

# CSCE 222-200 Discrete Structures for Computing

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## Assignment # 1

(Due September 5)

1. Prove by induction that  $3^n < n!$  if  $n$  is an integer greater than 6.
2. (a) Find a formula for  $\frac{1}{1 \cdot 2} + \frac{1}{2 \cdot 3} + \cdots + \frac{1}{n(n+1)}$  by examining the values of this expression for small values of  $n$ .  
(b) Prove by induction the formula you conjectured in part (a).
3. Prove by contradiction that if  $x^3$  is irrational, then  $x$  is irrational.
4. Prove by contradiction that  $\sqrt{2} + \sqrt{3}$  is irrational.

5. Let  $p$ ,  $q$ , and  $r$  be the propositions:

$p$ : You get an A on the final exam;

$q$ : You do every exercise in this book;

$r$ : You get an A in this class.

Write each of the propositions below using  $p$ ,  $q$ ,  $r$  and logical operators:

- (a) You get an A in this class, but you do not do every exercise in this book.
  - (b) You get an A on the final, you do every exercise in this book, and you get an A in this class.
  - (c) To get an A in this class, it is necessary for you to get an A on the final.
  - (d) You get an A on the final, but you do not do every exercise in this book; nevertheless, you get an A in this class.
  - (e) Getting an A on the final and doing every exercise in this book is sufficient for getting an A in this class.
  - (f) You will get an A in this class if and only if you either do every exercise in this book or you get an A on the final.
6. For each of the compound propositions below, use the conditional-disjunction equivalence to find an equivalent compound proposition that does not involve conditionals:
    - (a)  $\neg p \rightarrow \neg q$ ;
    - (b)  $(p \vee q) \rightarrow \neg p$ ;
    - (c)  $(p \rightarrow \neg q) \rightarrow (\neg p \rightarrow q)$ ;