



The Flipped Voltage Follower (FVF)

**A useful cell for low-voltage,
low-power circuit design**



part of this material was provided by Profs. [A.Torralba](#)¹ [J. Ramírez-Angulo](#)²,
[R.G.Carvajal](#)¹, [A. López-Martín](#)³,

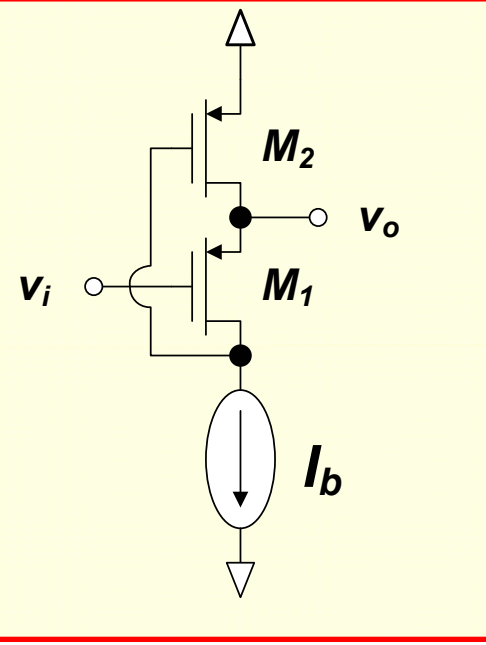
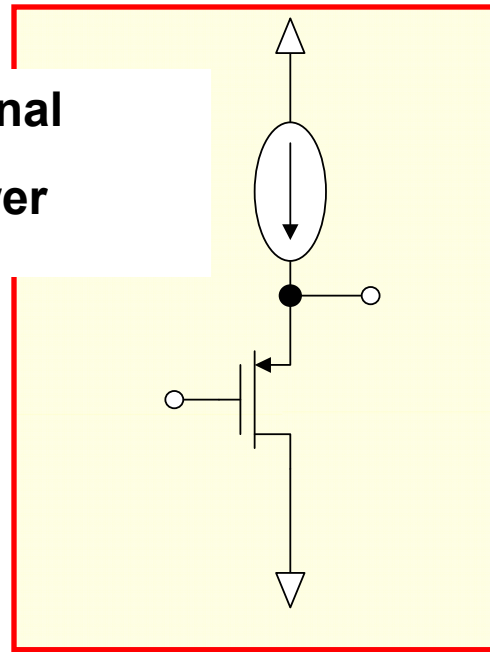
OUTLINE



1. Introduction.
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4. Applications.
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The Basic Flipped Voltage Follower (FVF)

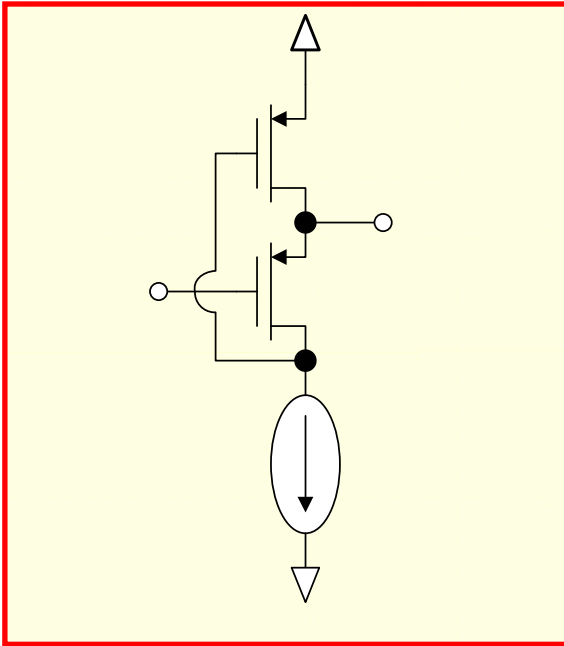
a) Conventional Voltage Follower



b) (FVF)

	Sourcing	Sinking	A_v	g_{out}
a) Conventional	I_b	HIGH	< 1	gm_1
b) FVF	HIGH	I_b	$= 1$	$gm_1 gm_2 ro_1$

[Ramirez-Angulo'92] J.Ramírez-Angulo, R.G.Carvajal, A.Torralba, J.Galán, A.P.VegaLeal, and J.Tombs. "The Flipped Voltage Follower: a useful cell for low-voltage low power circuit design," Proc. ISCAS'02, vol. 3, pp. 615-618, 2002.



FVF transistors
voltage limits to keep
them in saturation

V_i

Assuming that transistor M_1 is in saturation, and neglecting second-order effects, the condition of saturation for transistor M_2 is given by

$$V_{SDM2} = V_{DD} - \left(V_i + |V_{TP}|_{M1} + \sqrt{\frac{2I_o}{k_P \left(\frac{W}{L}\right)_{M1}}} \right) > \sqrt{\frac{2I_o}{k_P \left(\frac{W}{L}\right)_{M2}}} \quad (2)$$

where I_o is the drain current (I_b in this case), $k_P = \mu_P C_{ox}$, and V_{TP} is the transistor threshold voltage. In the same way, assuming that transistor M_2 is biased in saturation, the condition of saturation for transistor M_1 is given by the following relation:

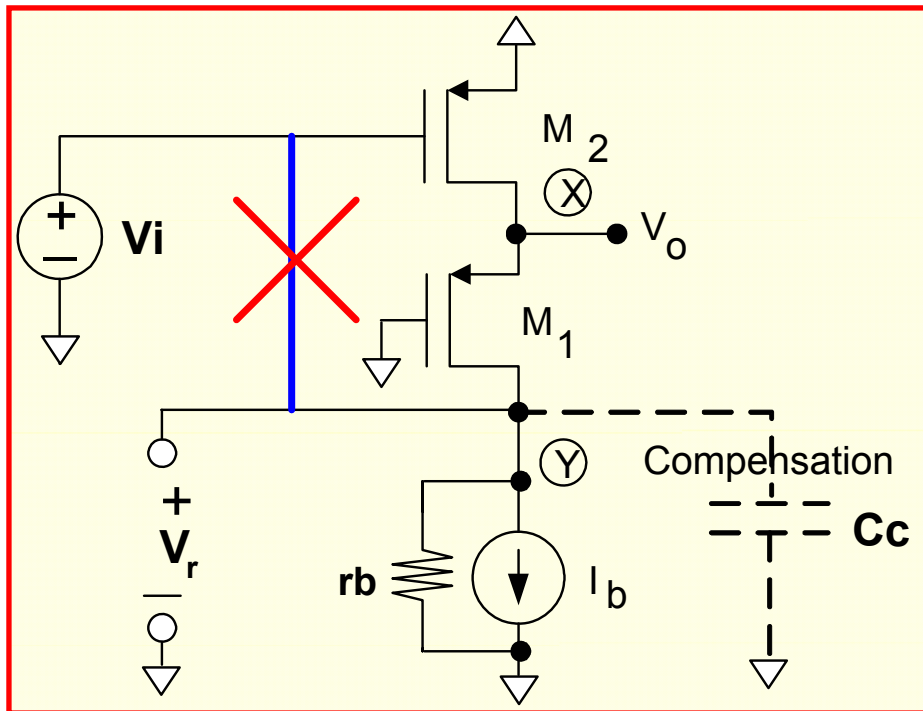
$$V_{SGM1} - V_{SDM1} = V_{DD} - \left(|V_{TP}|_{M2} + \sqrt{\frac{2I_o}{k_P \left(\frac{W}{L}\right)_{M2}}} \right) - V_i < |V_{TP}|_{M1}. \quad (3)$$

Although the linear region of operation is still valid for transistors M_1 and/or M_2 in certain applications, we will limit ourselves to the saturation region in this analysis. Therefore, the valid region of operation for the input signal is limited by

$$\begin{aligned} |V_{TP}|_{M1} + \sqrt{\frac{2I_o}{k_P}} \left(\sqrt{\frac{1}{\left(\frac{W}{L}\right)_{M1}}} + \sqrt{\frac{1}{\left(\frac{W}{L}\right)_{M2}}} \right) < V_{DD} - V_i \\ < |V_{TP}|_{M1} + |V_{TP}|_{M2} + \sqrt{\frac{2I_o}{k_P}} \sqrt{\frac{1}{\left(\frac{W}{L}\right)_{M2}}}. \end{aligned} \quad (4)$$

The Basic FVF Analysis

Open Loop Analysis



C_X parasitics at node X (incl. LOAD)

C_Y parasitics at node Y (incl. C_c if any)

Dc gain

$$A_{OL} = V_r / V_i = -g_{m2} R_{OLY}$$

$$R_{OLY} = r_b \parallel g_{m1} r_{o1} r_{o2},$$

$$R_{OLX} \approx (1+r_b/r_{o1})/g_{m1} \parallel r_{o2}$$

Dominant Pole

$$\text{At Y: } \omega_{pY} = 1 / C_Y R_{OLY}$$

Non-Dominant Pole

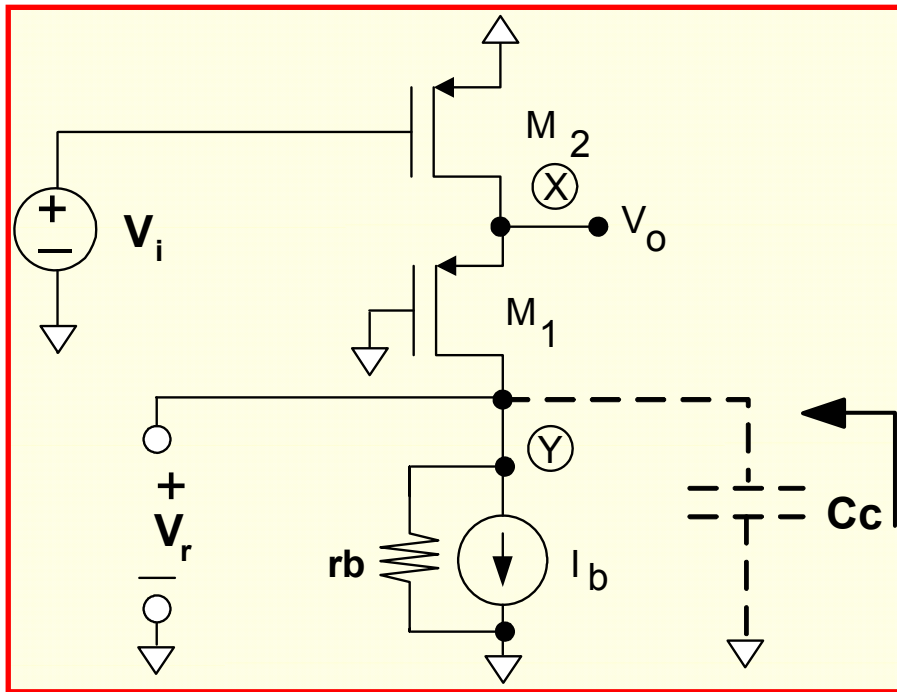
$$\text{At X: } \omega_{pX} = 1 / C_X R_{OLX}$$

Gain-Bandwidth Product

$$GB = g_{m2} / C_Y$$

2. The Basic FVF

Stability Analysis



C_X parasitics at node X (incl. LOAD)
 C_Y parasitics at node Y (incl. C_c if any)

Stability Criterion: $\omega_{pX} > 2 \text{ GB}$

$$\omega_{pX} = 1 / C_X R_{OLX}$$

- For I_b a simple current mirror ($r_b \approx r_{o1}$)

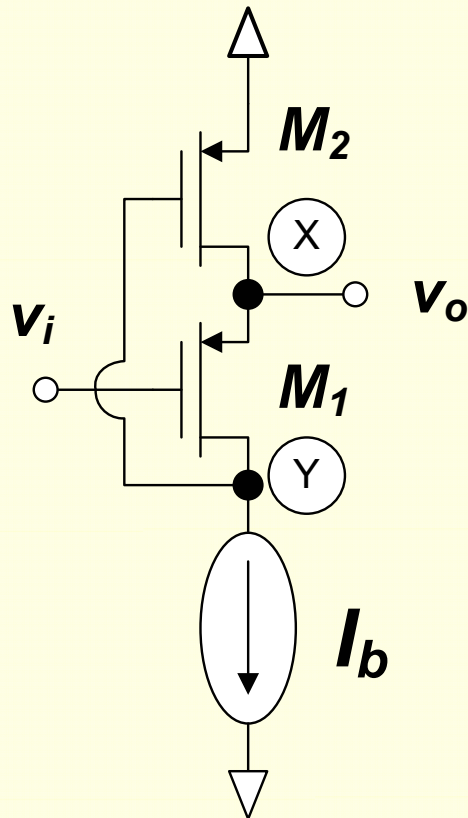
$$\frac{C_X}{C_Y} < \frac{gm_1}{4gm_2}$$

- For I_b a cascode current mirror ($r_b \approx gm_1 r_{o1} r_{o2}$)

$$\frac{C_X}{C_Y} < \frac{1}{gm_2 r_{o2}}$$

usually requires compensation

The Basic FVF



Closed Loop Output Resistance

$$R_{CLX} = \frac{R_{OX}}{1 + |A_{OL}|} \approx \frac{1}{gm_1} \left(1 + \frac{r_b}{ro_1} \right) \parallel ro_2$$

- For I_b a simple current mirror ($r_b \approx ro_1$)

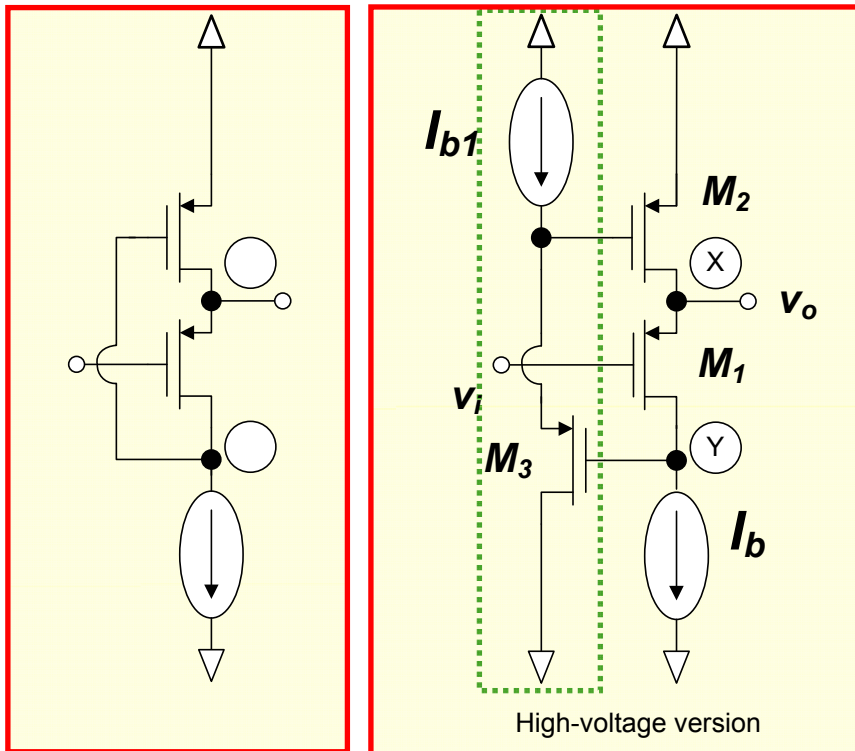
$$R_{CLX} \rightarrow \frac{2}{gm_1 gm_2 ro_1}$$

- For I_b a cascode current mirror ($r_b \approx gm_1 ro_1 ro_2$)

$$R_{CLX} \rightarrow \frac{1}{gm_1 gm_2 ro_1}$$

$A_{CL} \approx 1$ and R_{CLX} is only a few Ohms (20 – 100) in all cases

The Basic FVF

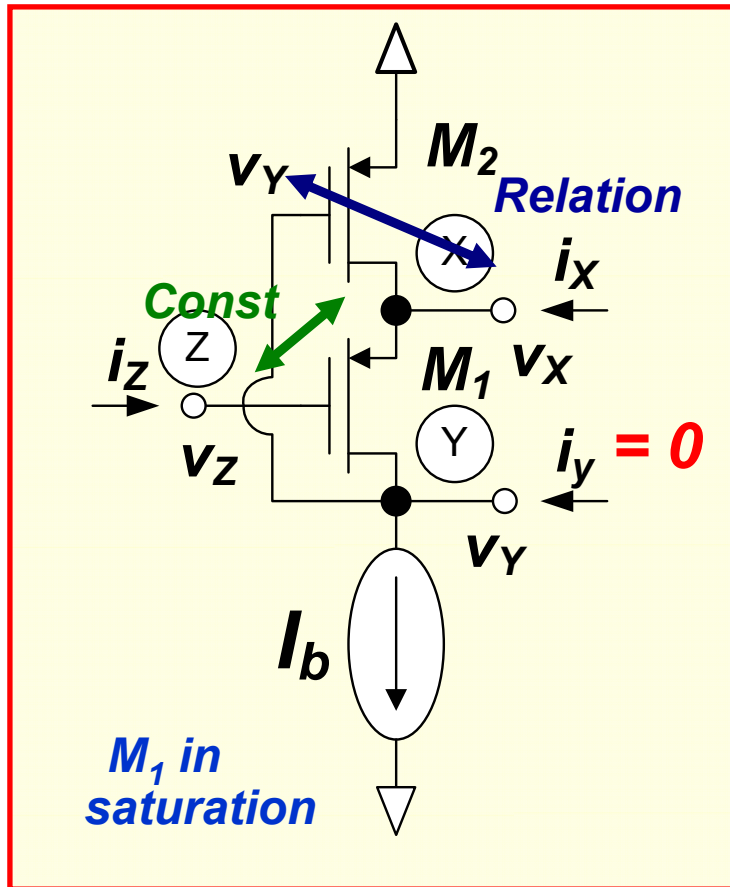


DC considerations

- $V_{DD}^{MIN} = V_{GS}^{MIN} + V_{DS}^{sat} \approx 0.8 \text{ V}$ for $0.6\mu\text{m}$ CMOS technology. It is a low-voltage cell.
- But, for large V_{DD} , biasing M_2 in saturation is difficult for low v_i . A high-voltage version includes a voltage shifter in the feedback loop [Chung-Chih'95]

[Chung-Chih'95] H.Chung-Chih, H.Changku, M. Ismail, "CMOS low-voltage rail-to-rail V-I converter," Proc. 38th MWSCAS, vol.2, pp. 1337-1340, 1995.

The Basic FVF



3-terminal cell (strong inv.)

$$v_X = v_Z + f(I_b, i_Y)$$

$$v_Y = g(I_b, i_X, i_Y, v_Z) \quad ; \quad f(I_b, i_Y) = |V_{Tp}| + \sqrt{\frac{2(I_b - i_Y)}{k_p (W/L)_{M_1}}}$$

$$i_Z = 0$$

- **For M_2 in saturation**

$$g(I_b, i_X, i_Y, v_Z) = V_{DD} - |V_{Tp}| - \sqrt{\frac{2(I_b - i_Y - i_X)}{k_p (W/L)_{M_2}}}$$

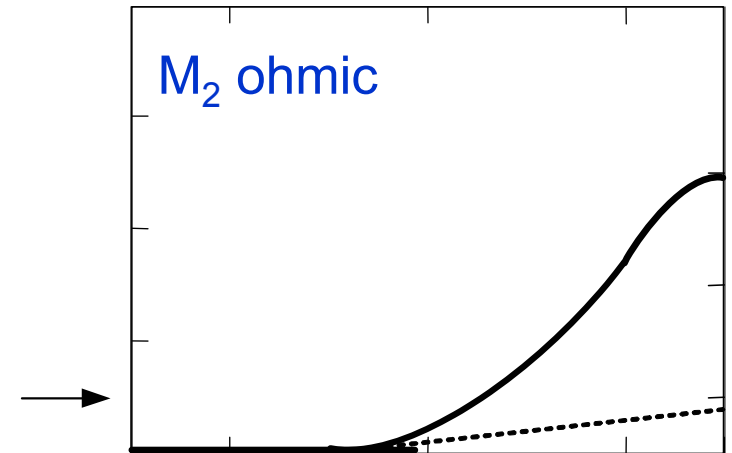
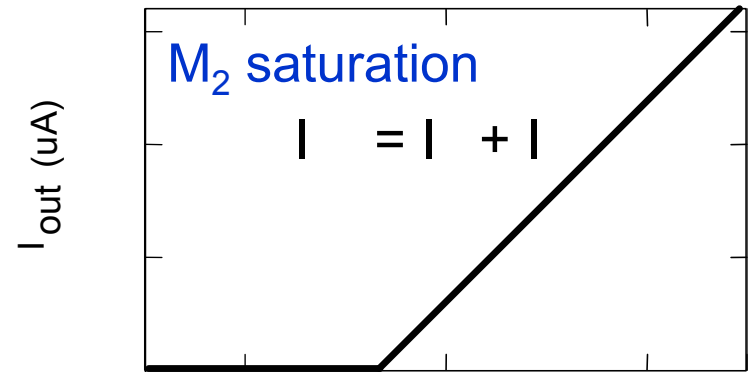
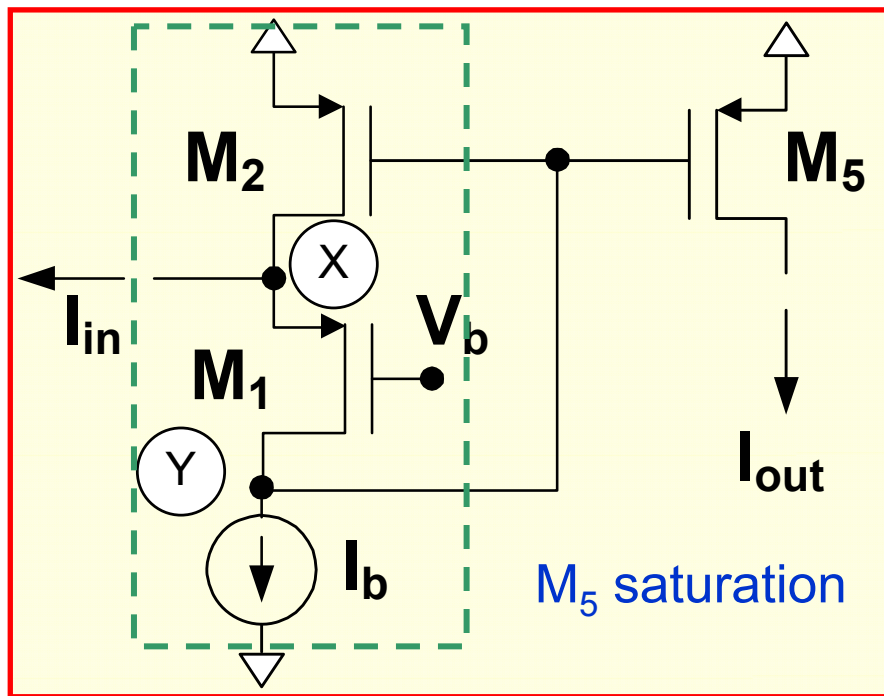
- **For M_2 in ohmic**

$$g(I_b, i_X, i_Y, v_Z) = V_{DD} - |V_{Tp}| - \frac{v_X}{2} - \frac{I_b - i_Y - i_X}{k_p (W/L)_{M_2}} \cdot \frac{1}{v_X}$$

The most interesting case is for $i_Y = 0$

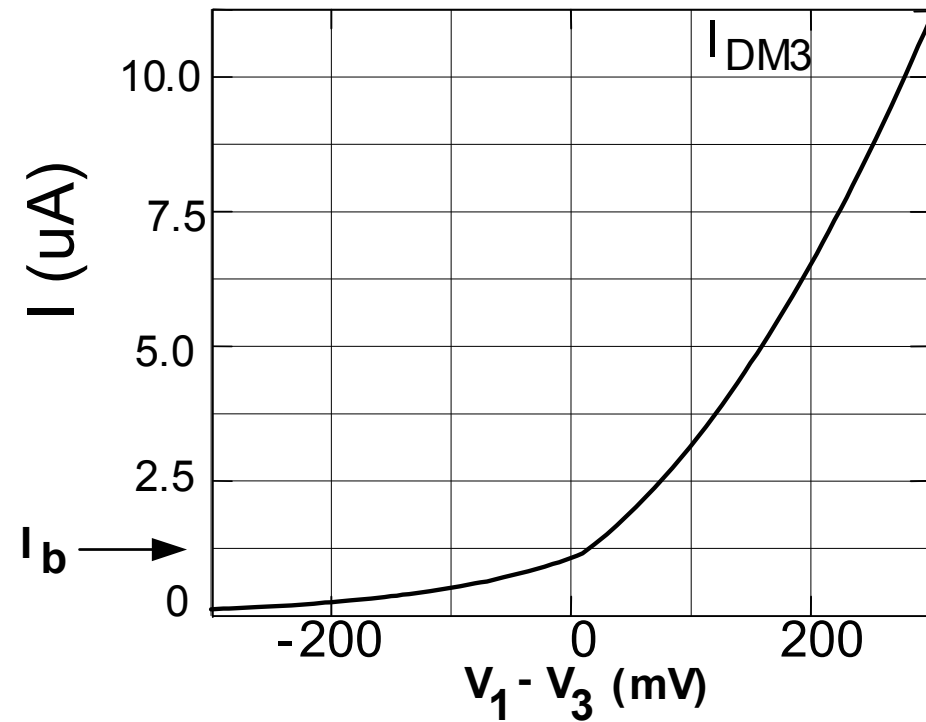
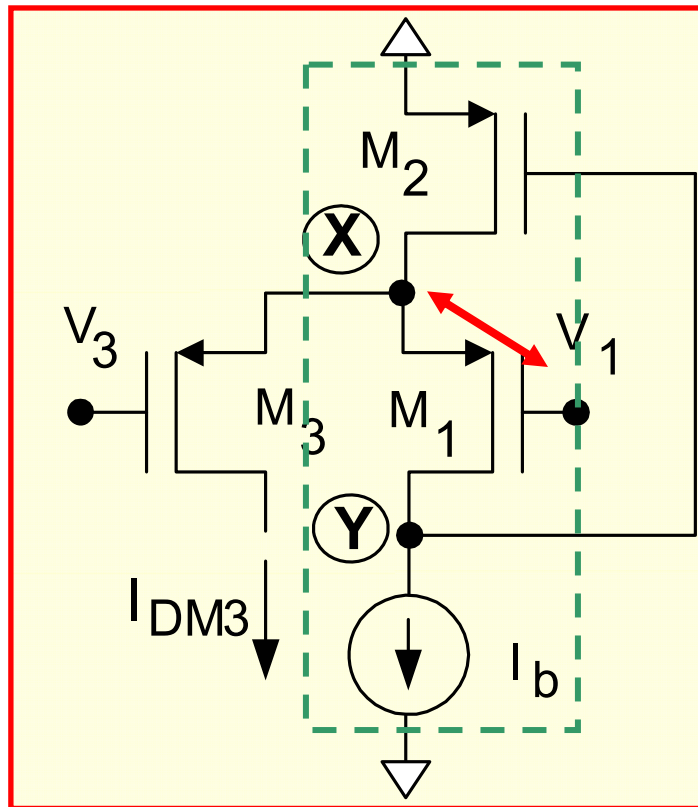
FVF Structures for different applications

Current sensor (FVF-CS)



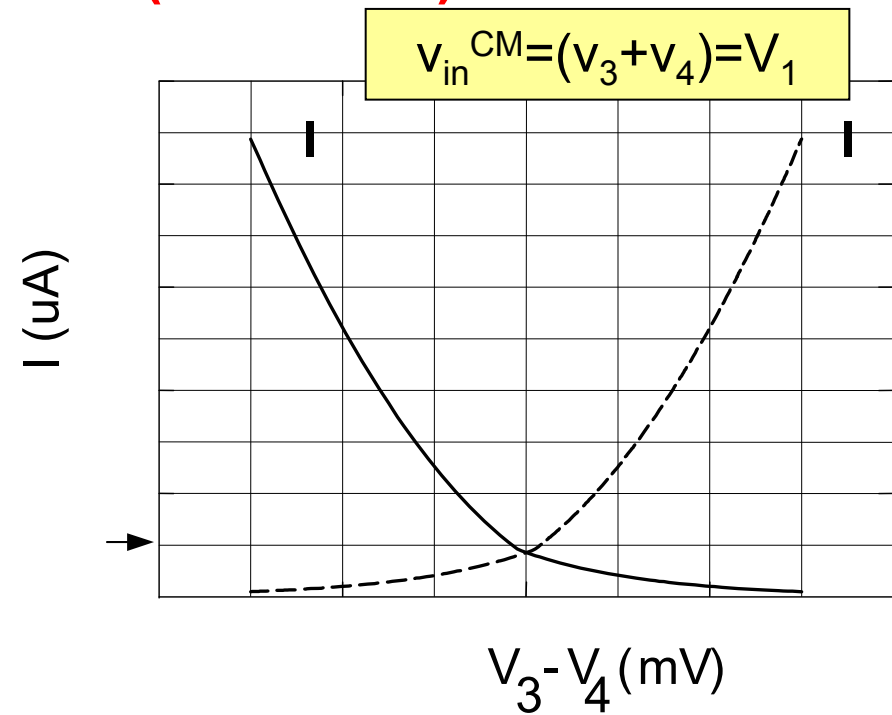
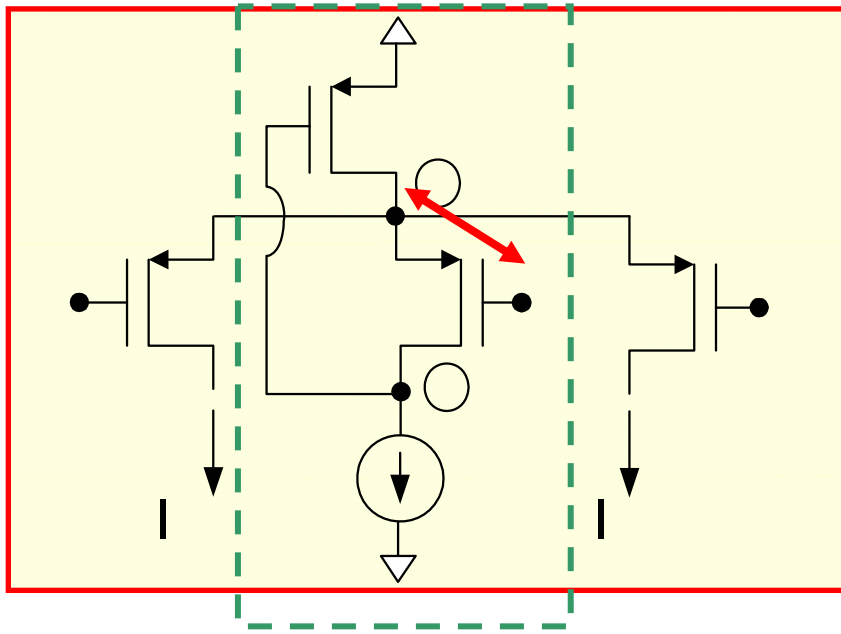
FVF Structures

Non-Symmetrical Class-AB Differential Pair (FVF-NDP)

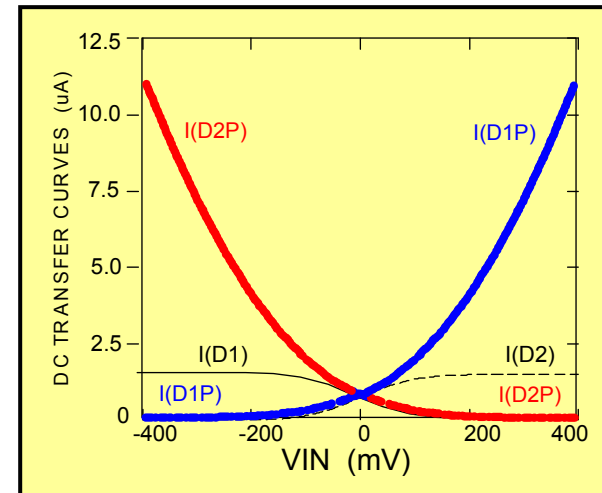
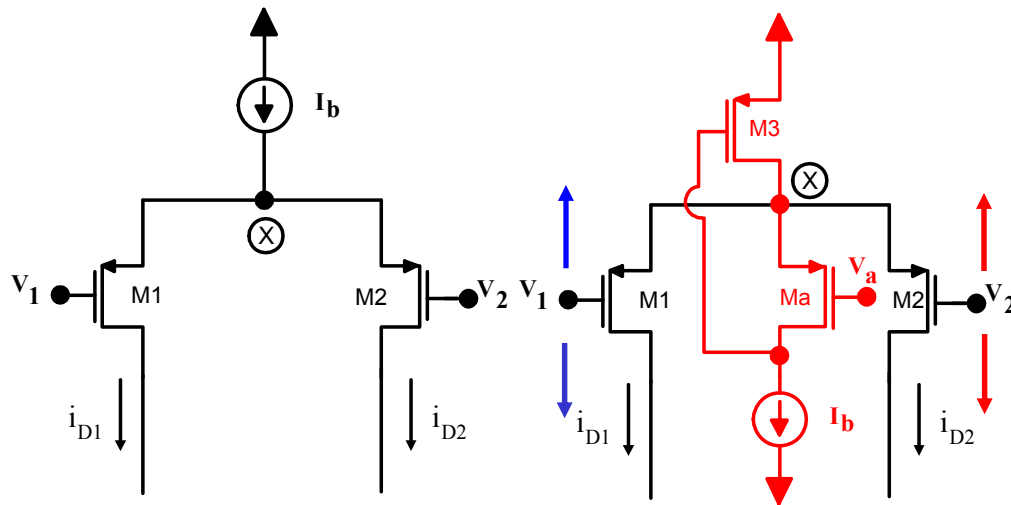


3.FVF Structures

Symmetrical Class-AB Pseudo Differential Pair (FVF-PDP)



Flipped voltage follower applications



Class A Differential Pair

Class AB pseudo Differential pair

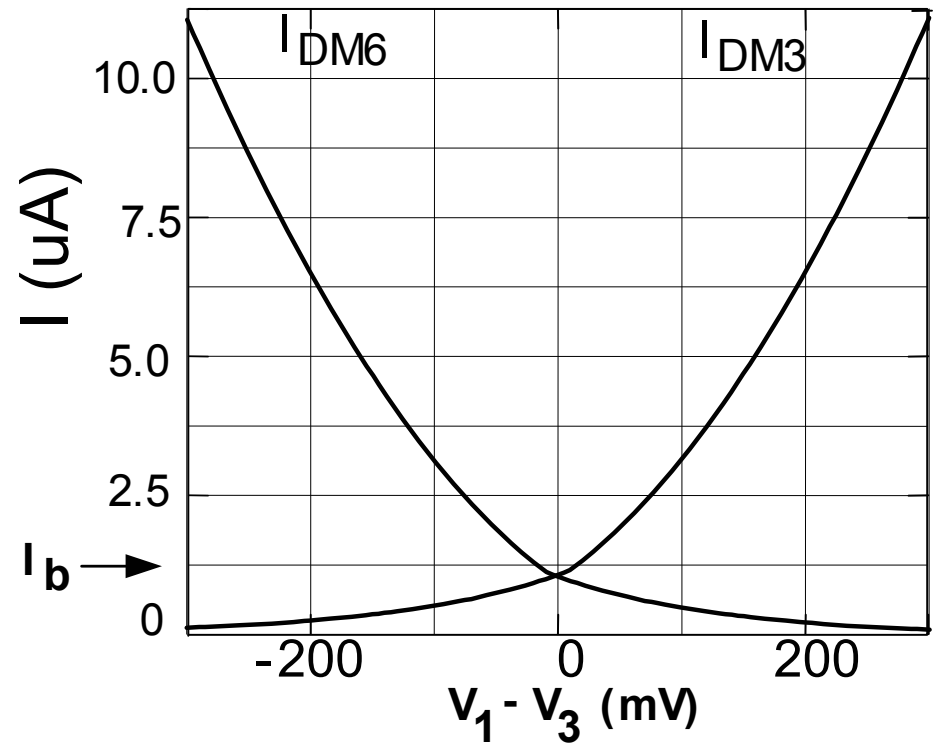
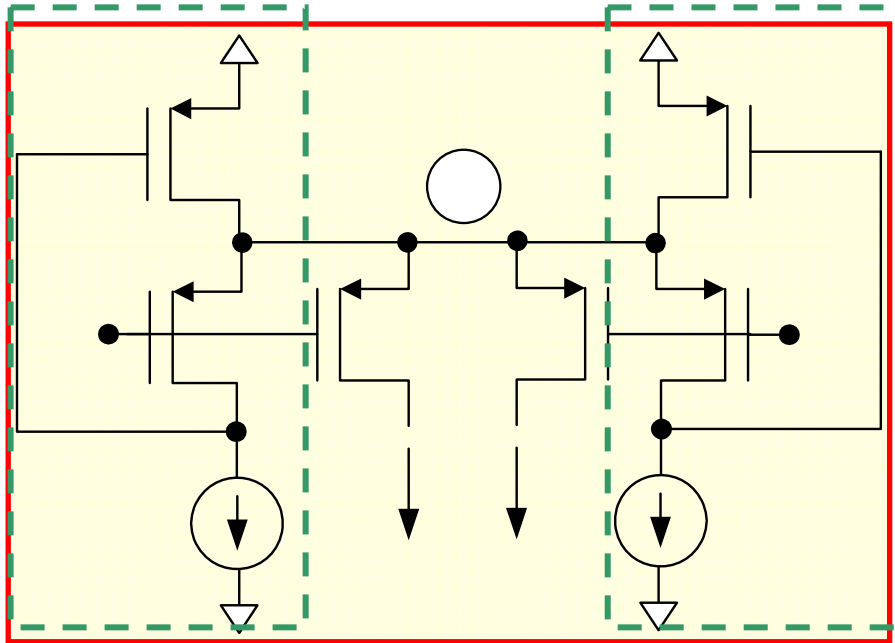
Comparison

$$V_{DD, \min} = |V_{TP}| + 2V_{DS, \text{sat}}$$

"A new Class AB differential Input stage for implementation of low voltage high slew rate op-amps and linear transconductors," J. Ramirez-Angulo, R. Gonzalez-Carvajal, A. Torralba and Carlos Nieva, *IEEE International Symposium on Circuits and Systems*, May 6-9, Sidney Australia

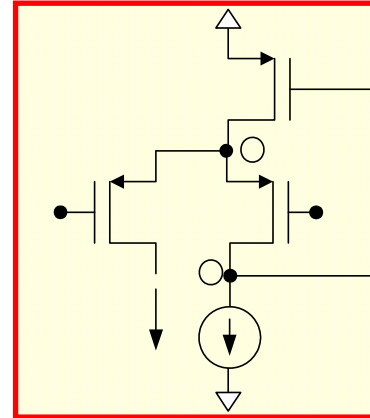
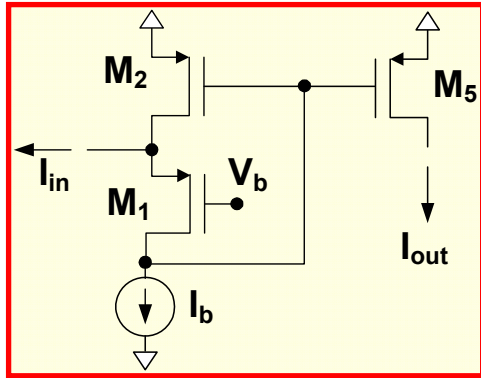
3.FVF Structures

Symmetrical Class-AB Differential Pair (FVF-SDP)

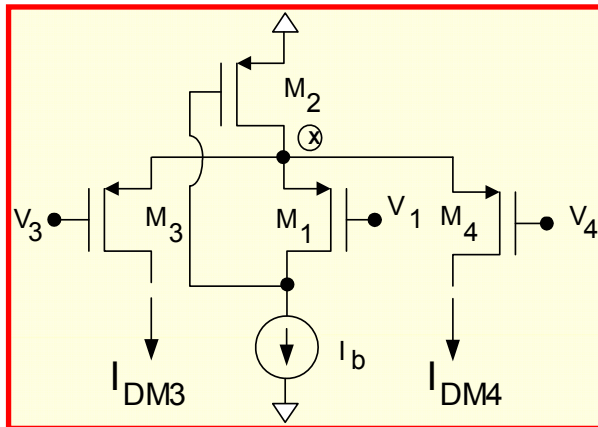


3.FVF Structures. Summary

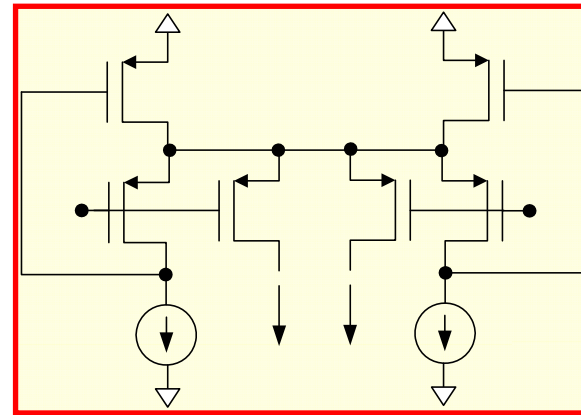
Current sensor (FVF-CS)



**Non-Symmetrical
Class-AB
Differential Pair
(FVF-NDP)**

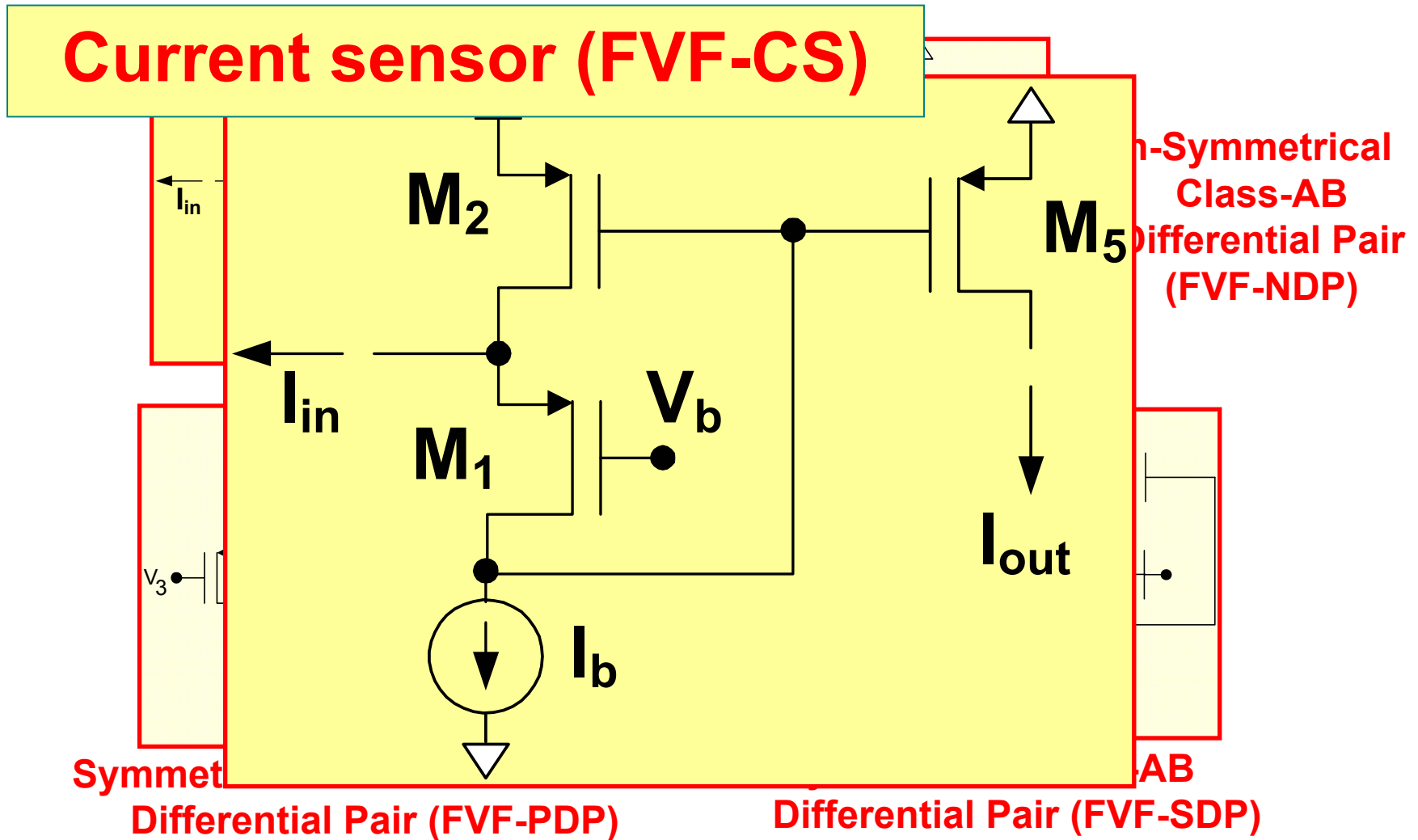


**Symmetrical Class-AB Pseudo
Differential Pair (FVF-PDP)**

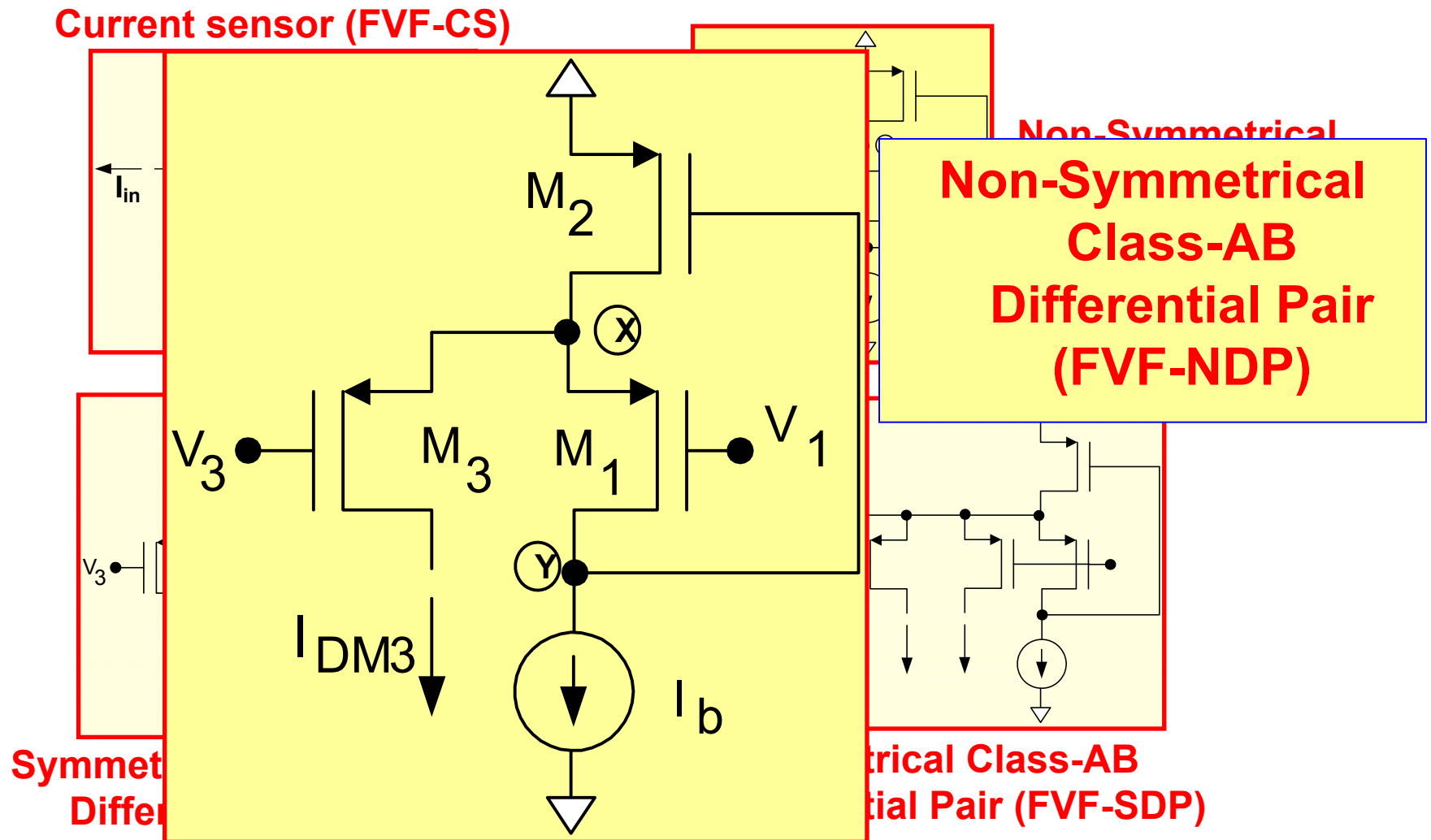


**Symmetrical Class-AB
Differential Pair (FVF-SDP)**

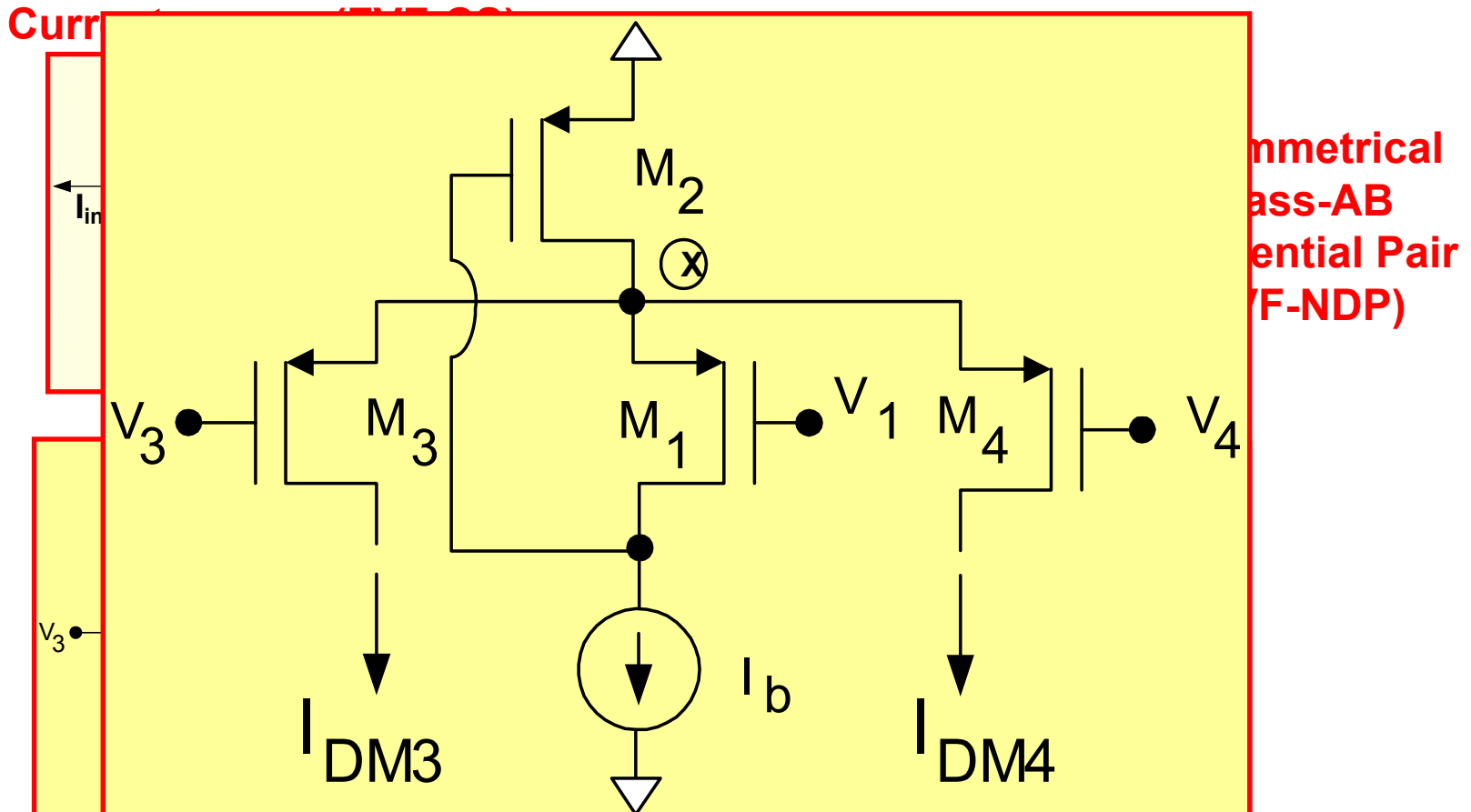
3.FVF Structures. Summary



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3.FVF Structures. Summary

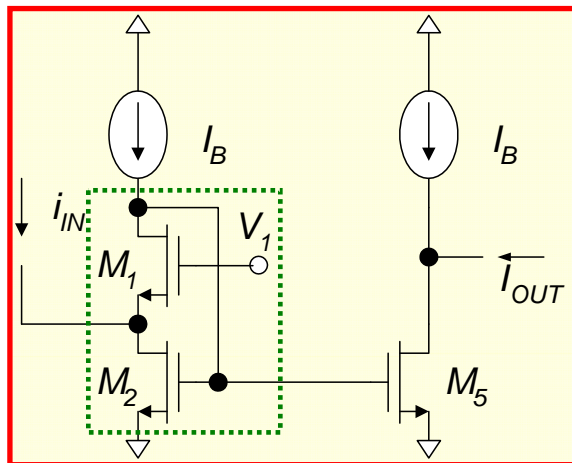


S Symmetrical Class-AB Pseudo Differential Pair (FVF-PDP)
 Differential Pair (FVF-PDP) Differential Pair (FVF-SDP)

4.FVF-CS Applications

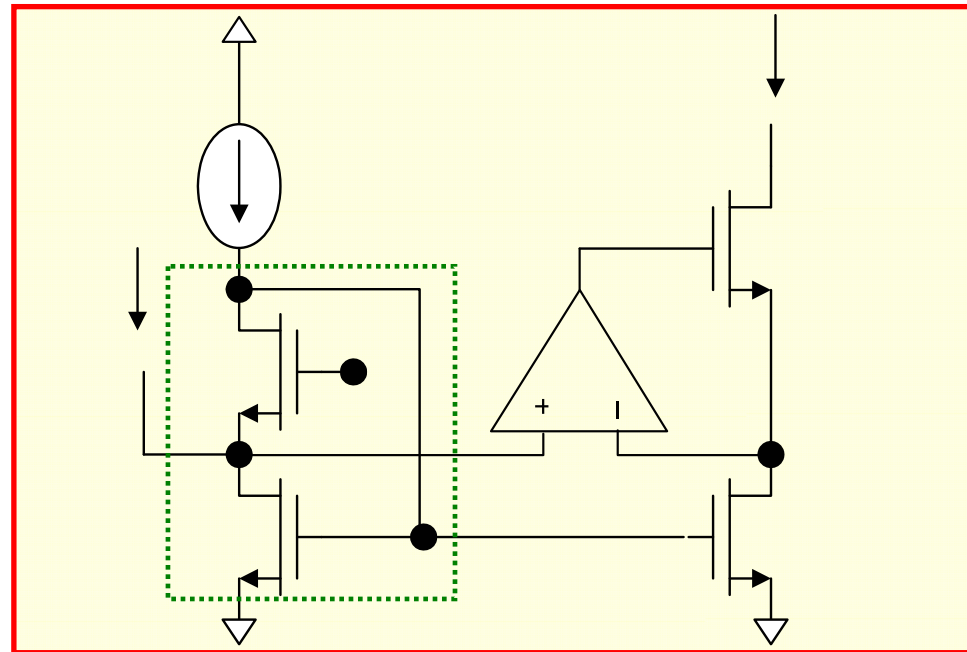
Current sensor (FVF-CS)

Low voltage current mirrors



[Rijns'93] J.J.F. Rijns, "54 MHz switched-capacitor video channel equalizer" *Electr.Lett.*, vol. 29, no. 25, pp. 2181-2182, Dec. 1993

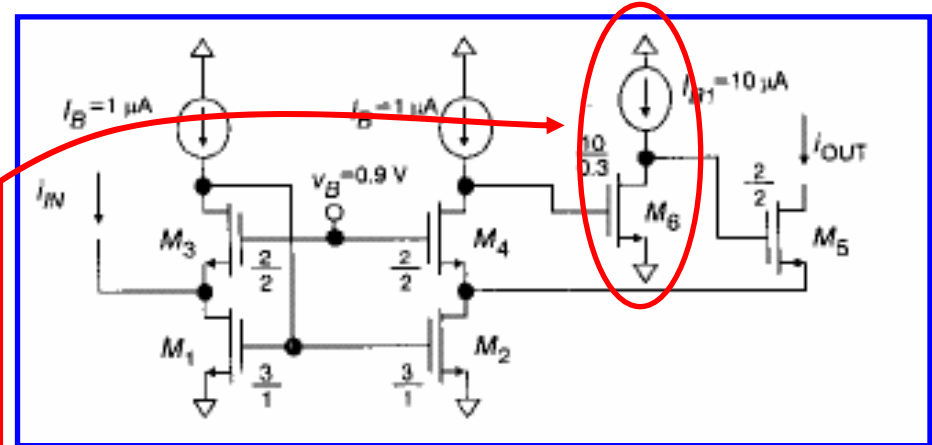
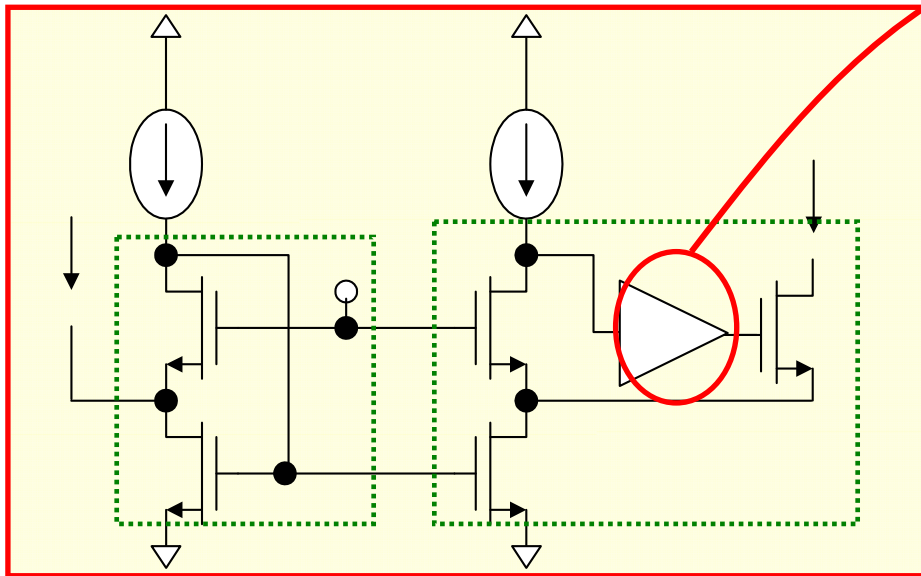
- $V_{in}^{MIN} = V_{DSsat}$
- **Very low input resistance (a few Ohms)**



[Ramirez-Angulo'04] J. Ramirez-Angulo, R.G.Carvajal, A.Torralba, "Low-supply voltage high-performance CMOS current mirror with low input and output voltage requirements," *IEEE TCAS-II*, vol.51, no. 3, pp. 124-129, March 2004.

4.FVF-CS Applications

**Current sensor (FVF-CS)
Low voltage current mirrors**



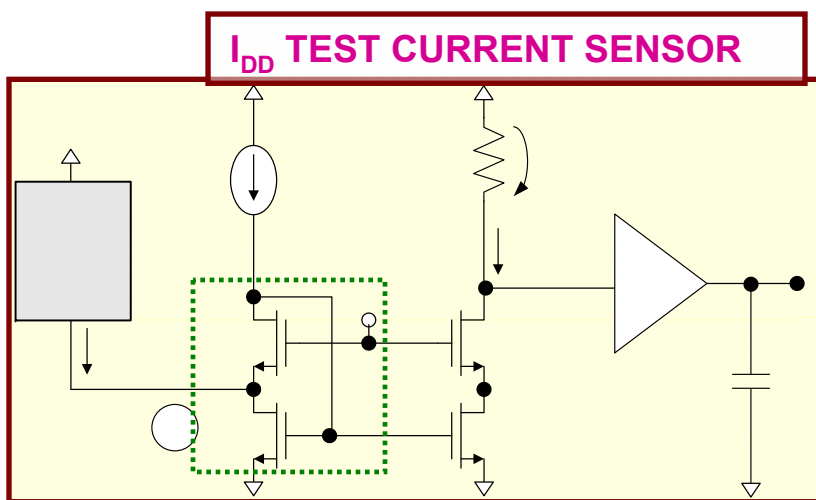
Technology	0,35 μm CMOS AMS
Minimum supply voltage	1 V
Load resistor	10 KOhm
Bandwidth	120 MHz
Input impedance	A few Ohms
Output impedance	$\approx 1\text{ GOhm}$
Input referred noise (@10MHz)	1.5 pA/ $\sqrt{\text{Hz}}$
Settling time (1%, 4 μA step)	20ns
THD (10 μA pp, @10KHz)	-66dB

[Torralba'02] A. Torralba, R.G.Carvajal, J.Ramírez-Angulo, "Output stage for low supply voltage CMOS current mirrors" *Electr.Lett.*, vol. 38, no. 24, pp. 1528-1529, Nov. 2002

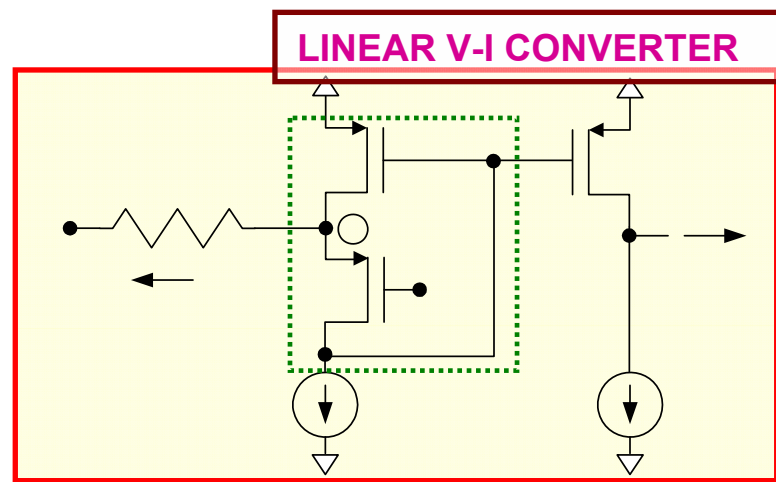
4.FVF-CS Applications

Current sensor (FVF-CS)

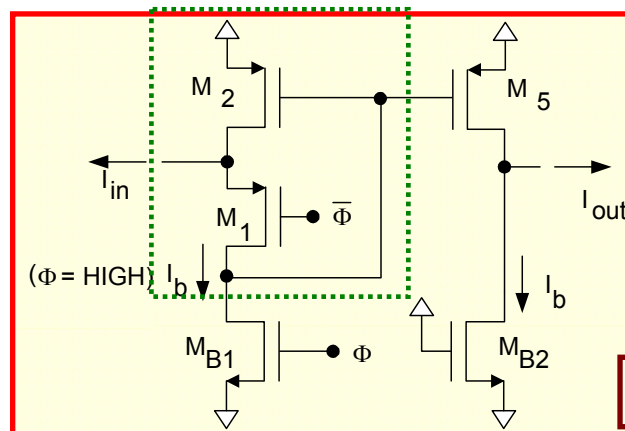
Other applications



[Docudray'03] G.O.Ducodray, R.G.Carvajal, J.Ramírez-Angulo, "A high-speed dynamic current sensor scheme for I_{DD} test using a FVF" *Proc. SSMSD*, pp. 50-53, 2003



[Karthikeyan'01] S. Karthikeyan, A. Tamminneedi, E.K.F.Lee, "Design of low-voltage front-end interfaces for switched-opamp circuits," *IEEE TCAS-II*, vol.48, no. 7, pp. 722-726, July 2001.



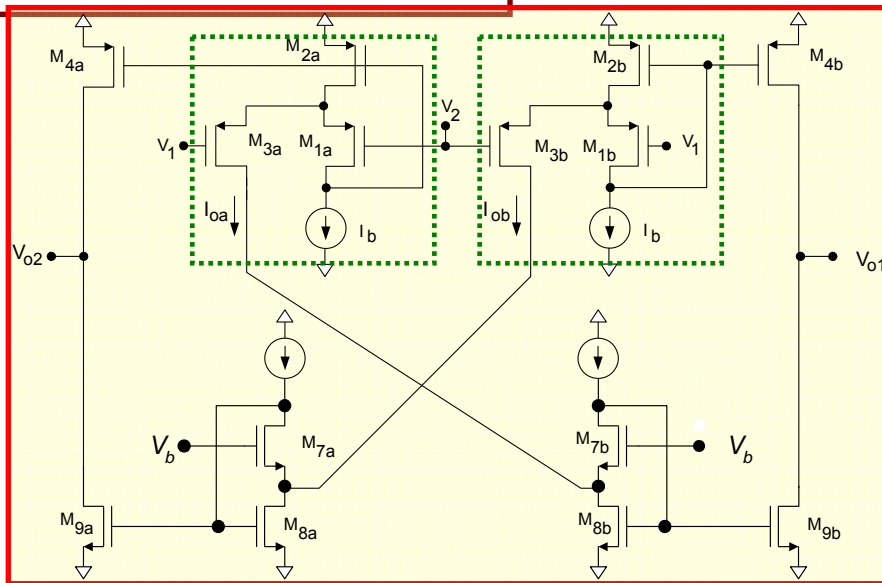
[Rout'00] S. Rout, E.K.F.Lee, "Design of 1 V switched-current cells in standard CMOS process," *Proc. ISCAS*, vol.2, pp. 421-424, 2000

SI Circuits

4.FVF-NDP Applications

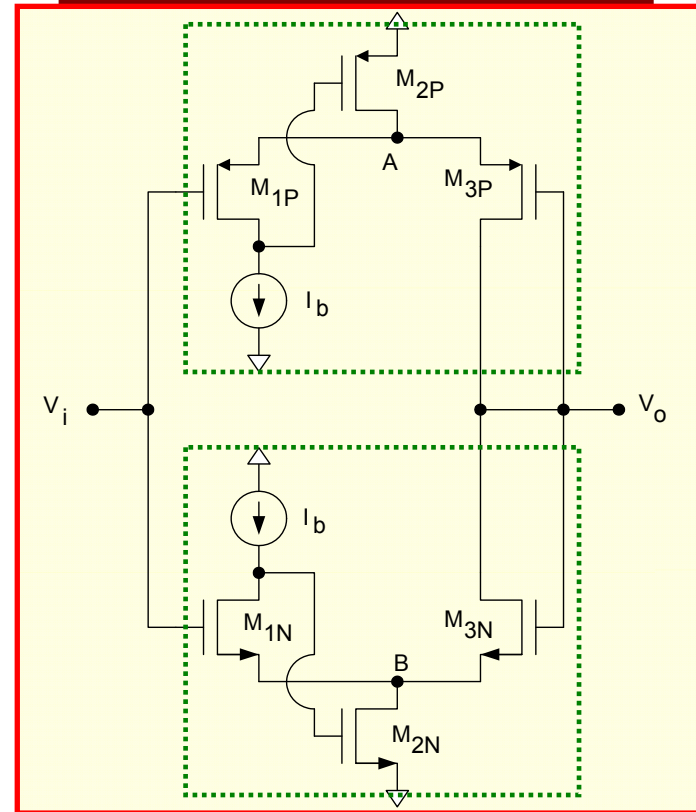
Non-Symmetrical Class-AB Differential Pair (FVF-NDP)

NON-LINEAR CLASS_AB TRANSCONDUCTOR



[Peluso'00] V.Peluso, P. Vancorenland, A.M.Marques, M.S.J.Steyaert, W.Sansen, "A 900mV low-power $\Delta\Sigma$ A/D converter with 77dB dynamic range," *IEEE J.Solid-State Circuits*, vol. 35, no. 4, pp. 632-636, April 2000.

CLASS-AB OUTPUT BUFFER

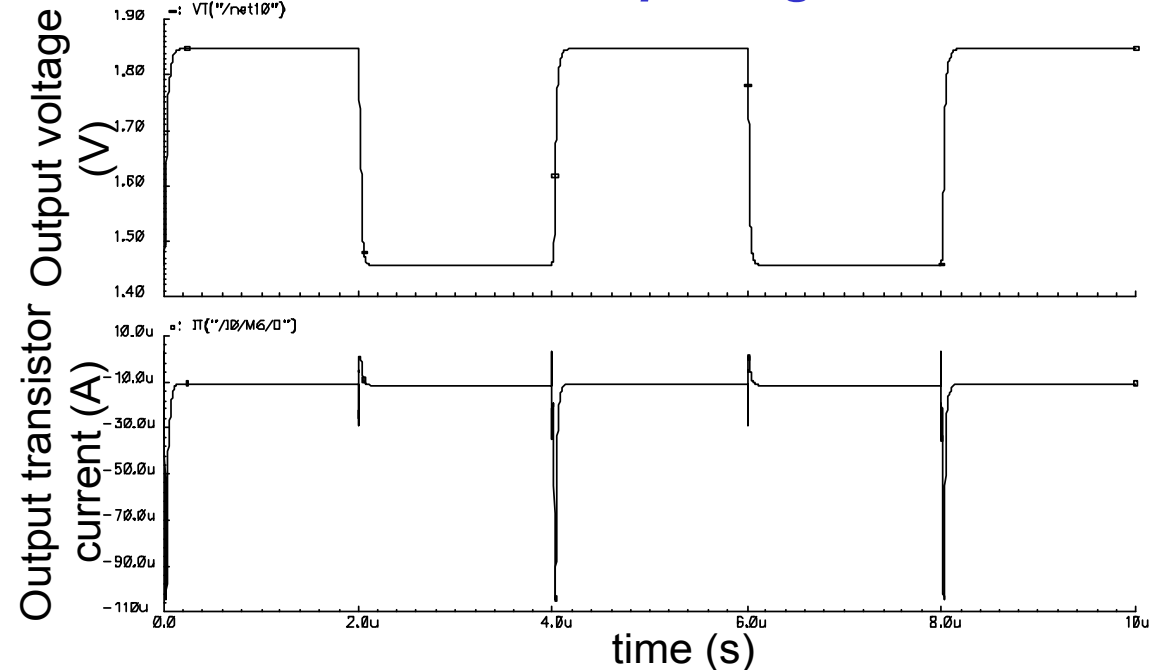
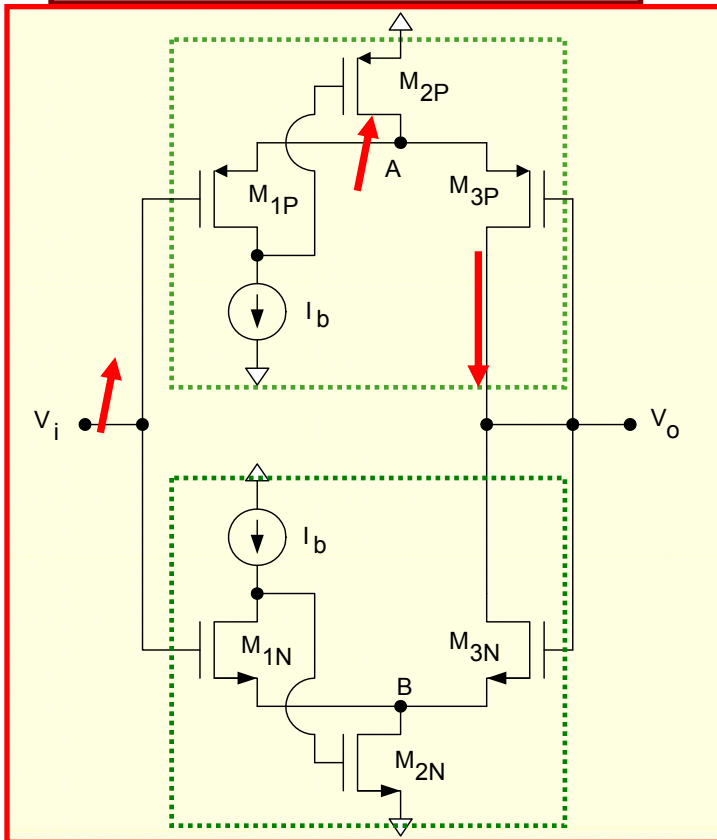


[Carvajal'02] R.G.Carvajal, A. Torralba, J.Ramírez-Angulo, J.Tombs, F. Muñoz, "Compact low-power high slew-rate CMOS buffer for large capacitive loads," *Electron. Lett.*, vol.38, no. 32, pp. 1348-1349, Oct. 2002.

4. FVF-NPD Applications

CLASS-AB OUTPUT BUFFER

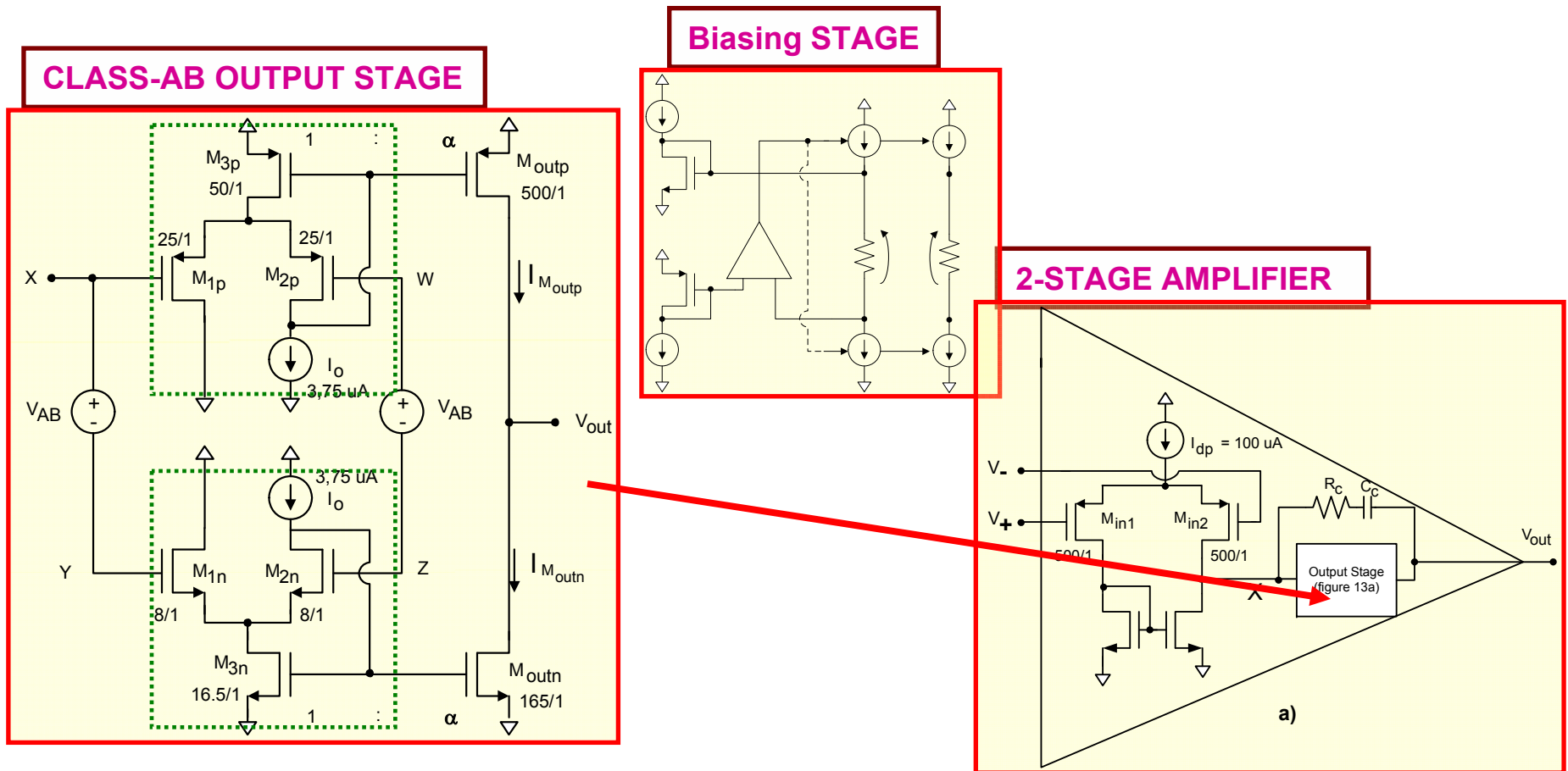
2 V supply, 10pF capacitor load,
250 KHz input signal



[Carrillo'04] J.M.Carrilo R.G.Carvajal, A. Torralba, J.Duque-Carrillo, "Rail-to-rail, low-power high slew-rate CMOS analog buffer," *Electron. Lett.*, vol.40, no. 14, July 2004.

More than 100uA max. output current with 30uA total quiescent current !

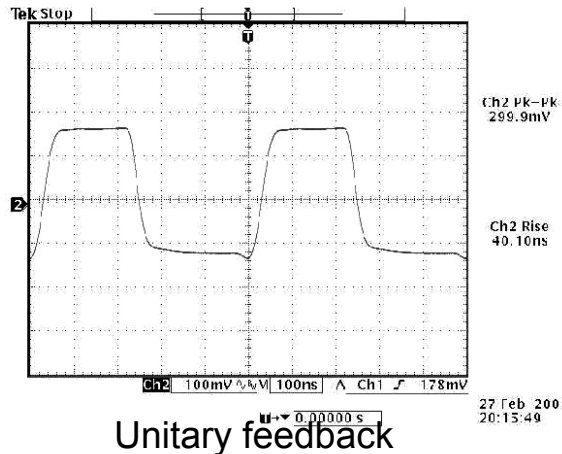
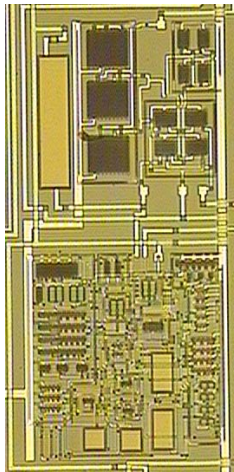
4.FVF-NPD Applications



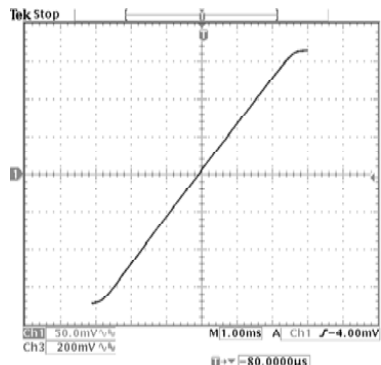
[Torralba'00] A. Torralba, R.G.Carvajal, J. Martínez-Heredia, J.Ramírez-Angulo, "Class-AB output stage for low voltage CMOS op-amps with accurate quiescent current control," *Electron. Lett.*, vol.36, no. 21, pp. 1753-1754, Oct. 2000.

4.FVF Applications

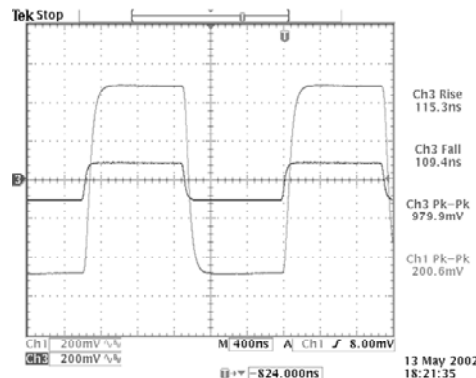
CLASS-AB OUTPUT STAGE in a 2-STAGE OP-AMP



Unitary feedback



Non-inverting Gain= 5 with 2 internal resistors

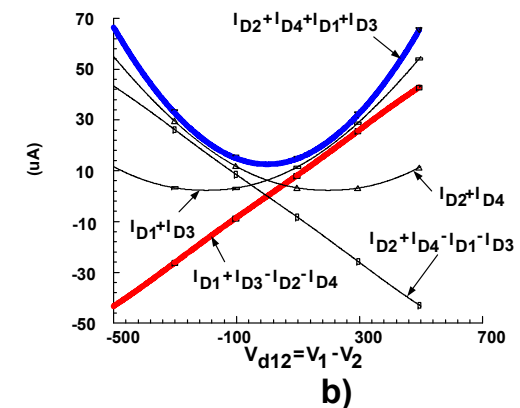
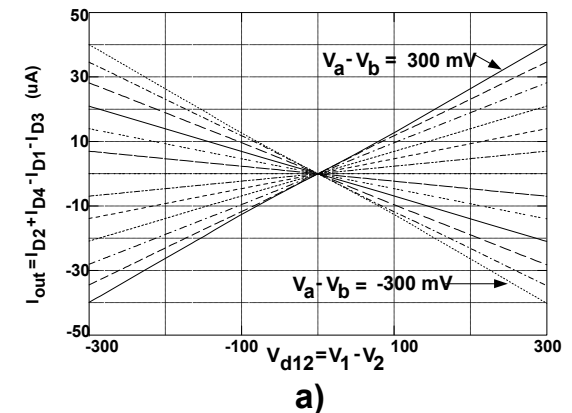
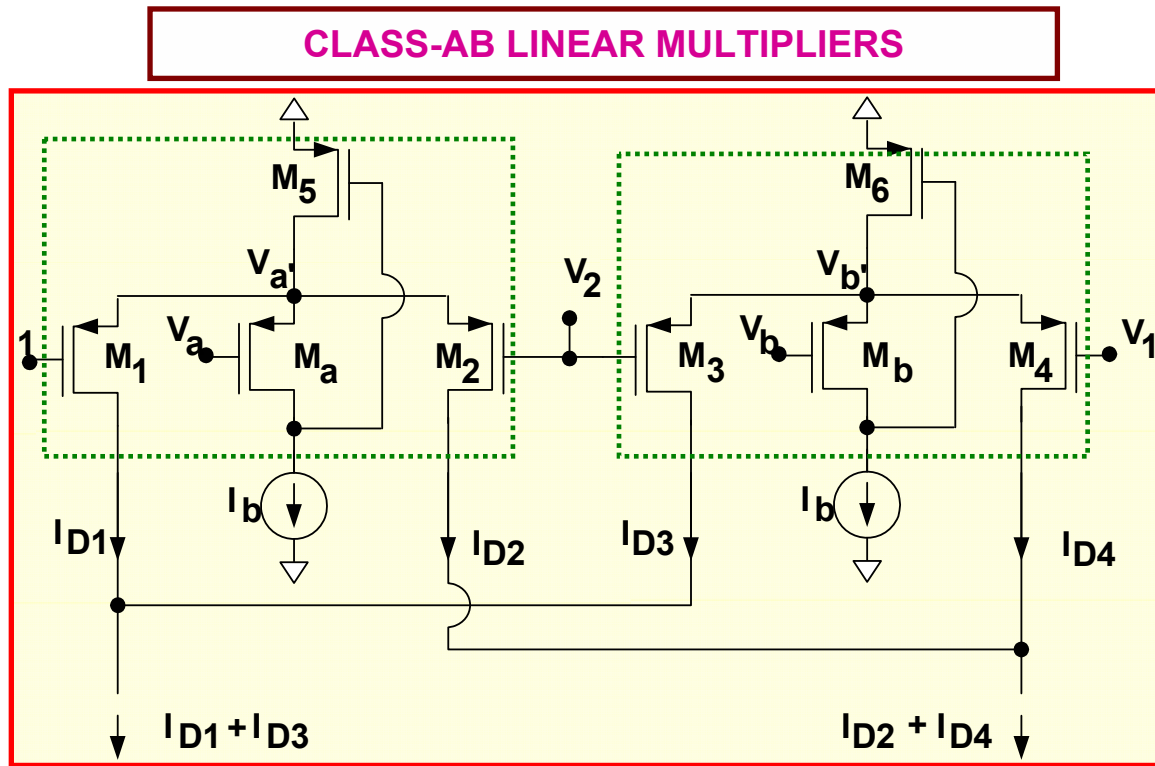


DC Gain	dB	65
Phase Margin	deg (°)	75°
Unity Gain frequency	MHz	15
Quiescent output current	(μ A)	76
Minimum current through output transistors	(μ A)	38
Supply current	(μ A)	218
PSRR	dB	38
CMRR	dB	45
THD (1kHz)	dB	65
Input referred noise (100kHz)	nV ² /Hz	21
Slew Rate * (@ 0.3 V peak)	V/ μ s	10
Peak output current * (@ 0.3 V peak)	μ A	500

$V_{DD}=1.5$ V, $C_L=10$ pF, 0.8 μ m CMOS ($V_t \approx 0.85$ V)
Op-amp comp. $C_C=10$ pF, $R_C=500\Omega$

4.FVF-PDP Applications

Symmetrical Class-AB Pseudo-Differential Pair (FVF-PDP)

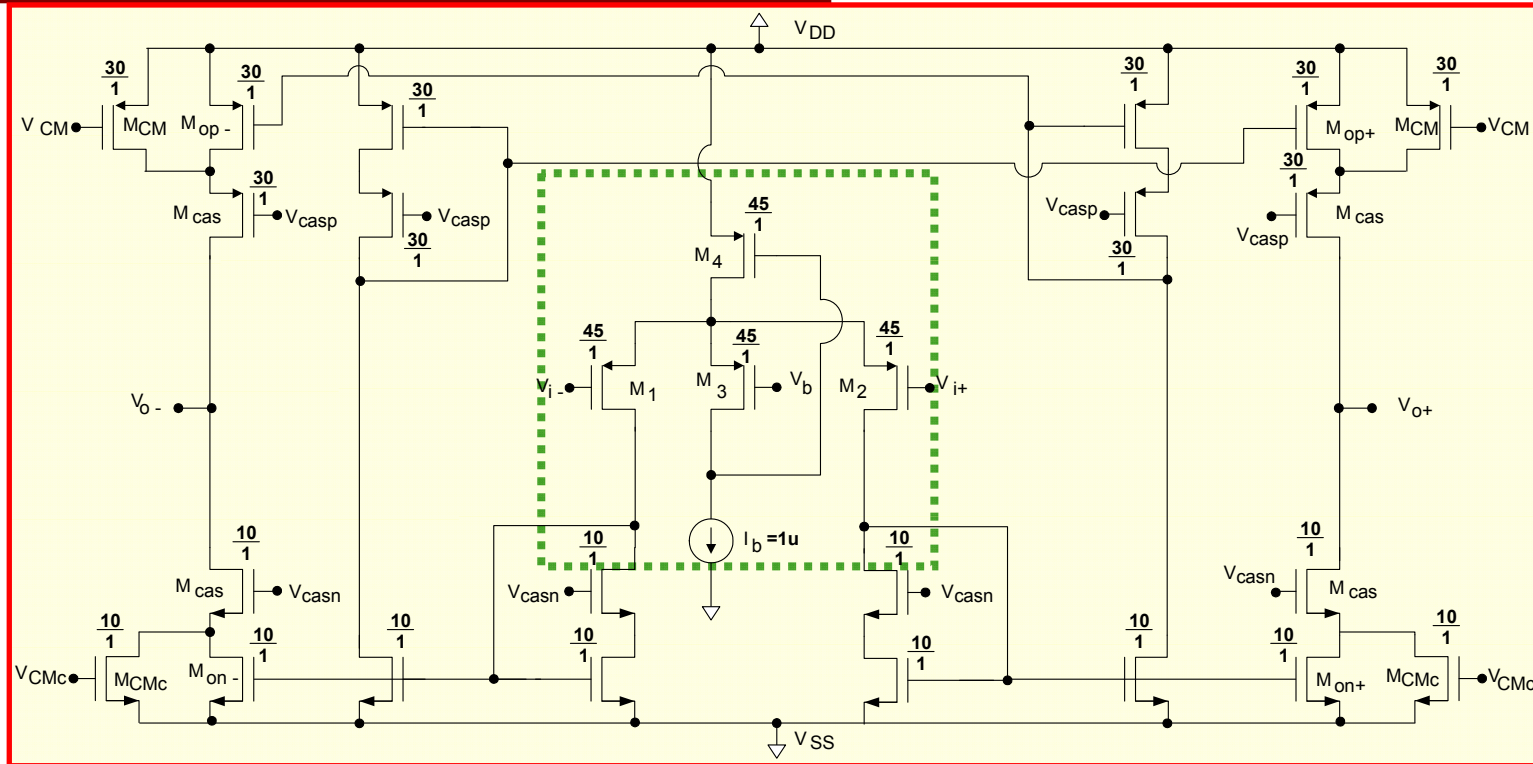


[Ramirez-Angulo'00] J.Ramírez-Angulo, R.G.Carvajal, J.M.Martínez-Heredia, "1.4V supply, wide swing, high frequency CMOS analogue multiplier with high current efficiency," *Proc. ISCAS*, vol. 5, pp. 533-536, 2000

[Ramirez-Angulo'03] J.Ramírez-Angulo, S.Thoutam, A.López-Martín, R.G.Carvajal, "Low voltage CMOS analogue four quadrant multiplier based on Flipped-Voltage-Followers," *Electron. Lett.*, vol.39, no. 25, Dec. 2003.

4.FVF-PDP Applications

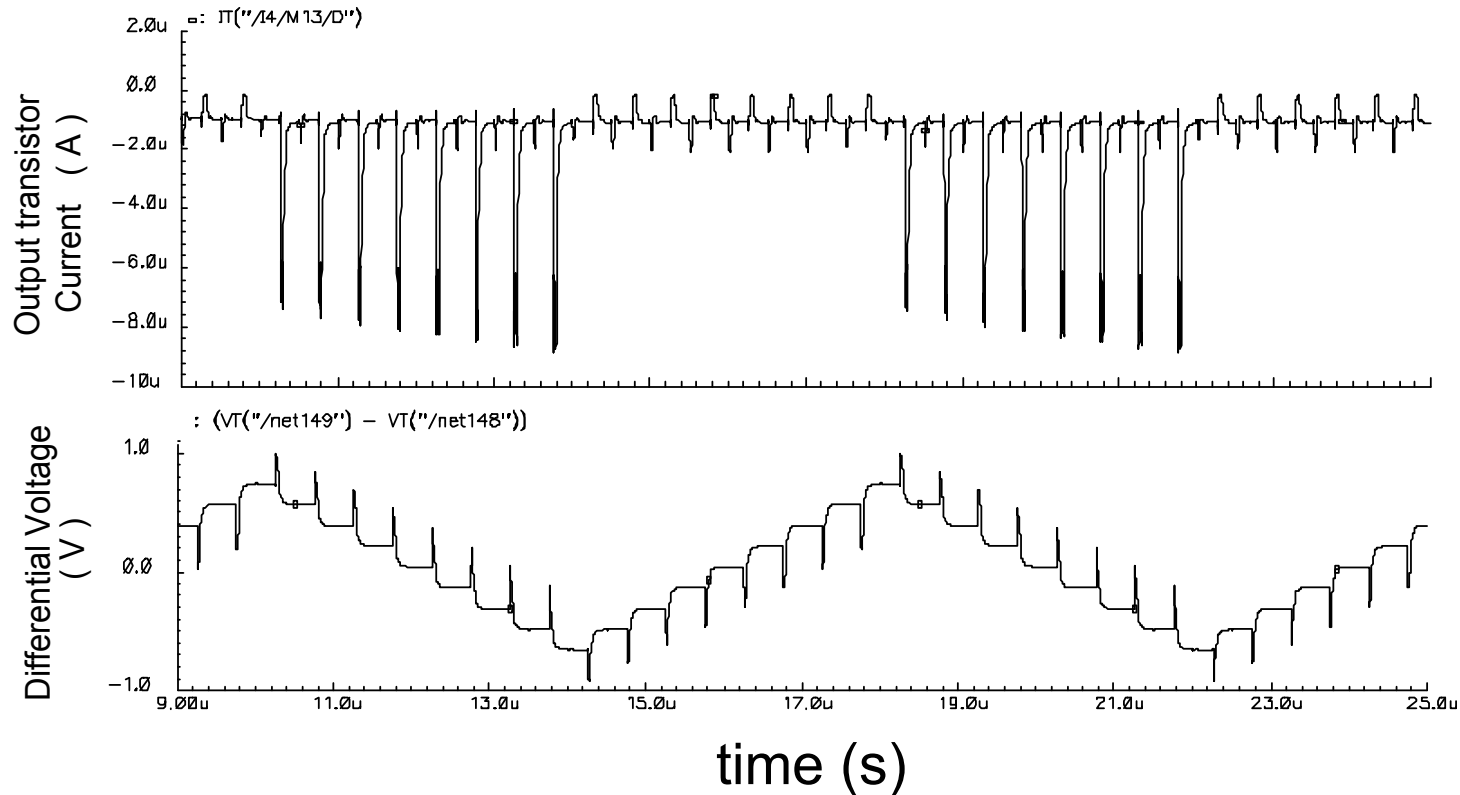
NON-LINEAR CLASS_AB TRANSCONDUCTORS



- [Carvajal'02] R.G.Carvajal, J.Galán, J.Ramírez-Angulo, A. Torralba, "Low-power, low voltage differential class-AB OTAs for SC circuits," *Electron. Lett.*, vol.38, no. 22, pp. 1304-1305, Oct. 2002.
- [Galan'02] J.Galán, A.P. VegaLeal, F. Muñoz, R.G.Carvajal, A.Torralba, J.Tombs, J. Ramírez-Angulo, "A 1.1V very low-power SD modulator for 14-b 16 KHz A/D conversion using a novel class AB transconductance amplifier," *Proc. ISCAS*, vol. 2, pp. 616-619, 2002.

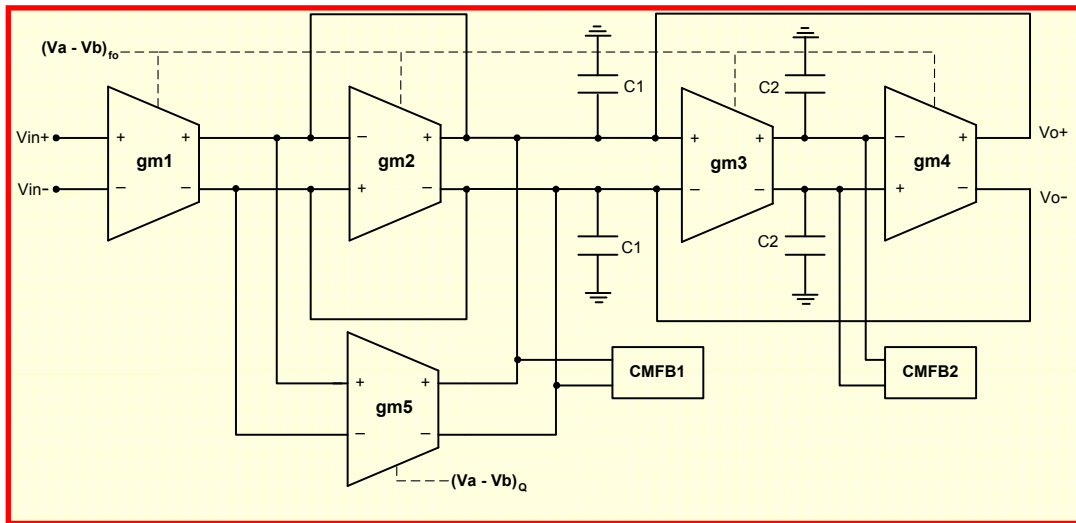
4. FVF-PDP Applications

1.1 V, SC Integrator. 1pF capacitor load, 2MHz switching frequency

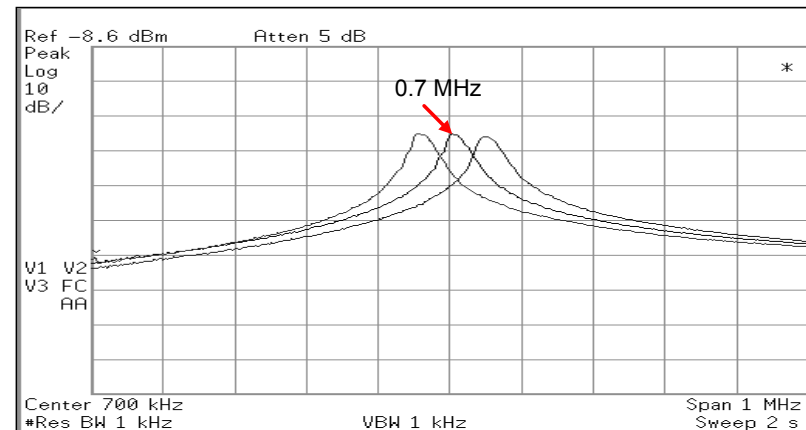
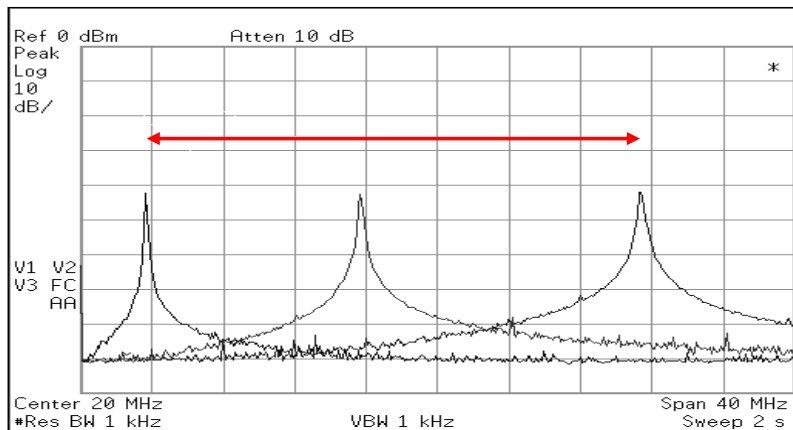


**10 V/usec SR with only 11 uA total quiescent current !
(0.35 μm CMOS)**

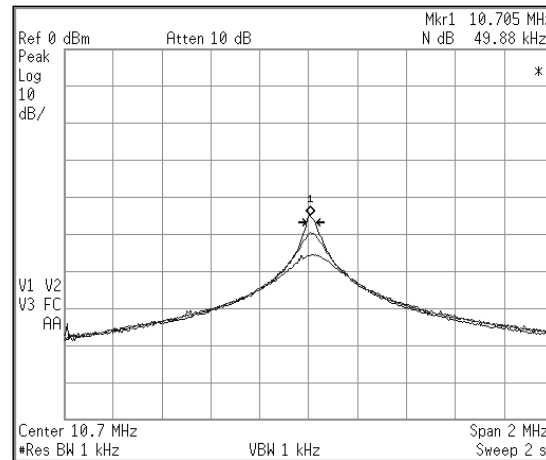
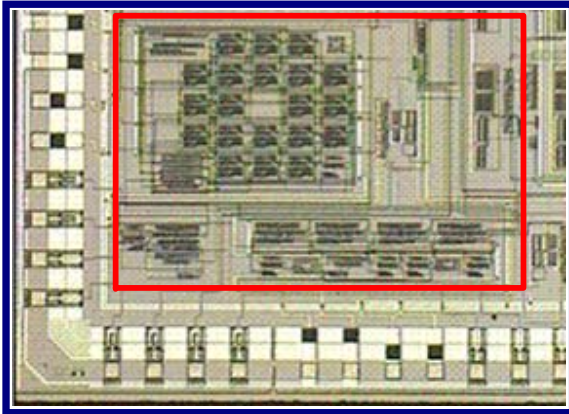
4.FVF-PDP Applications



**gm-C
Filter**

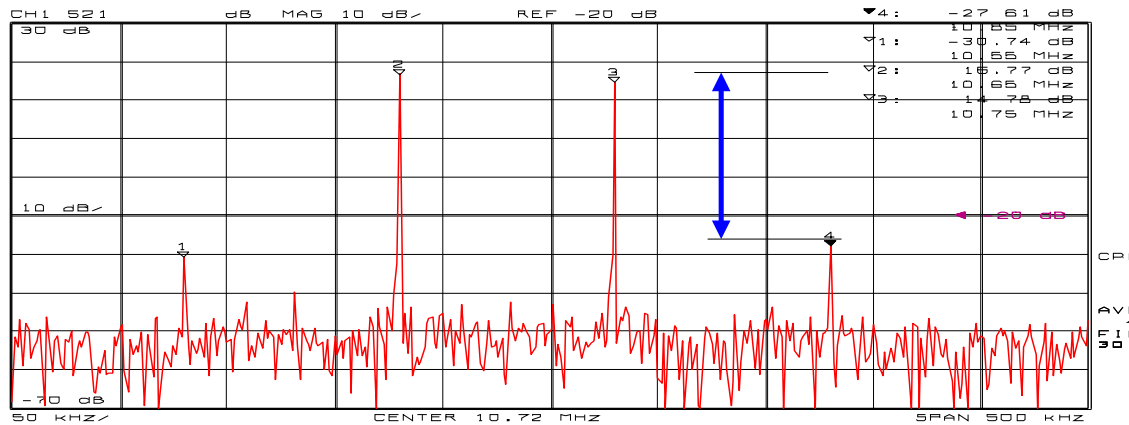


4.FVF-PDP Applications

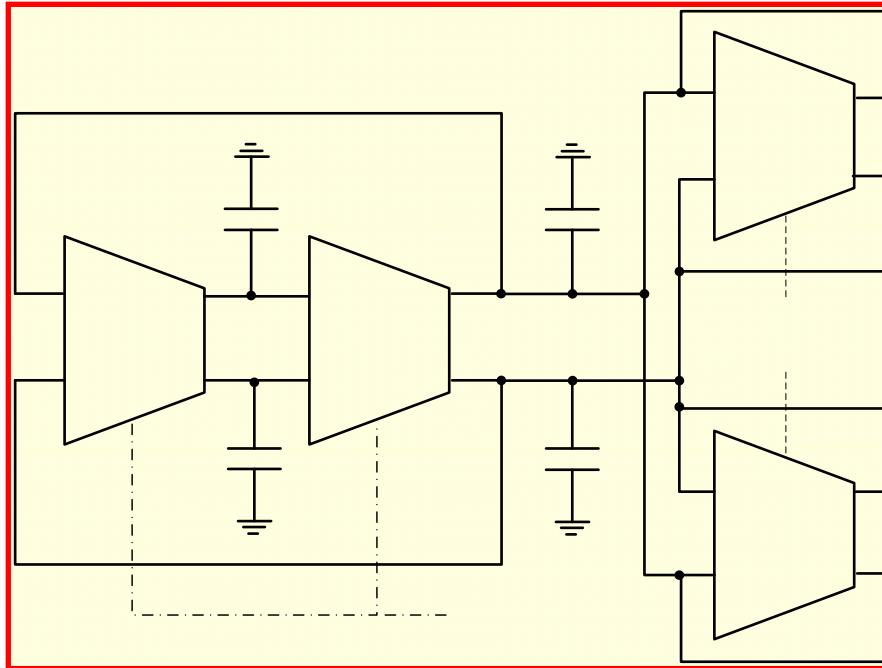


gm-C Filter

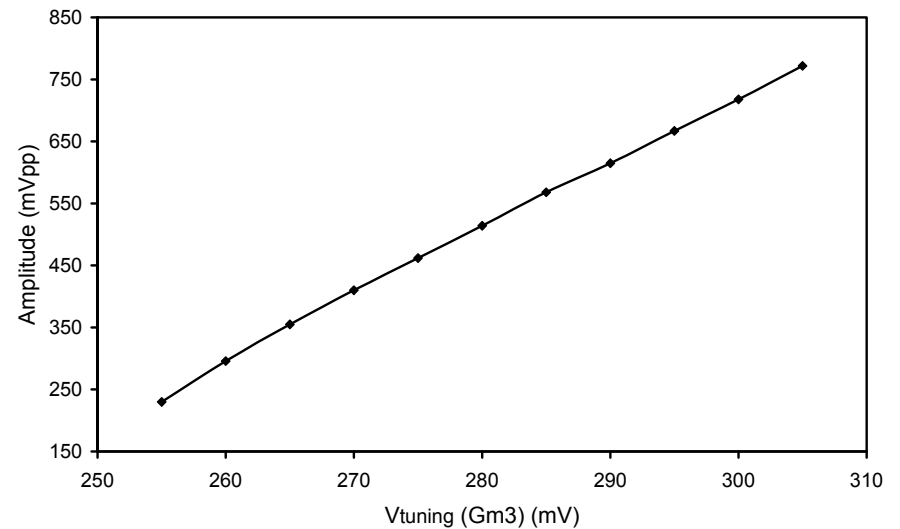
Power supply	2 V
Technology	0.8 μ m CMOS
Chip area	1.44 mm ²
Frequency tuning range	300 kHz–32 MHz
Q range (@10.7MHz)	4–501
$V_{o,CM}$ variation in the entire tuning range	14 mV
Power consumption range	1.18–1.8 mW
THD (@10.7MHz)	-40dB@200 mV _{pp}
SNR	45 dB
IM3 (@10.7MHz)	46 dB
IIP3	8 dBm
PSRR (@ 10.7 MHz)	39 dB
CMRR (@ 10.7 MHz)	42 dB



4.FVF-PDP Applications



gm-C VCO

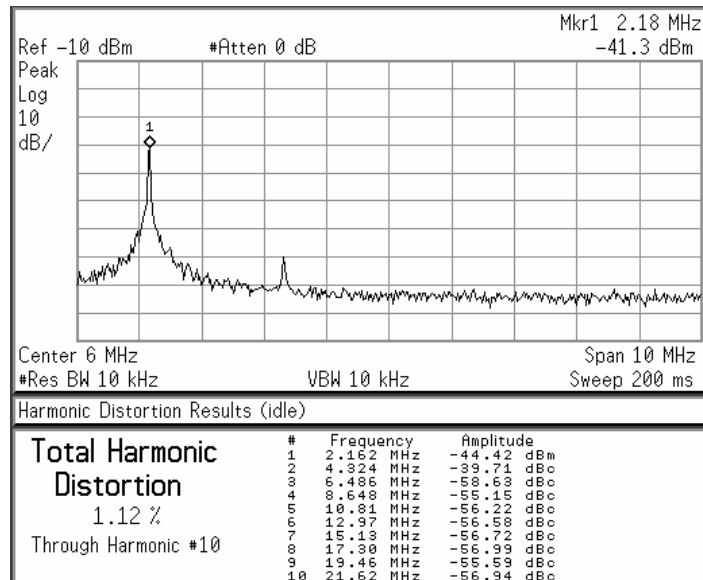
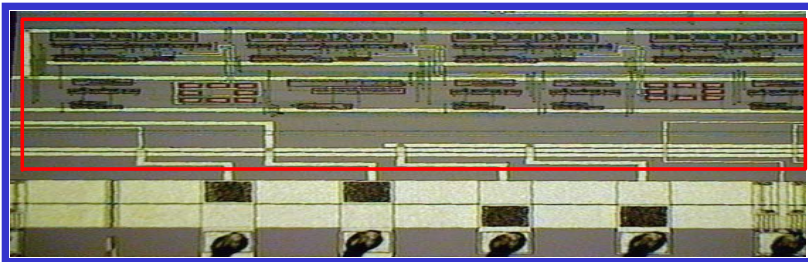


- [Galan'03] J.Galán, R.G.Carvajal, F. Muñoz, A.Torralba, J. Ramírez-Angulo, "A low-power low-voltage OTA-C sinusoidal oscillator with more than two decades of linear tuning range," *Proc. ISCAS*, vol. 1, pp. 677-680, 2003.
- [Galan'04] J. Galan, R. G. Carvajal, A. Torralba, F. Muñoz, and J. Ramirez-Angulo, A low-power, low-voltage OTA-C sinusoidal oscillator with a large tuning range. *IEEE Trans. On CAS-II. (to appear)*

4.FVF Applications

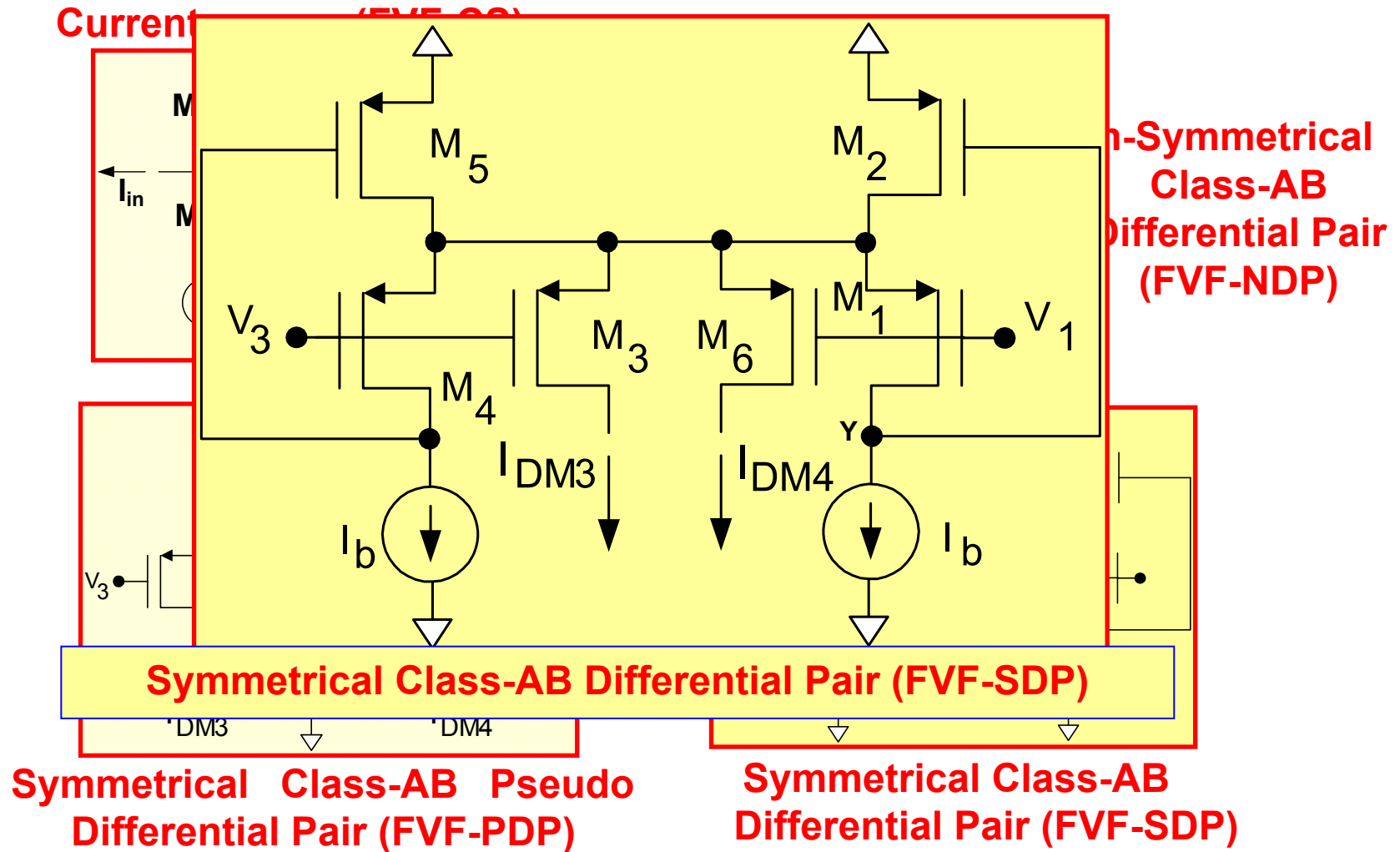
Symmetrical Class-AB Pseudo-Differential Pair (FVF-PDP)

gm-C VCO



Power supply	2 V
Chip area	0.63 mm ²
Technology	0.8 μm
V_{tuning} control	25 mV–500 mV
Frequency tuning range	1 MHz–25 MHz
Power consumption range	1.05–1.58 mW
THD (2 / 25 MHz) @200 mV _{pp}	1.12% / 0.66%
Phase Noise at 10kHz offset	-67 dBc/Hz

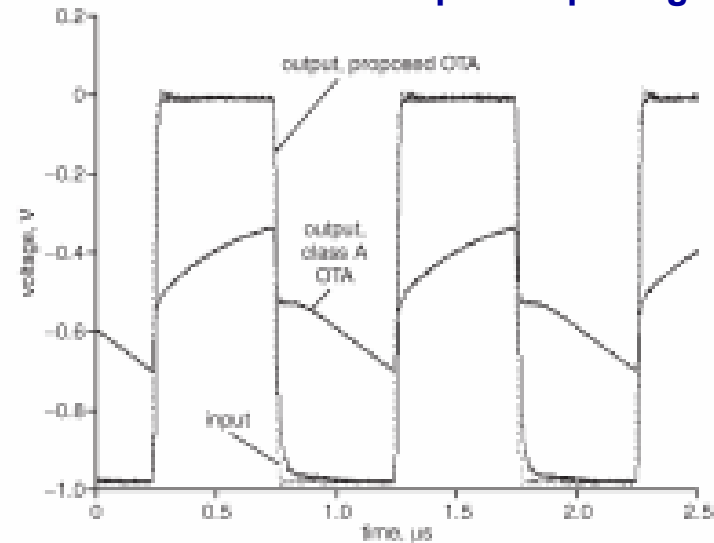
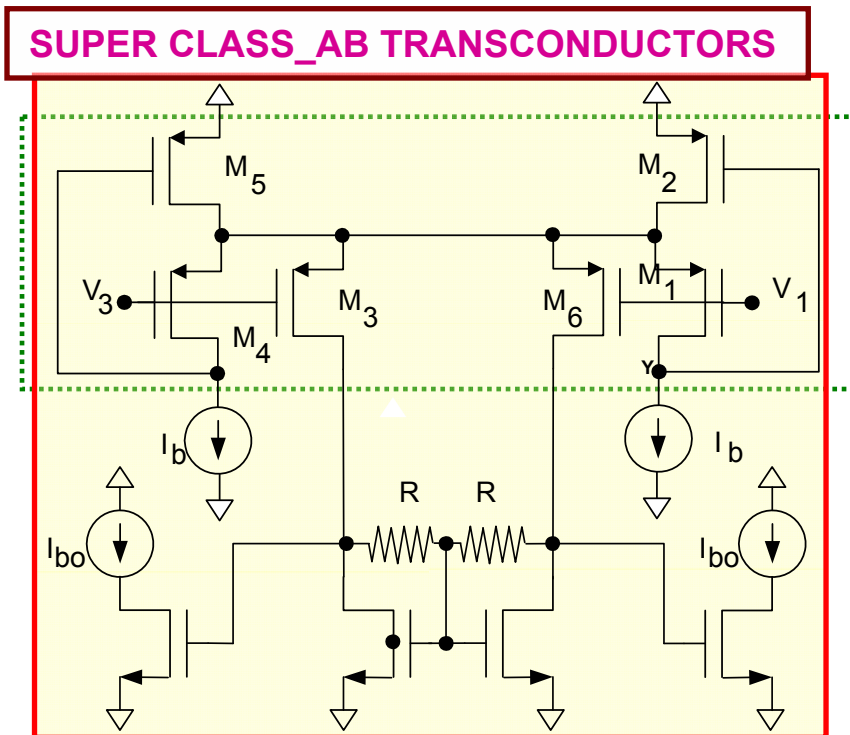
3.FVF Structures. Summary



4.FVF-SDP Applications

Symmetrical Class-AB Differential Pair (FVF-SDP)

0.5 μ CMOS, $V_{DD} = 2$ V, $C_L = 80$ pF
2 MHz square input signal

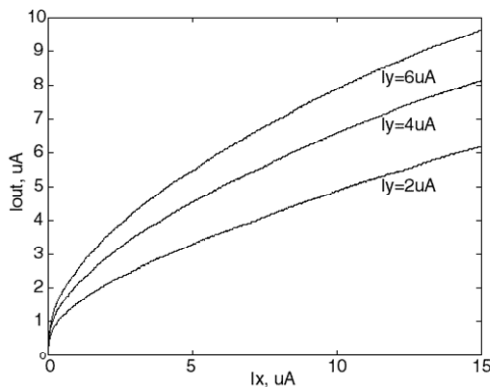
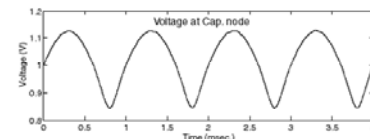
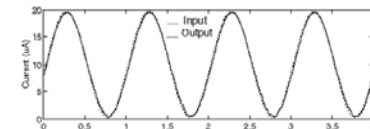
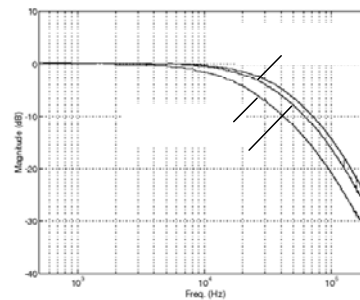
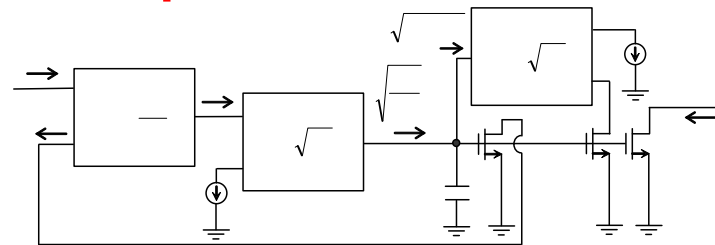
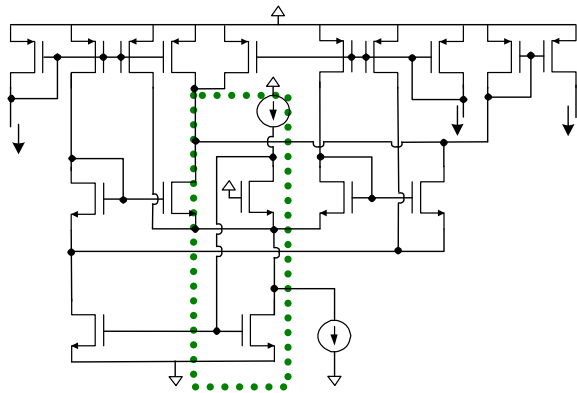


Quiescent power consumption = 120 μ W
SR = 78 V/ μ s, 1% settling time = 110 ns
THD (@100 kHz) = 0.15 %

[Baswa'04] S. Baswa, A. López-Martín, R.G.Carvajal, J.Ramírez-Angulo, "Low voltage micro-power super class-AB CMOS OTA," *Electron. Lett.*, vol.40, no. 4, Feb. 2004.

4. Other Applications

Translinear loops, Geometric Mean, Square-Root Domain Filters, etc.

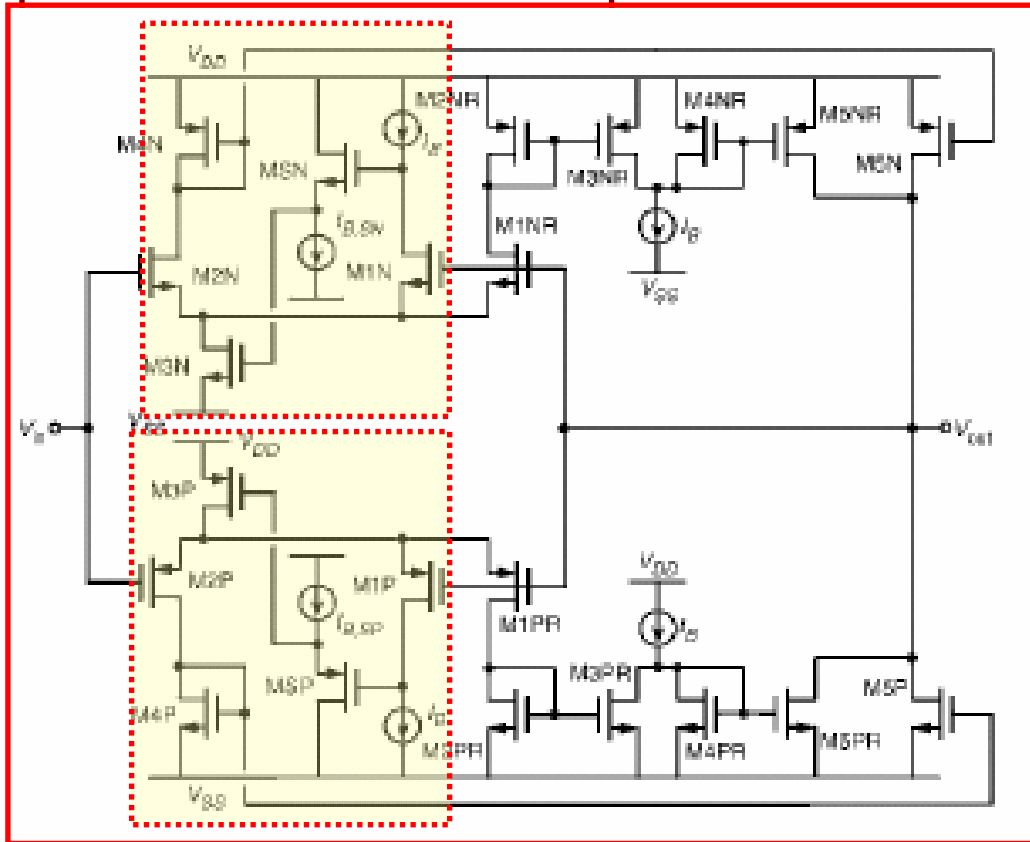


- A.J. López-Martín and A. Carlosena, “Current-mode multiplier/divider circuits based on the MOS translinear principle”, *Analog Integrated Circuits and Signal Processing*, vol. 28, no. 3, pp. 265-278, 2001.
- A.J. López-Martín and A. Carlosena, “Systematic design of companding systems by component substitution”, *Analog Integrated Circuits and Signal Processing*, vol. 28, no. 1, pp. 91-106, 2001.
- A.J. López-Martín and A. Carlosena, “A 3.3V CMOS RMS-DC converter based on the MOS Translinear principle”, *VLSI Design*, 2002

$$\frac{1}{2}X \quad \frac{1}{2}X$$

4. FVF-NPD Applications

CLASS-AB OUTPUT BUFFER



[Carrillo'04] J.M.Carrilo R.G.Carvajal, A. Torralba, J.Duque-Carrillo, "Rail-to-rail, low-power high slew-rate CMOS analog buffer," *Electron. Lett.*, vol.40, no. 14, July 2004.

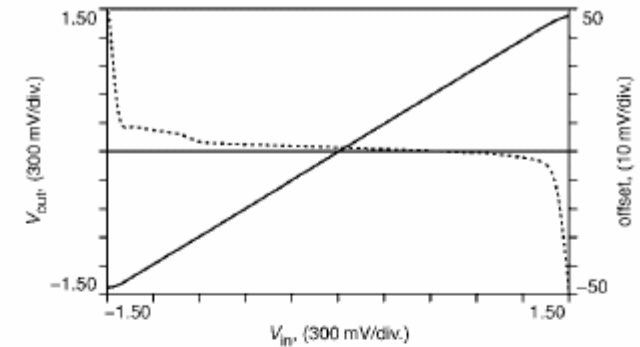


Fig. 3 DC transfer characteristic of analogue buffer in Fig. 2
 — output voltage - - - - - offset voltage

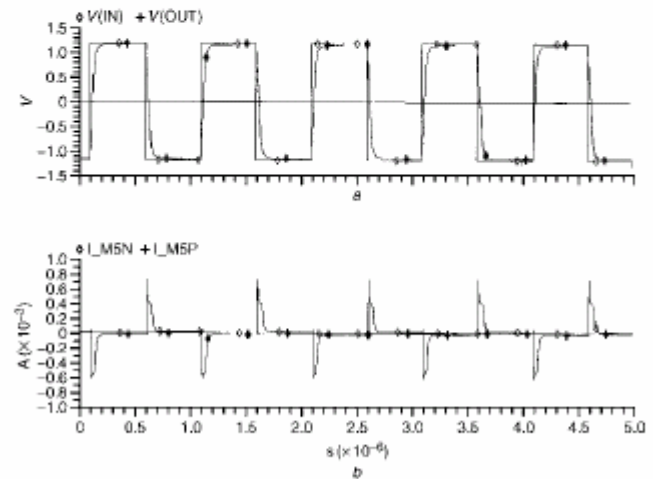


Fig. 4 Large-signal transient response of buffer in Fig. 2 for 2.4 V_{pp}, 1 MHz square input signal with 10 pF load
 a Input and output voltages b Currents through output transistors

Conclusions

1. A new cell, called *Flipped Voltage Follower (FVF)* has been identified.
2. For low-voltage, low power, class AB operation.
3. Different applications have been reviewed (current mirror, voltage buffer, mixer, OTA, transconductance multiplier and op-amp output stage, filters, VCO, SD modulators...).
4. Simulation and experimental results have been presented that show the potential of the so-called FVF structure.