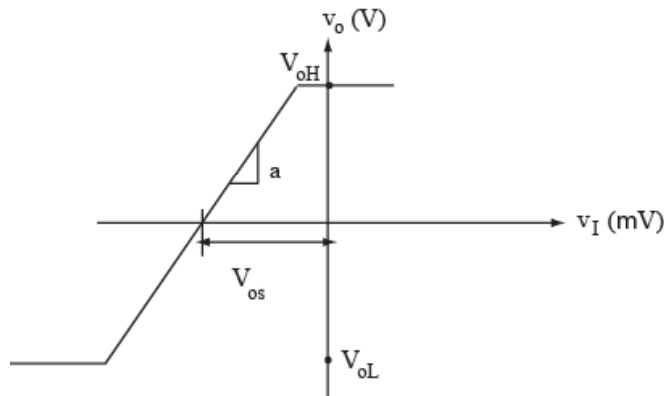
1. *Super-beta input op amps:*  $\beta_F \sim 1000$  !, LM308 ( $I_B = 1\text{ nA}$ )
2. *Input – bias –current cancellation:* Using internal circuitry, OP – 07 ( $I_B = 1\text{ nA}$ ,  $I_{OS} = 0.4\text{ nA}$ )
3. *JFET input op amps:*  $I_G$  in the order of tens of Pico amps. LF 356 BiFET ( $I_B = 30\text{ pA}$ ,  $I_{OS} = 3\text{ pA}$ ), AD549, OPA129: Special JFET +Isolation techniques ( $I_B < 100\text{ fA}$ )
4. *MOSFET input op amps:* Input leakage current is around pA . TLC 279 CMOS ( $I_B = 0.7\text{ pA}$ ,  $I_{OS} = 0.1\text{ pA}$ ),

## Input bias current drift

- For Bipolar op amps increasing the temperature decreases  $I_B$
- For p-n junction (Diode or JFET ):  $I_B(T) \sim I_B(T_0) \cdot 2^{(T - T_0)/10}$
- $T_0$  : Ambient temperature ( $^{\circ}\text{C}$ )
- At high temperatures, there is no advantage in using FET op amps

# Static op amp limitations

## 2 ) Input offset voltage



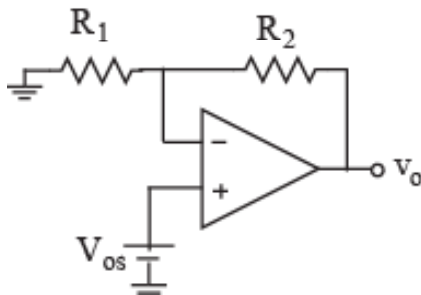
- $V_o = a \cdot (v_P - v_N)$ ;
- By shorting  $v_P$  and  $v_N$ :  $v_o = 0$ ,
- Due to inherent mismatches  $v_o$  is not zero

To force  $v_o$  to zero, a suitable correction voltage must be applied between the input ports.

$$v_o = a \cdot (v_P + V_{os} - v_N) = 0; v_N = v_P + V_{os}$$

Errors caused by  $V_{os}$  :

$$E_o = (1 + (R_2 / R_1)) \cdot V_{os}$$



$R_2 \gg R_1$  : good for measuring  $V_{os}$

# Static op amp limitations

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## Thermal Drift

Temperature coefficient:  $T_c (V_{os}) = d V_{os} / dT$  (mv/°C)

$$V_{os} (T) \sim V_{os} (25^\circ\text{C}) + T_c (V_{os}) \cdot (T - 25^\circ\text{C})$$

## Common Mode Rejection Ratio

We model this phenomena with a change in the input offset voltage due to  $v_{CM}$  variation  
 $1 / CMRR = d V_{os} / d v_{CM}$  ( $\mu\text{V/V}$ ), In practice  $v_{CM} \sim V_P$

## Power Supply Rejection Ration

We model this phenomena with a change in the input offset voltage due to supply variation :  $1 / PSRR = d V_{os} / d V_S$  ( $\mu\text{V/V}$ )

## Changes of $V_{os}$ with output swing

$$\Delta V_{os} = \Delta v_o / a$$



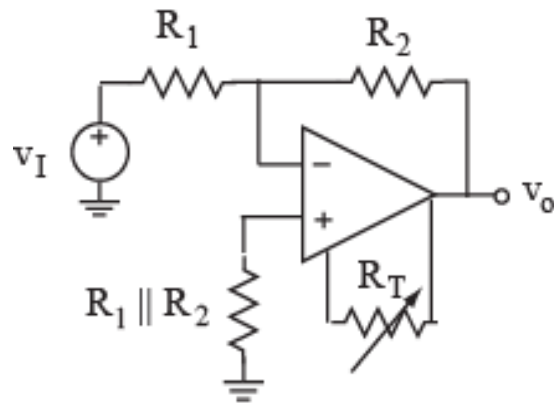
# Static op amp limitations

Summary of effects which generate  $V_{os}$  :

$$V_{os} = V_{os0} + Tc (V_{os}) \cdot \Delta T + (\Delta V_p / CMRR) + (\Delta V_s / PSRR) + (\Delta v_o / a)$$

## 3 ) Input offset –error compensation

Internal offset nulling:



$$E_o = (1 + (R_2 / R_1)) \cdot [ V_{os} - (R_1 \parallel R_2) I_{os} ]$$

$$E_i = V_{os} - (R_1 \parallel R_2) I_{os}$$

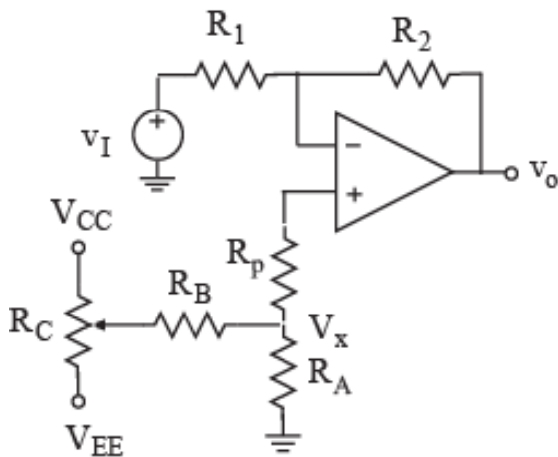
$E_i$  can be nulled by using a suitable trimmer, a smart designer tries to minimize  $E_i$  by a combination of circuit tricks (scaling, op amp selection, etc). The last choice would be trimming.

# Static op amp limitations

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## External offset nulling:

Does not introduce any additional imbalance to the input stage, no degradation drift CMRR, PSRR



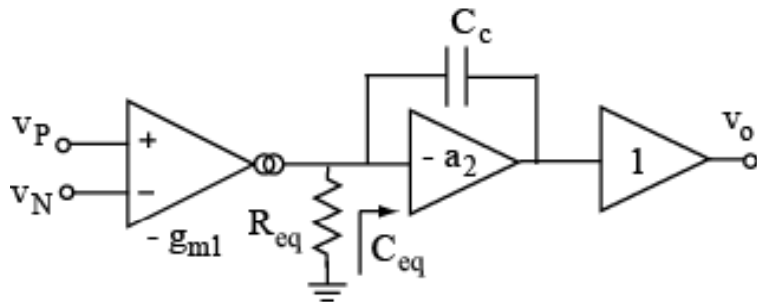
Input Error:  $E_I + V_x$

$R_B \gg R_C$  (Excessive loading of the wiper)

$R_A \ll R_P$  (Avoid perturbing)

## 1 ) Open-loop response

**Dominant pole response:**



**Low frequencies:**  $v_o = g_{m1} R_{eq} a_2 (v_P - v_N)$

**Higher frequencies: Low pass filter action**

$$f_b = \frac{1}{2\pi R_{eq} C_{eq}} \quad (\text{dominant pole frequency})$$

$C_{eq} \longrightarrow$  Very big for integration

$C_{eq} = (1 + a_2) \cdot C_c \longrightarrow$  Miller Effect

**Expression for open-loop response:**

$$a(jf) = \frac{a_0}{1 + j(f/f_b)}$$

$$|a(jf)| = \frac{a_0}{[1 + (f/f_b)^2]^{1/2}}$$

$f_t$  : unity gain freq.

$$f_t = a_0 f_b$$

$$(f_b \ll f_t)$$

$a_0$  : open-loop DC gain

$$\angle a(jf) = -\tan^{-1}(f/f_b)$$

The open-loop response has higher order poles and zeroes, but the dominant pole frequency is chosen deliberately low to ensure that gain has dropped well below unity and the effect of higher order roots can be ignored

# Dynamic op amp limitations

## Dominant pole response:

$a(jf) \rightarrow -j(f_t / f)$  ; Integrator

$(f \gg f_b)$

$GBP = f_t = \text{Const.}$

- For general –purpose type op amps:  $500 \text{ kHz} < GBP < 20 \text{ MHz}$
- $a_0$  and  $f_b$  are ill-defined because of  $R_{eq}$  and  $a_2$  due to manufacturing process variations.  $f_t$  is more practical parameter.

$$v_o \sim \frac{1}{2 \pi j f C_c} g_{m1} (v_P - v_N) \quad f_t = \frac{g_{m1}}{2 \pi C_c} = \frac{I_A}{8 \pi V_T C_c}$$

Stable, predictable values of  $I_A$  and  $C_c$

$$a(jf) = \frac{g_{m1}}{2 \pi j f C_c} = -j(f_t / f)$$

## Graphical visualization of loop-gain:

$$T(jf) = a(jf) \cdot (1/\beta)$$

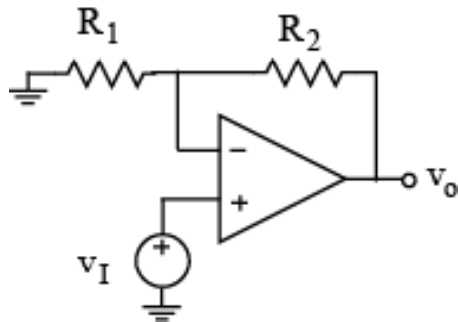
$$|T|_{dB} = |a|_{dB} - |1/\beta|_{dB}$$

$$\angle T = \angle a - \angle(1/\beta)$$

# Dynamic op amp limitations

## 2 ) Closed-loop response

**Non- inverting Amplifier:**



$$A(jf) = \left(1 + \frac{R_2}{R_1}\right) \cdot \frac{1}{1 + \left[\left(1 + \frac{R_2}{R_1}\right) / a(jf)\right]}$$

$$A(jf) = \frac{A_0}{1 + j(f/f_B)}$$

$$A_0 = \left(1 + \frac{R_2}{R_1}\right) \cdot \frac{1}{1 + \left[\left(1 + \frac{R_2}{R_1}\right) / a_0\right]} \sim \left(1 + \frac{R_2}{R_1}\right)$$

$$f_B = f_b (1 + a_0 \beta) \sim \beta \cdot f_t ; f_B : \text{Closed loop bandwidth}$$

- a)  $|T| \gg 1$  ,  $A \sim A_{ideal}$
- b)  $|T| = 1$  ,  $\text{phase}(T) = -90^\circ$  ,  $A = A_{ideal} / (1 + j)$
- c)  $|T| \ll 1$  ,  $A \sim A_{ideal} \cdot T = a$

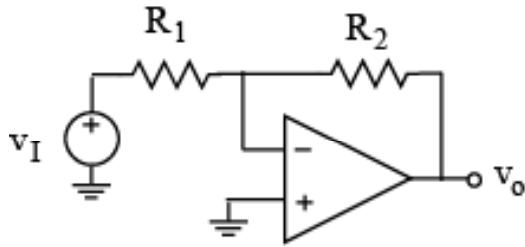
Negative feedback reduces gain from  $a_0$  to  $A_0$  ( $A_0 \ll a_0$ ), but widens the bandwidth from  $f_b$  to  $f_B$  ( $f_b \gg f_B$ ).

**Gain – Bandwidth trade off:**

$$GBP = |A_0| \cdot f_B = f_t$$

# Dynamic op amp limitations

## Inverting Amplifier:



$$A(jf) = \frac{A_0}{1 + j(f/f_B)} \quad A_0 \sim -\frac{R_2}{R_1} \quad f_B \sim \beta \cdot f_t$$

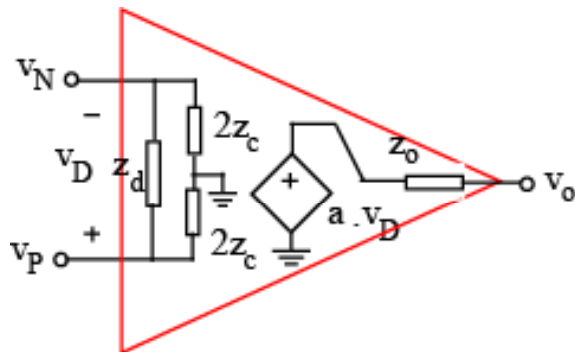
Gain – Bandwidth trade off:

$$GBP = |A_0| \cdot f_B = (R_2 / R_1) \cdot f_t \cdot (R_1 / (R_1 + R_2)) = (1 - \beta) \cdot f_t$$

Non-inverting unity gain amplifier :  $GBP = f_t$

Inverting unity gain amplifier :  $GBP = 0.5 f_t$

## 3) Output and input impedances

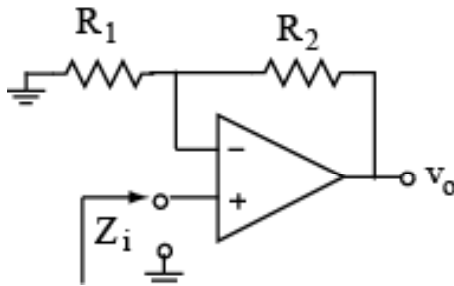


- $z_d, z_o$  are capacitive or inductive
- $z_c$ , common mode input impedance
- Data sheets provide  $r_d, r_o, r_c$
- Some times  $C_d, C_c$  information is provided

$Z \sim z (1 + T)$  (series) or  $Z \sim z (1 + T)^{-1}$  (shunt)  
By decreasing  $T$  at higher frequencies the series impedance is more capacitive and the shunt Impedance is more inductive

# Dynamic op amp limitations

## Input series impedance:



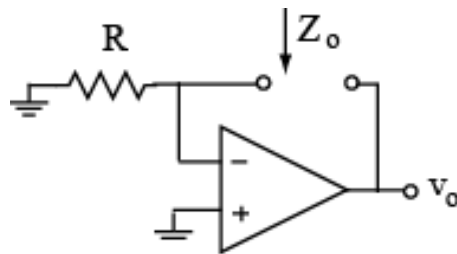
$$Z_d \sim z_d (1 + a \beta)$$

$$Z_d \sim r_d (1 + a_0 \beta) \frac{1 + j(f/f_B)}{1 + j(f/f_b)}$$

$$|T| \gg 1, Z_d \sim r_d (1 + a_0 \beta)$$

$$|T| = 0, Z_d \sim r_d$$

## Output series impedance:



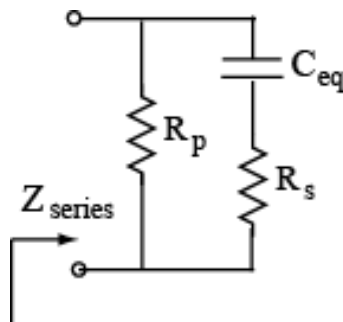
$$Z_o \sim R (1 + a)$$

$$Z_o \sim R (1 + a_0) \frac{1 + j(f/f_t)}{1 + j(f/f_b)}$$

$$|T| \gg 1, Z_o \sim R (1 + a)$$

$$|T| = 0, Z_o \sim R$$

## Equivalent Circuit



### Input

$$\text{Low freq.} \rightarrow R_p = (2 z_c) \parallel [r_d (1 + a_0 \beta)]$$

$$\text{High freq.} \rightarrow R_p \parallel R_s = r_d \text{ OR } R_s \sim r_d$$

$$|Z_{Ceq}(jf_B)| = r_d \rightarrow C_{eq} = \frac{1}{2 \pi f_B r_d}$$

### Output

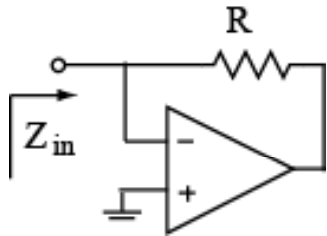
$$\text{Low freq.} \rightarrow R_p \sim R (1 + a_0)$$

$$\text{High freq.} \rightarrow R_s \sim R$$

$$C_{eq} = \frac{1}{2 \pi f_t R}$$

# Dynamic op amp limitations

## Input shunt impedance:



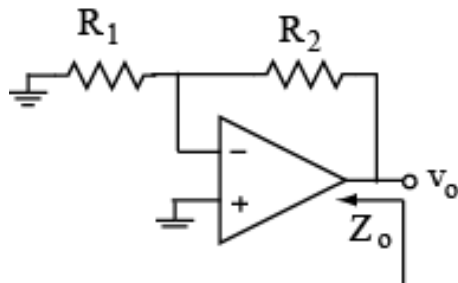
$$Z_i \sim R / (1 + a)$$

$$Z_i \sim [R / (1 + a_0)] \frac{1 + j(f / f_b)}{1 + j(f / f_t)}$$

$$|T| \gg 1, Z_i \sim R / (1 + a_0)$$

$$|T| = 0, Z_o \sim R$$

## Output shunt impedance:



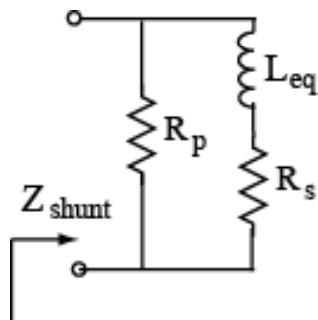
$$Z_o \sim r_o / (1 + a \beta)$$

$$Z_o \sim [r_o / (1 + a_0 \beta)] \frac{1 + j(f / f_b)}{1 + j(f / f_B)}$$

$$|T| \gg 1, Z_o \sim r_o / (1 + a_0 \beta)$$

$$|T| = 0, Z_o \sim r_o$$

## Equivalent Circuit



### Output

Low freq.  $\rightarrow R_p = r_o$

High freq.  $\rightarrow R_p \parallel R_s \sim R_s = r_o / (1 + a_0 \beta)$

$$|Z_{Leq}(jf_B)| = r_o \rightarrow L_{eq} = \frac{r_o}{2 \pi f_B}$$



# Dynamic op amp limitations

## 4 ) Transient response

Examining the transient response to a step signal

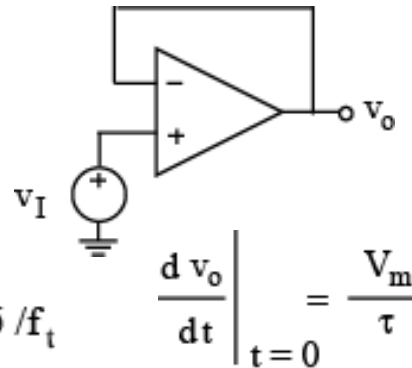
### Rise Time ( $t_R$ )

$$A(jf) = \frac{A_0}{1 + j(f/f_t)} \rightarrow \text{Voltage Follower}$$

$$v_I(t) = S(t) \rightarrow v_o(t) = V_m(1 - \exp(-t/\tau))$$

$$\tau = 1 / (2 \pi f_t)$$

$$t_R = \tau (\ln(0.9) - \ln(0.1)) = 0.35 / f_t$$



$t_R$  : time for  $V_o$  to swing from 10% to 90% of  $V_m$ :

### Slew –Rate limiting

- Above a certain step – amplitude the output slope saturates at a constant value named slew-rate and the output waveform is a ramp
- Slew rate limiting is a nonlinear effect that stems from the limited ability by the internal circuitry to charge or discharge the frequency compensation capacitor  $C_c$

# Dynamic op amp limitations

$$\frac{V_{om(crit.)}}{\tau} = S.R. \quad V_{om(crit.)} = \frac{S.R.}{2\pi f_t}$$

Generalization for  $\beta < 1$ :  $f_t \rightarrow \beta \cdot f_t$

## Full - Power Bandwidth :

The maximum frequency at which the op amp will yield an undistorted AC output With the largest possible amplitude.

$$V_o(t) = V_{om} \cdot \sin(2\pi f t) \quad \left. \frac{dV_o}{dt} \right|_{Max} = 2\pi f V_{om} = S.R.$$

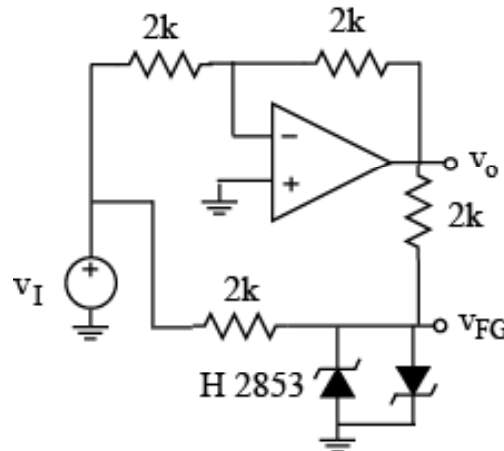
$$F.P.B = \frac{S.R.}{2\pi V_{sat}}$$

## Settling time ( $t_s$ )

The time it takes for the response to a large input signal to settle and remain within Specified error band (0.1% and 0.01% of a 10 V input step).

## Test Circuit for $t_s$

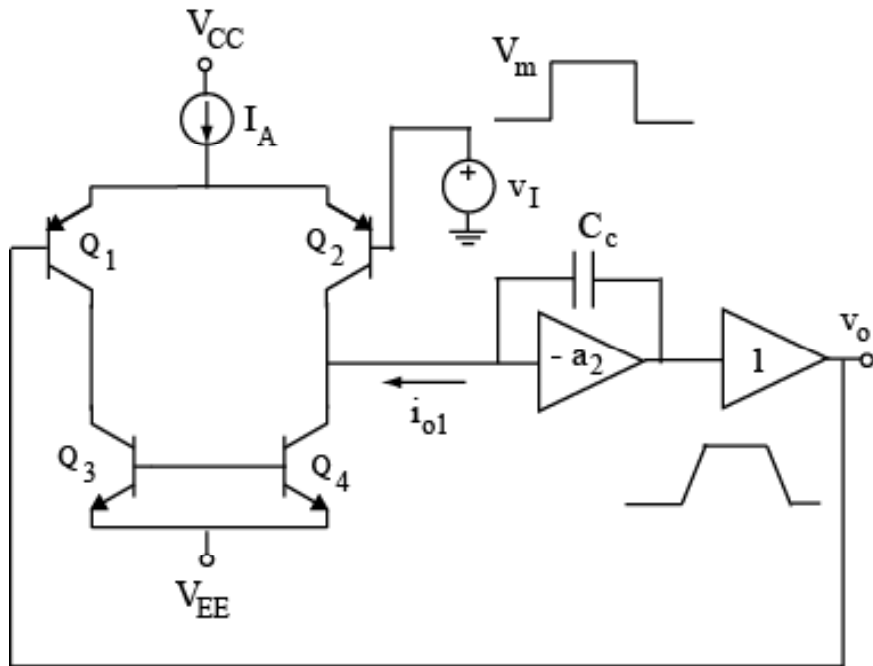
$$v_{FG} = (1/2)(v_I + v_o) = 0$$



Fast  $t_s$  is desirable in high speed, high accuracy D-A converters, S & H circuits and multiplexed amplifiers

# Dynamic op amp limitations

## Slew rate limiting – causes and cures



$V_m$  small; input stage in linear region:

$$i_{o1} = g_{m1} V_m$$

$$\frac{dv_o}{dt} = \frac{g_{m1} V_m}{C_c}$$

By overdriving input stage  $i_{o1}$  saturates at  $I_A$  and  $C_c$  is current starved.

$$\left. \frac{dv_o}{dt} \right|_{\text{Max}} = \frac{I_A}{C_c} = \text{S.R.}$$

$$f_t = \frac{g_{m1}}{2\pi C_c} \rightarrow \text{S.R.} = \frac{I_A (2\pi f_t)}{g_{m1}}$$

During slew-rate limiting,  $v_N$  may depart from  $v_P$  (input stage saturation).

Three different ways of improving S.R. :

- (1) Increasing  $f_t$  (reducing  $C_c$ )
- (2) Reducing  $g_m$
- (3) Increasing  $I_A$