

# Learning What the Internal State Means, Through Action



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## The Question

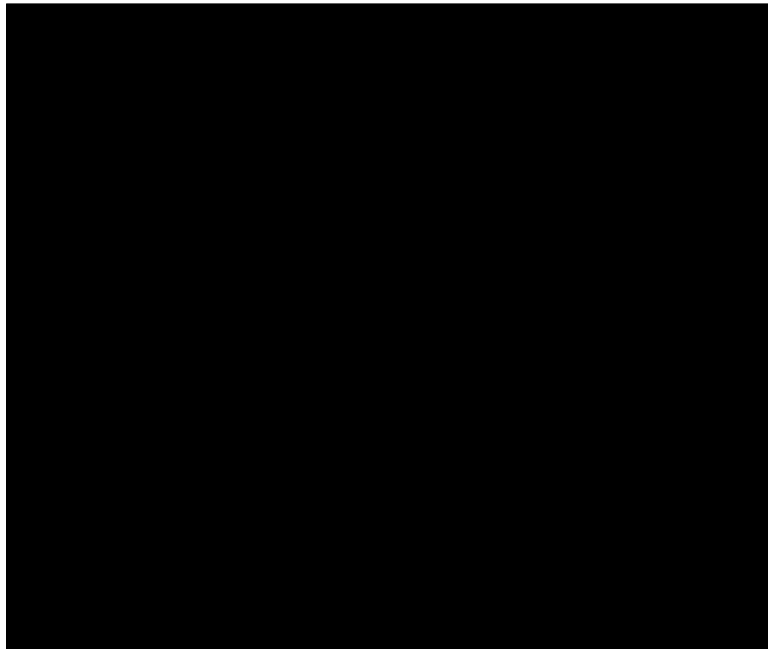
- What do these green lights mean (following slides)?

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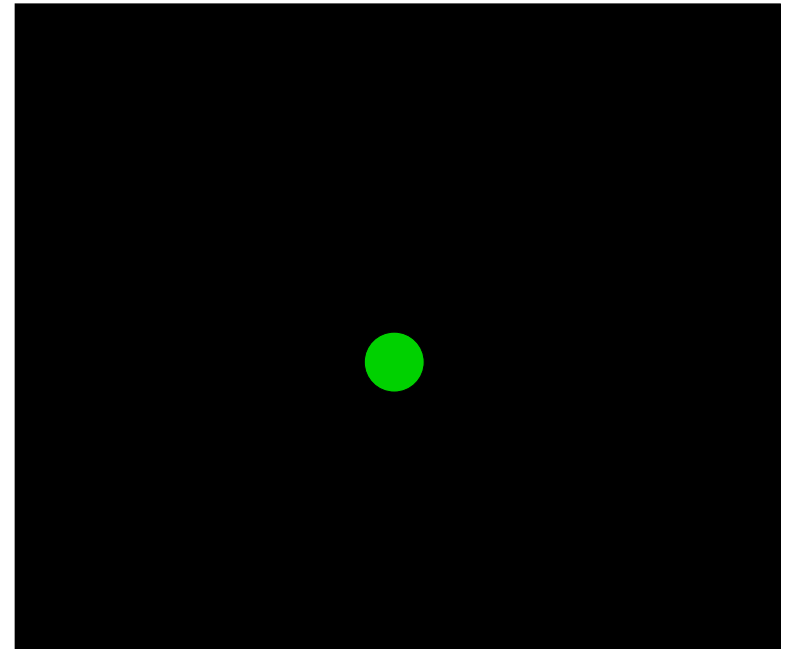
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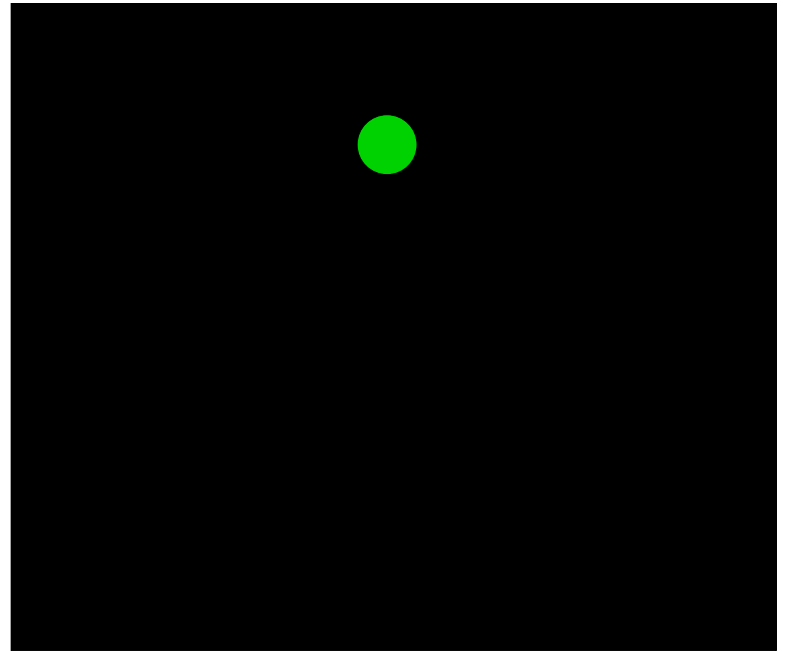
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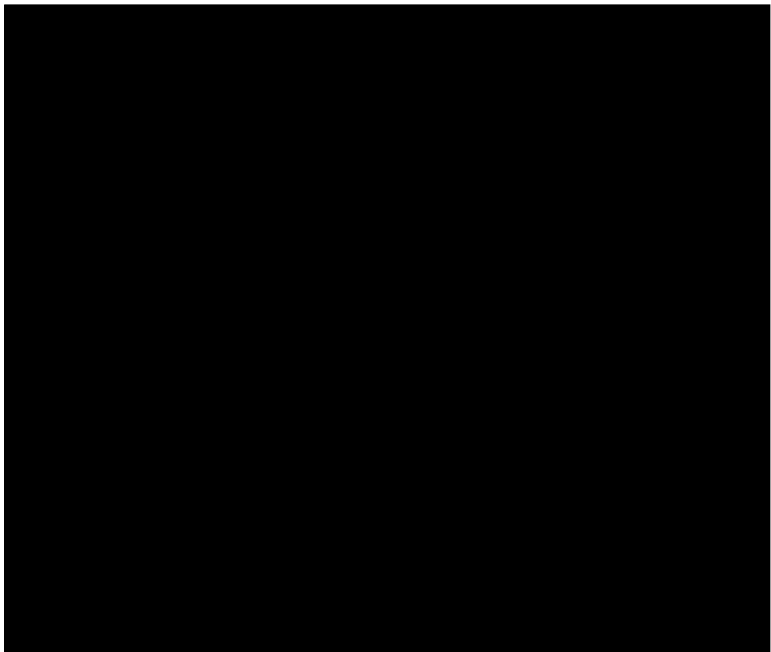
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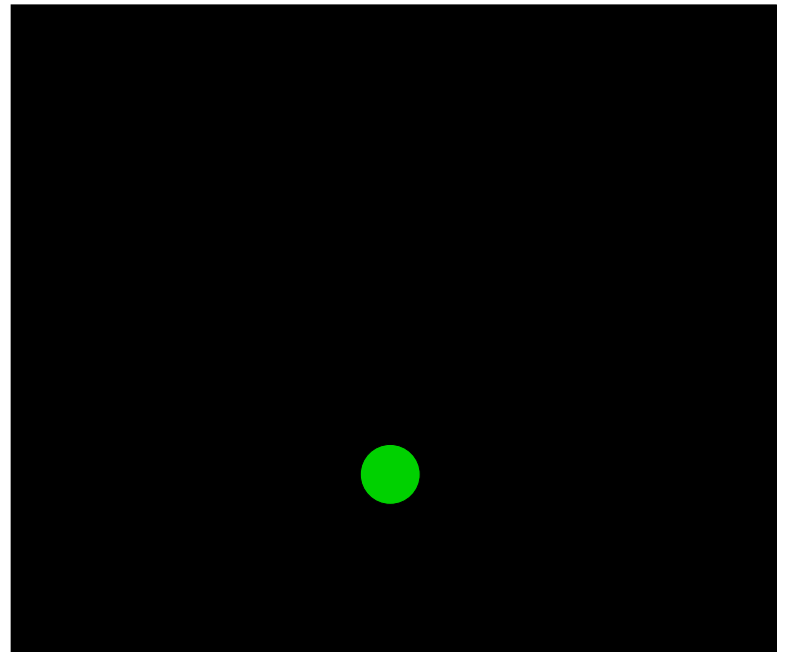
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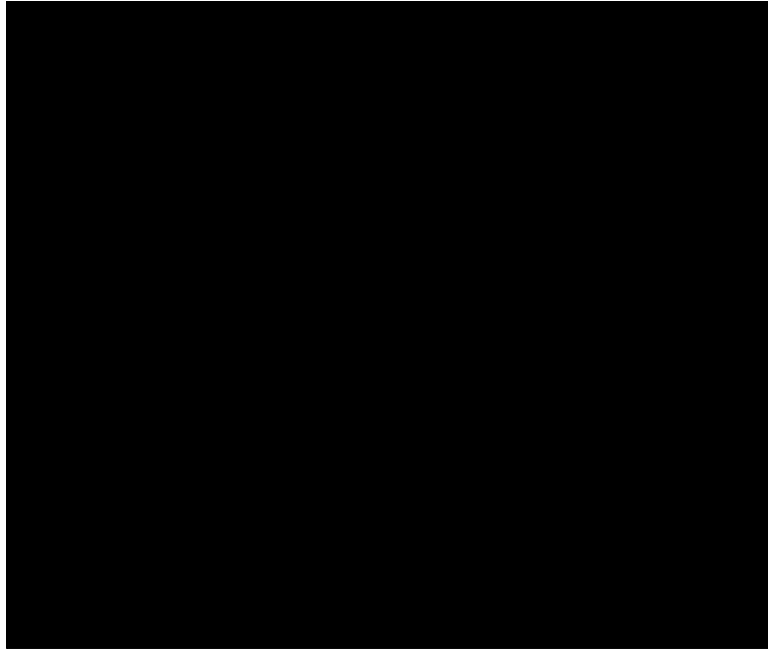
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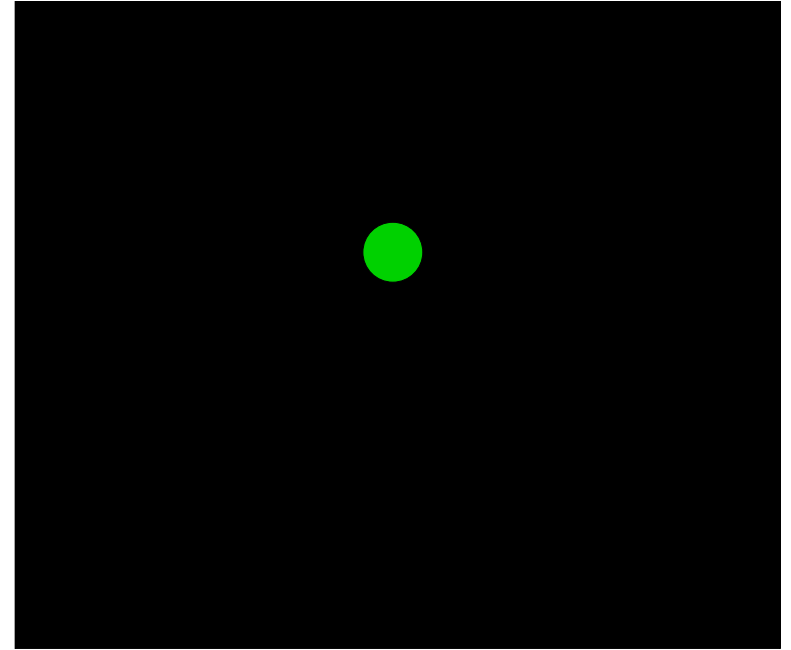
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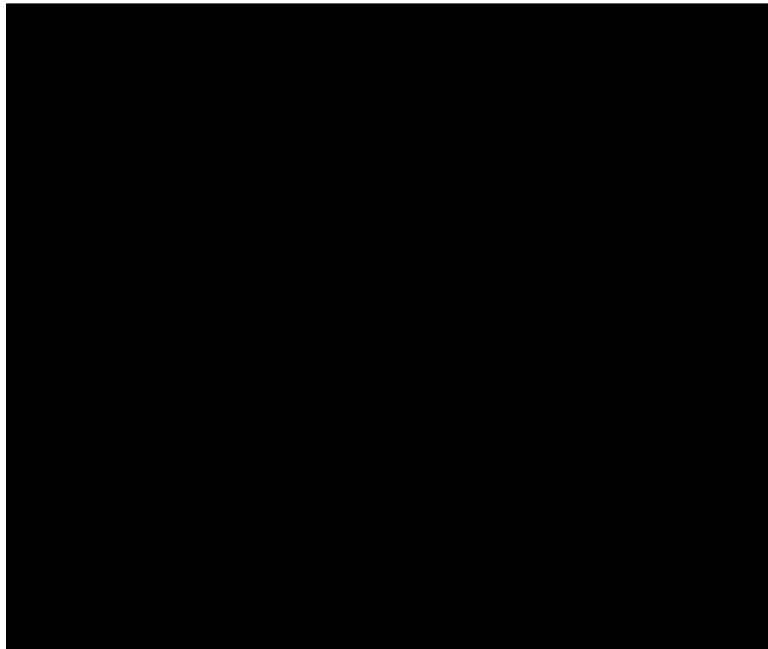
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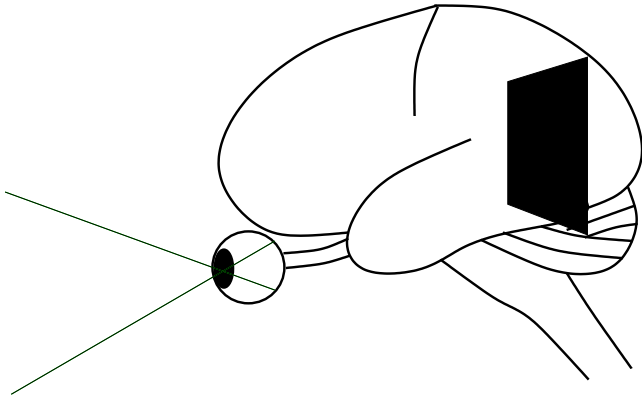
## What Do Those Green Lights Represent?

- It is hard to get any idea at all.
- Actually, this is how it might be like looking at the **brain's activity from the inside** of the brain.

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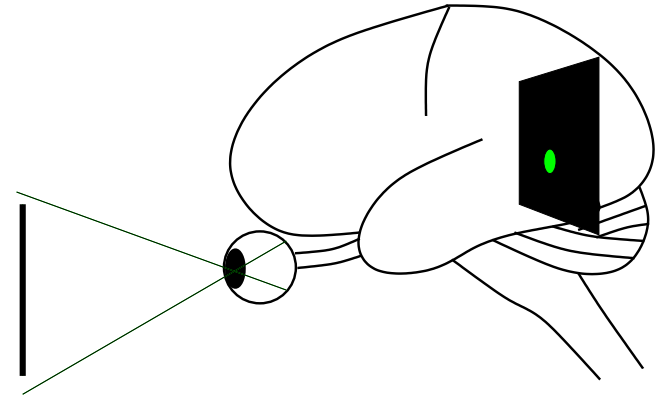
## They Are Visual Cortical Responses to Oriented Lines



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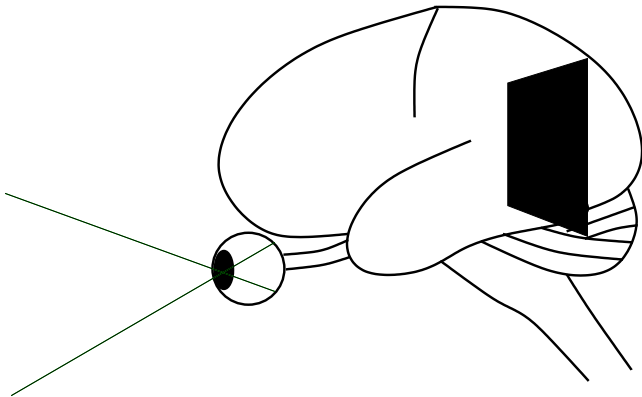
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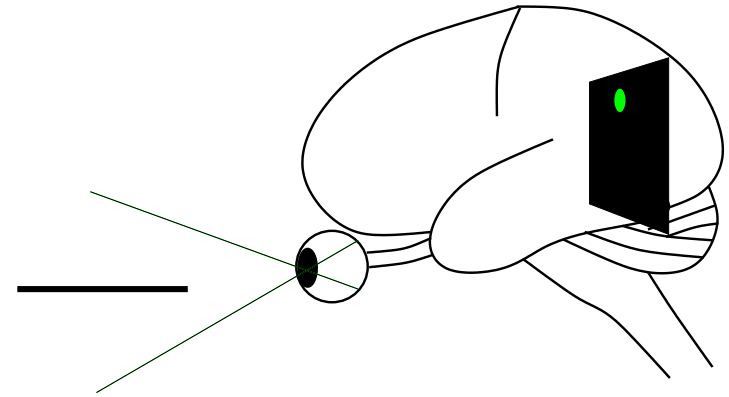
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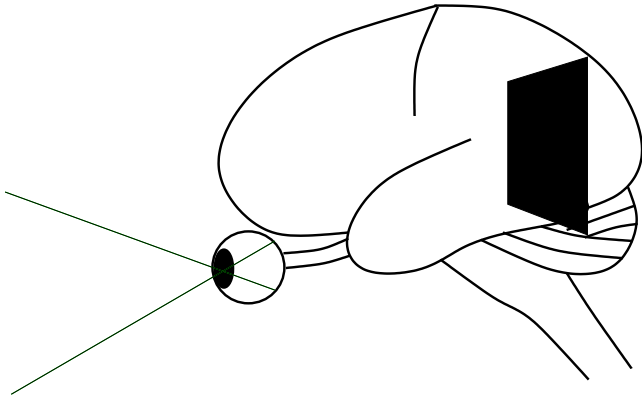
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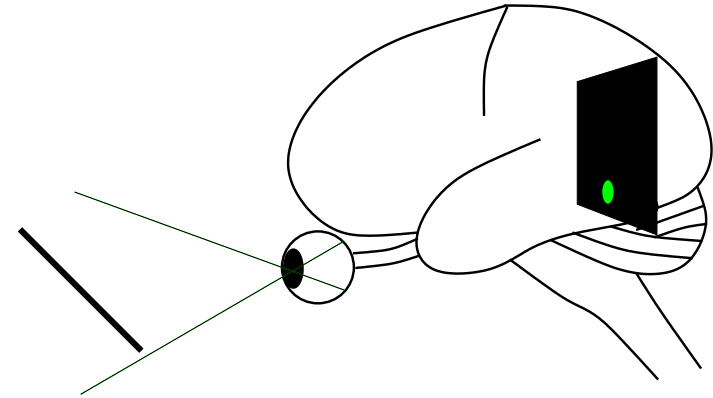
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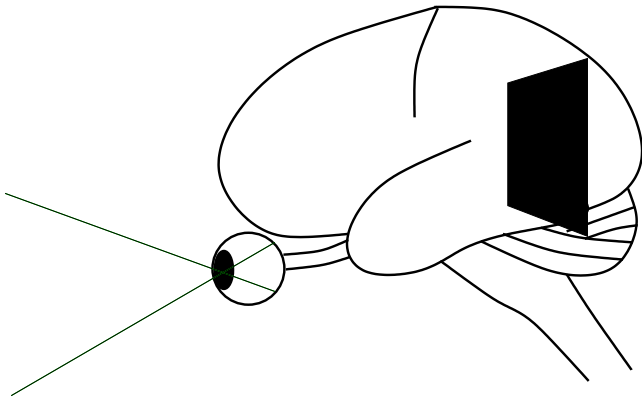
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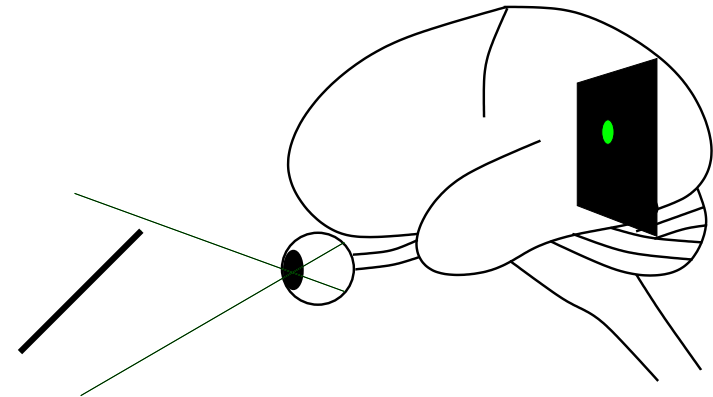
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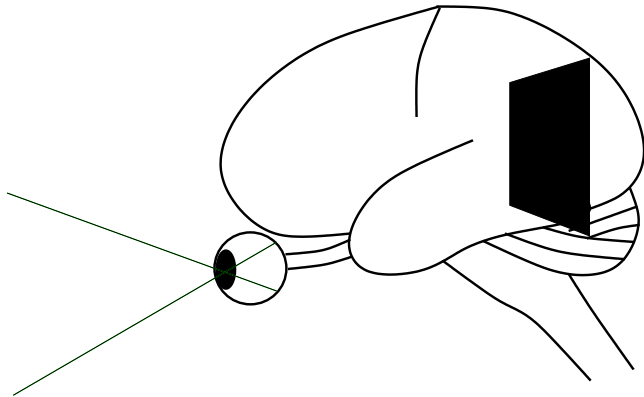
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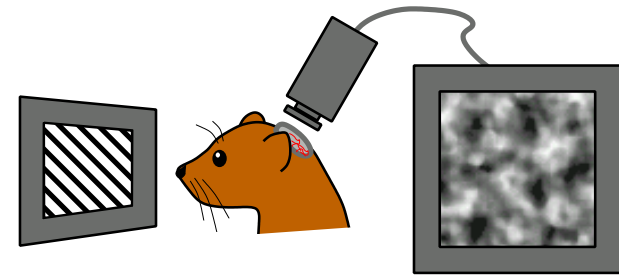
## They Are Visual Cortical Responses to Oriented Lines



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## The Main Question



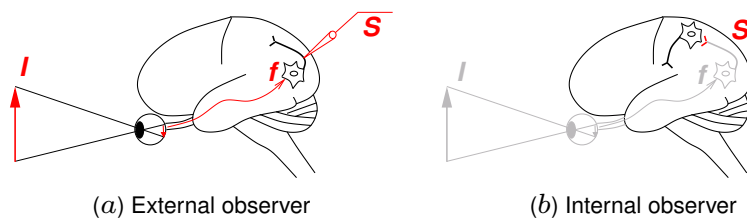
How can we understand what the **pattern of activity** in the brain **means**? (cf. Freeman 2003)

1. How can **scientists** understand the pattern?
2. How does **the brain itself** make sense of its **own activity**?

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## Scientist vs. the Brain

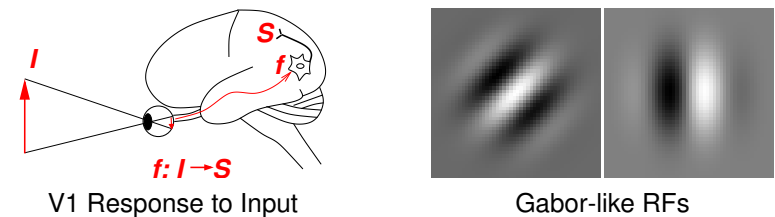


- External observer (e.g., a neuroscientist) **can figure out** how  $S$  relates to  $I$  (transformation  $f : I \rightarrow S$ ).
- Internal observer **cannot**: But the brain does this all the time, so this does not seem right!

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## Example: The Visual Cortex

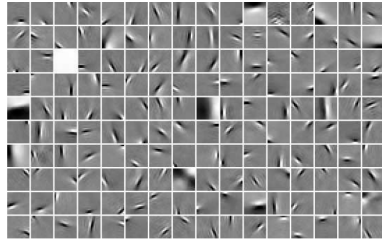


- With access to both  $I$  and  $S$ , Hubel and Wiesel (1959) figured out  $f : I \rightarrow S$  in V1 (oriented Gabor-like receptive fields Jones and Palmer 1987).
- But even before that, and with access to only  $S$ , humans had no problem perceiving orientation.

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## Theories on RF Formation



Hoyer and Hyvärinen (2000)

Well-developed understanding on how RFs form:

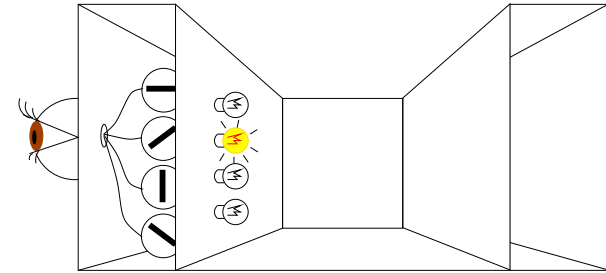
- Olshausen and Field (1997): Sparse coding; Barlow (1994): Redundancy reduction; Bell and Sejnowski (1997): Information maximization; Miikkulainen et al. (2005): Self-organization through Hebbian learning.

However, how is the resulting code to be used remains a question.

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## A Metaphor of the Problem



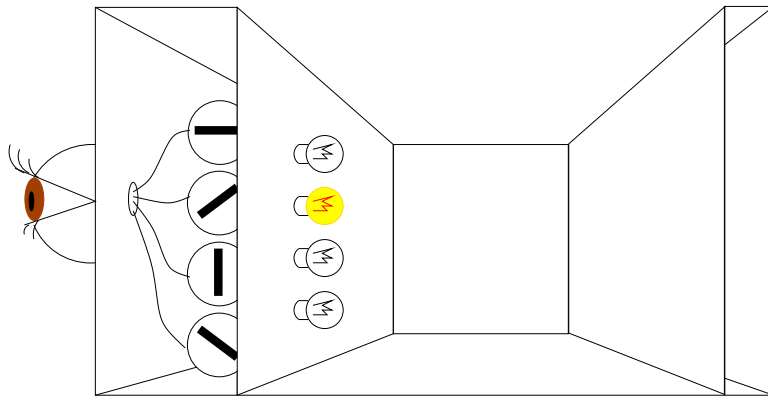
- Imagine sitting in a room, looking at blinking lights, without knowledge of the sensors nor the RFs.
- The lights may be due to any other sensory modality (as in vision-audition rewiring Sur et al. 1999).
- Similar to the **Chinese Room** (Searle 1980): Problem of “**Symbol Grounding**” (Harnad 1990).

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## The Sensory Organ Can (Possibly)

### Give Us a Clue

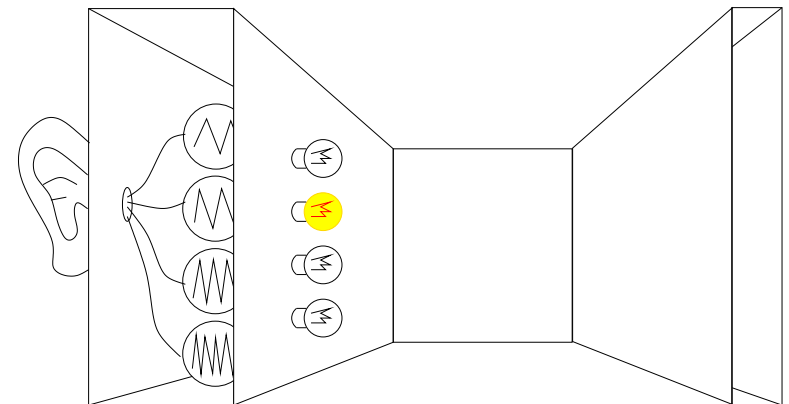


- It could have been caused by a **visual input**.

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## But, Equally Likely Is ...

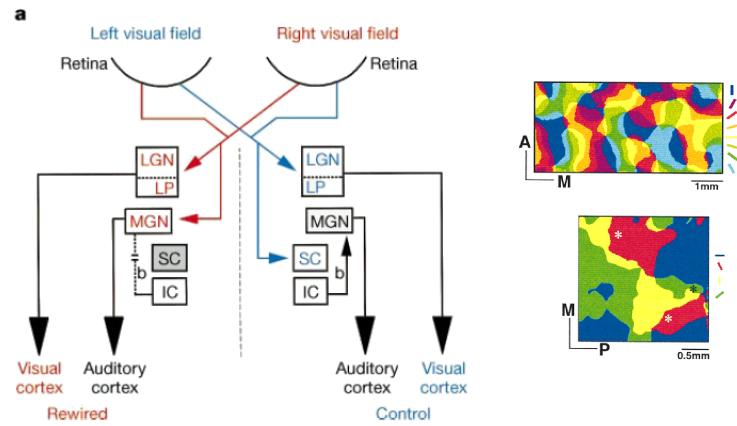


- It could have been caused by an **auditory input**.
- Sur et al., Rewiring cortex, *Journal of Physiology*, 41:33–43, 1999

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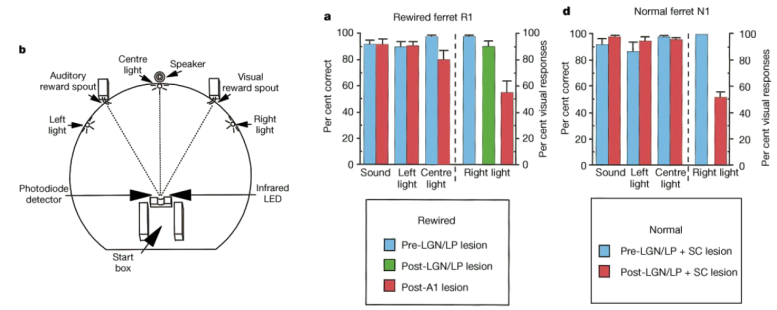
# Rewiring Vision to Auditory Area



von Melchner et al. (2000); Sharma et al. (2000); Sur et al. (1999)

- Rewired auditory cortex develops **visual cortex-like** organization.
- Question: does it **see** light or **hear** light?

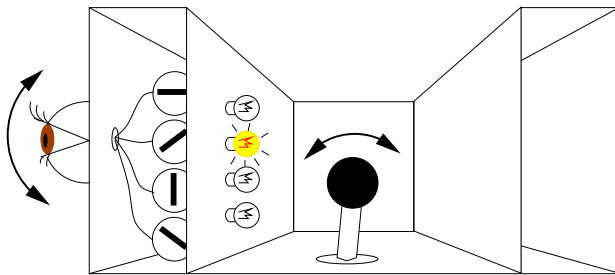
# Rewiring: Behavioral Results



von Melchner et al. (2000); Sharma et al. (2000)

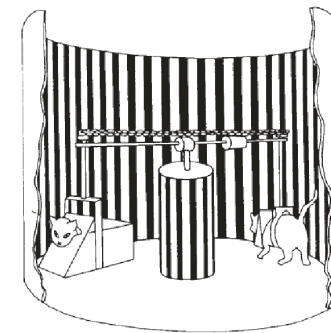
- Ferret **trained to behave differently** for visual vs. auditory stimuli: Behavior *suggests* that the ferret is actually **seeing** light **with its auditory cortex!**

# Possible Solution: Through Action



- A major problem in the metaphor is the **passiveness** of the whole situation.
- Adding action **can help solve** the problem.
- But **why** and **how**?

# Experimental Evidence

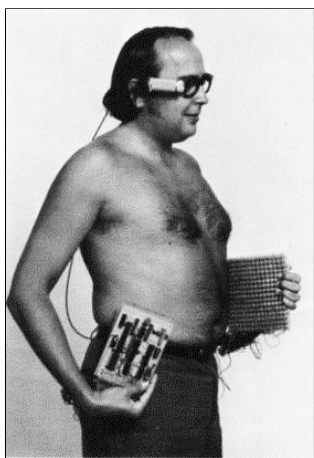


Held and Hein (1963)

- Active animal developed normal vision.
- Passive animal did not.
- Suggests the importance of action in vision.



## Experimental Evidence



Bach y Rita (1972; 1983)

- Vibrotactile array linked to a video camera.
- Passive viewing results in **tactile** sensation.
- Moving the camera results in a **vision-like** sensation.
- Sensation as related to **voluntary/intentional action** may be the key!

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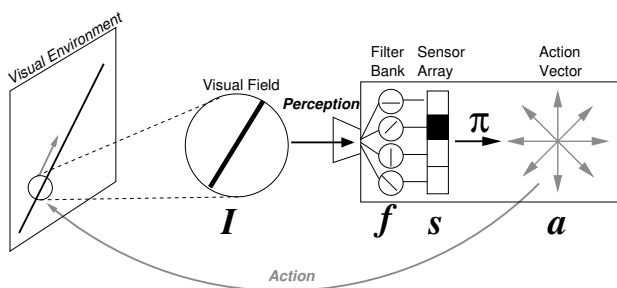
## Theoretical Insights

- Philipona et al. (2003) showed that properties of ambient space (such as the dimensionality) can be inferred based on internal sensory input alone.
- The key concept is about the compensability between ego-motion and the change in the environmental input conveyed to exteroceptors.

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## Approach: A Sensorimotor Agent



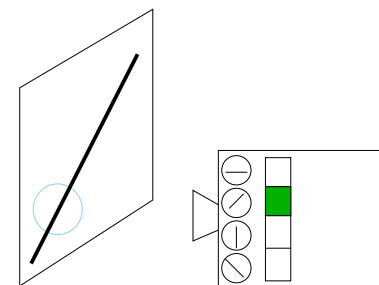
Choe and Bhamidipati (2003)

- A simple **visuomotor** agent.
- **How** can it **learn** about the visual world?
- What should be the **objective (or goal)** of learning?

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## Action for Unchanging Internal State

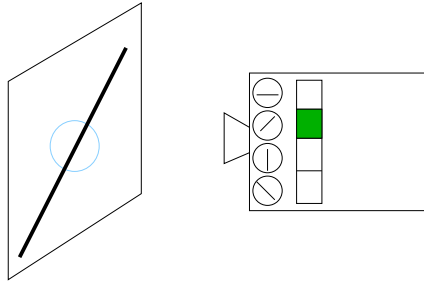


- Diagonal motion causes the *internal state* to **remain unchanging** over time.
- Property of such a movement **exactly reflects** the property of the input  $I$ : Semantics figured out through action.

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## Action for Unchanging Internal State

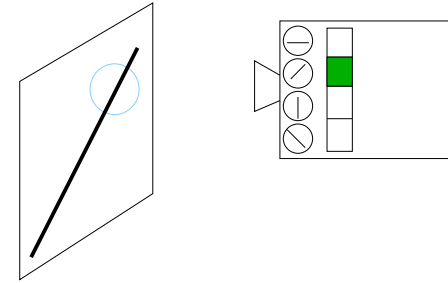


- Diagonal motion causes the *internal state* to **remain unchanging** over time.
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## Action for Unchanging Internal State

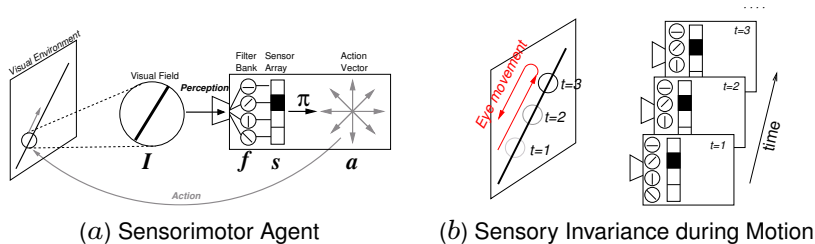


- Diagonal motion causes the *internal state* to **remain unchanging** over time.
- Property of such a movement **exactly reflects** the property of the input  $I$ : Semantics figured out through action.

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## Action for Internal Invariance



- Agent can **move** its visual field.
- Movement in a certain direction (diagonal) causes the *sensory array* to **stay invariant** over time.
- Property of such a movement **exactly reflects** the property of the input  $I$ .

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## Outline of Experimental Methods

- Input preparation.
- Orientation response calculation.
- Learning algorithm and policy generation.

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## Methods: Input Preparation

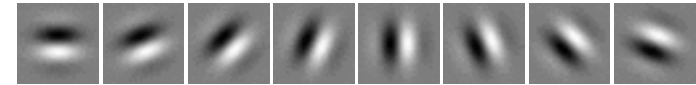


- Convolve with Difference-of-Gaussian (DoG) filter ( $15 \times 15$ ).
- Then, sample a  $31 \times 31$  region.

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## Methods: Orientation Response



- Find the vectorized dot product of the  $31 \times 31$  input  $I$  and the  $n$  Gabor filters  $G_i$  ( $i = 1..n$ ,  $\theta = \lfloor (i - 1)\pi/n \rfloor$ ):

$$r_i = \sum_{x,y} G_i(x,y)I(x,y).$$

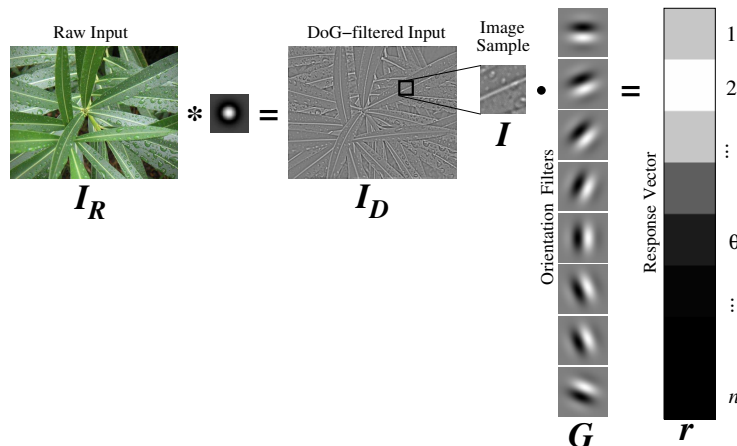
- The above results in a response vector  $\mathbf{r}$ , and the orientation response  $s$ :

$$s = \arg \max_{i=1..n} r_i$$

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## Orientation Response



Sensory state:

$$s = \arg \max_{1 \leq \theta \leq n} r_\theta.$$

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## Methods: Reinforcement Learning (Reward)

- Immediate reward is measured as the dot product of current and previous response vectors:

$$\rho_{t+1} = \mathbf{r}_t \cdot \mathbf{r}_{t+1}$$

- The task the agent is to learn a state-to-action mapping so that it maximizes the reward  $\rho$ .

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## Methods: Policy $\pi$

Suppose we know the probability  $P(a|s)$  (let us call this  $R(s, a)$ ), where stochastically generating action given the state  $s$  with this probability maximizes the reward.

1. Given the current state  $s_t \in S$ , randomly pick action  $a_t \in A$ .
2. If  $a_t$  equals  $\arg \max_{a \in A} R(s_t, a)$ ,
  - (a) then perform action  $a_t$ ,
  - (b) else perform action  $a_t$  with probability  $R(s_t, a_t)$ .
3. Repeat steps 1 to 3 until exactly one action is performed.

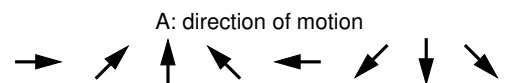
In practice, momentum was added so that  $a_{t+1} = a_t$  with a 30% chance, and in step 2, if a random draw from  $[0..1]$  was less than  $cR(s_t, a_t)$ , then the action was accepted.

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## Reward Probability Table

A: direction of motion



S: sensory state (orientation)

	0.5	0	0	0	0.5	0	0	0
	0	0.5	0	0	0	0.5	0	0
	0	0	$R(s, a)$	0	0	0	0.5	0
	0	0	0	0.5	0	0	0	0.5

- Reward probability  $R(s, a)$  can be tabulated.
- In an ideal case (world consists of straight lines only), we expect to see two diagonal matrices (shaded gray, above).

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## Methods: Learning $R(s, a)$

- A simple update rule was used:

$$R_{t+1}(s_t, a_t) = R_t(s_t, a_t) + \alpha \rho_{t+1},$$

where  $\alpha = 0.002$  is the learning rate, and  $\rho_{t+1}$  the immediate reward.

- $R_{t+1}(s_t, a)$  was then normalized by:

$$R_{t+1}(s_t, a) := \frac{R_{t+1}(s_t, a)}{\sum_{a' \in A} R_{t+1}(s_t, a')}, \text{ for all } a.$$

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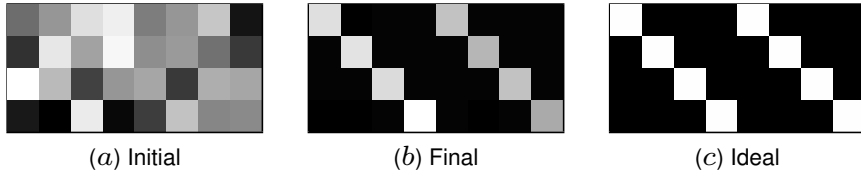
## Results: Overview

1. Synthetic input and natural image input.
2. Learned  $R(s, a)$ .
3. Error in  $R(s, a)$  and average reward  $\rho$  over time.
4. Distribution of reward  $\rho$ .
5. Gaze trajectory.

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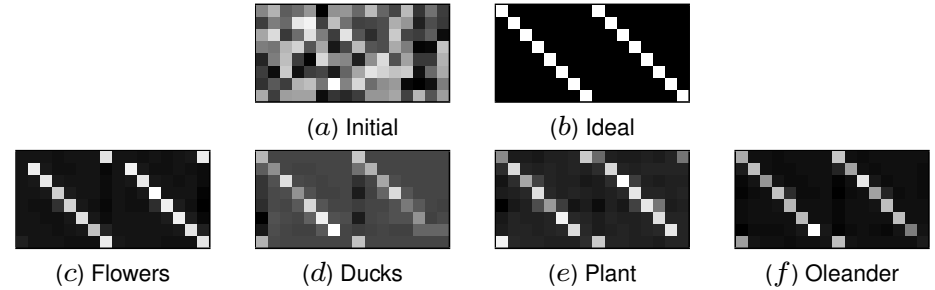
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## Results: Learned $R(s, a)$ for Synthetic Input



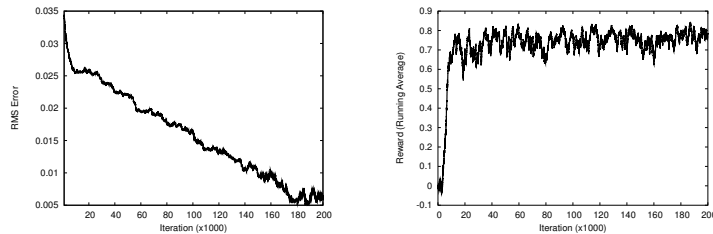
- Learned  $R(s, a)$  close to ideal.

## Results: Learned $R(s, a)$ for Natural Images



- Learned  $R(s, a)$  close to ideal even for natural image inputs.

## Results: Error in $R$ and Average $\rho$

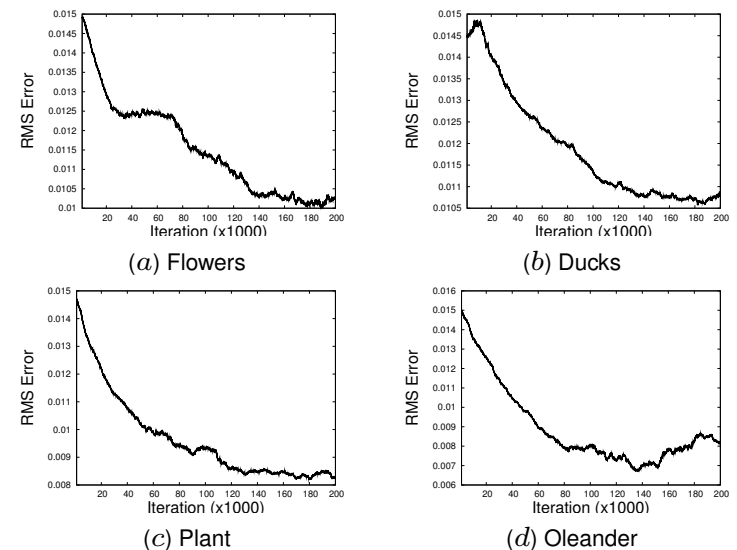


Synthetic Input

- Left: Root-mean-squared error in  $R(s, a)$  compared to the ideal case.
- Right: running average of immediate reward  $\rho$ :

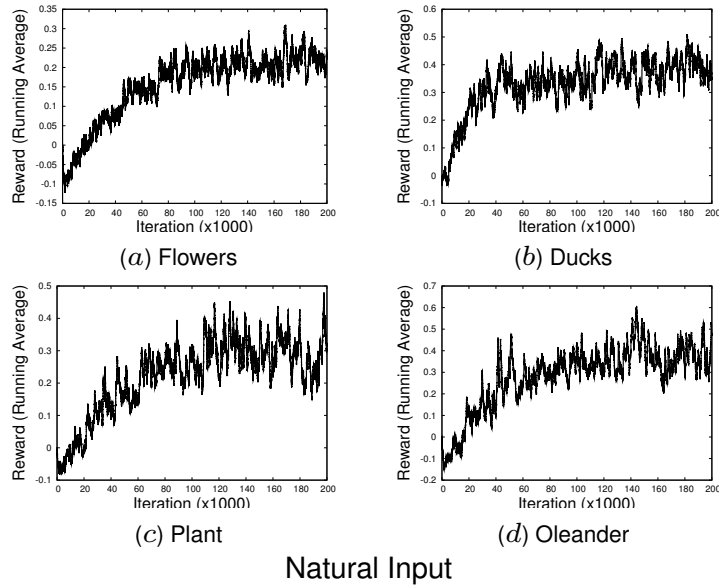
$$\mu_t = (1 - \alpha)r_t + \alpha \mu_{t-1}, (\mu_1 = \rho_1, \alpha = 0.999).$$

## Results: Error in $R(s, a)$



Natural Input

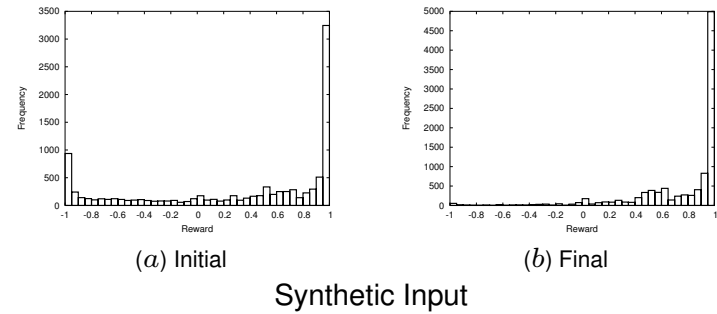
## Results: Average $\rho$



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## Results: Distribution of $\rho$

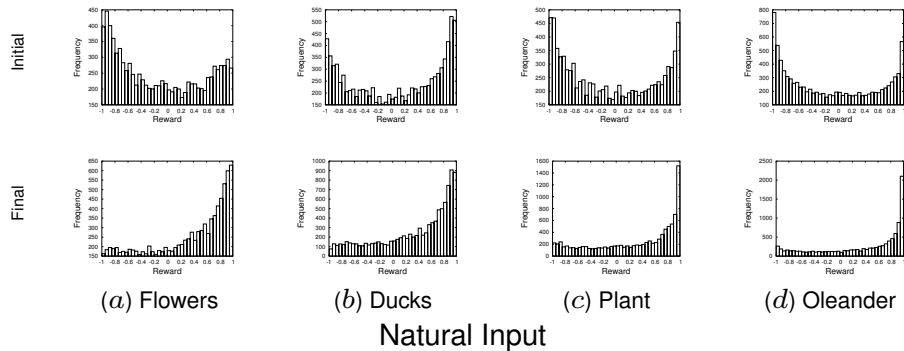


- Initially, two peaks: near negative min and positive max  $\rho$ .
- Near the end, only one peak: near positive max  $\rho$ .

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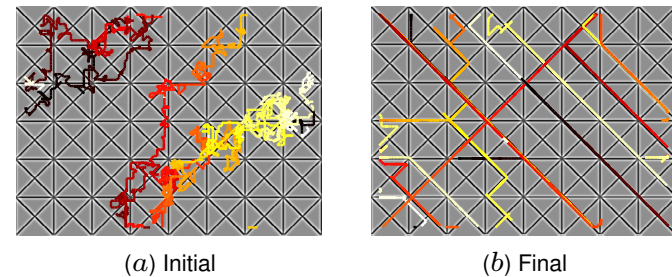
## Results: Distribution of $\rho$



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## Results: Gaze Traj. for Synth. Input

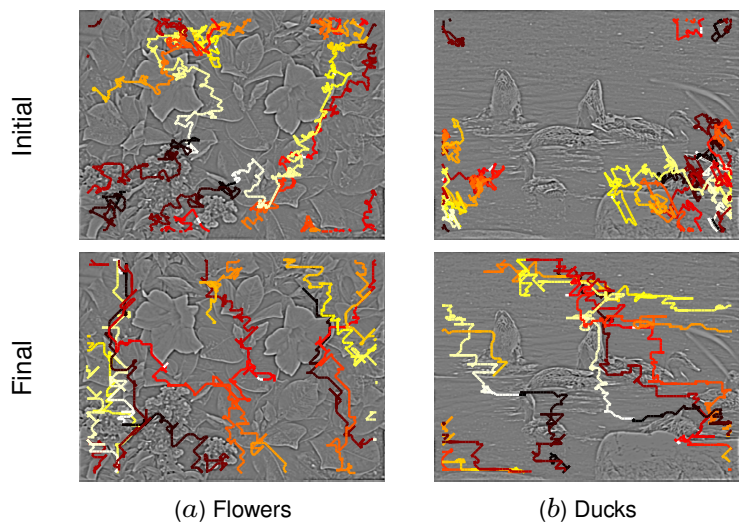


- Gaze trajectory reflects orientation represented by internal state.

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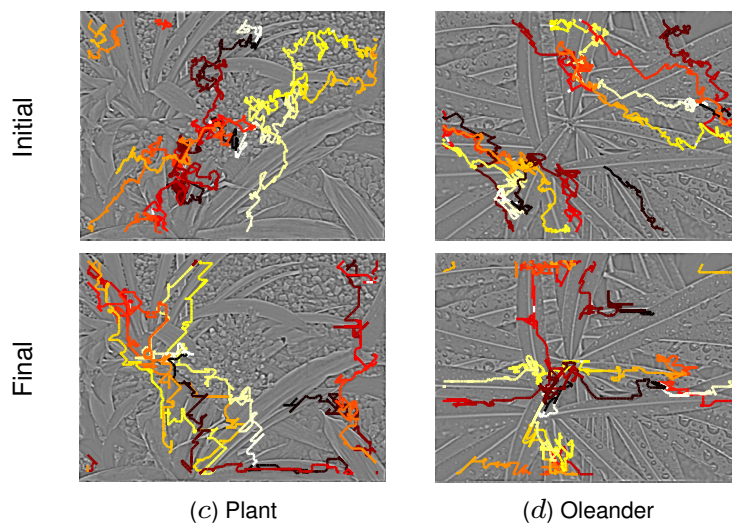
## Results: Gaze Traj. for Nat. Input



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## Results: Gaze Traj. for Nat. Input

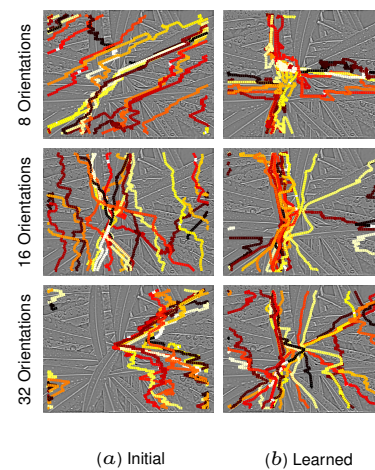


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## Results: Demo

## Work in Progress: Q-Learning



Trajectories from Q-Learning sessions (Choe and Smith 2006).

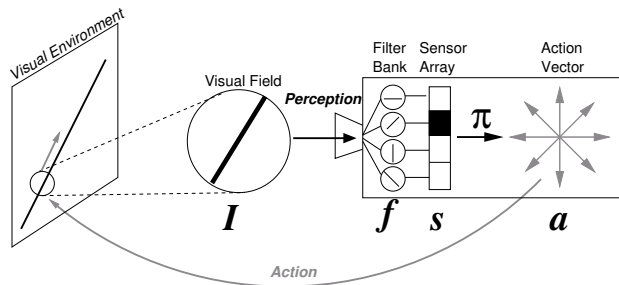
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## Interpretation of the Results

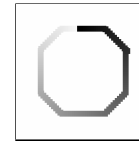


- Using **invariance** as the only criterion, particular **action pattern** that has the **same property** as the input that triggered the sensors was learned.
- Question: Can this approach be extended to learning complex stimulus concepts?

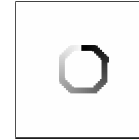
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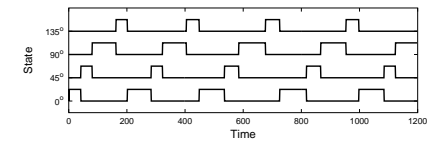
## Learning About Complex Objects



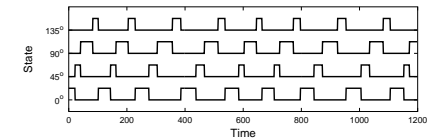
(a) Eye position (large input)



(c) Eye position (small input)



(b) Internal state (large input)



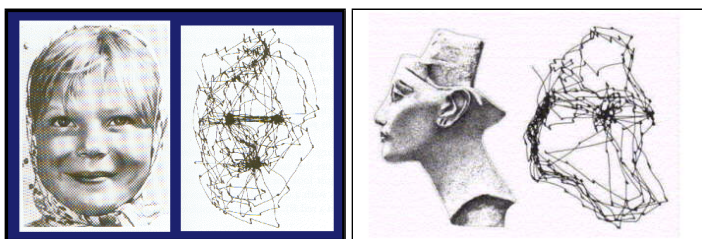
(d) Internal state (small input)

- For complex objects, a history of sensory activity may be needed (i.e., some form of memory).
- Invariance can be detected in the spatiotemporal pattern of sensor activity.

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## Supporting Evidence?



Yarbus (1967)

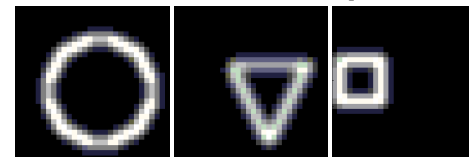
- When we look at objects, our gaze wanders around.
- Could such an interaction be necessary for object recognition?

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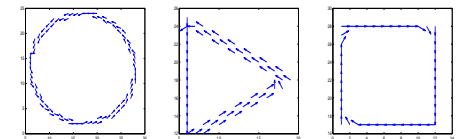
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## Advantage of Motor-Based Memory

### (Habit, or Skill)



(a) Sensor-based Representation



(b) Motor-based Representation

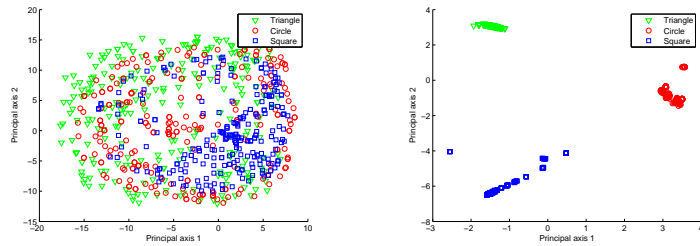
- Sensor-based representations may be hard to learn and inefficient.
- Motor-based approaches may generalize better.
- Comparison: Make both into a 900-D vector and compare backpropagation learning performance.

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## Class Separability

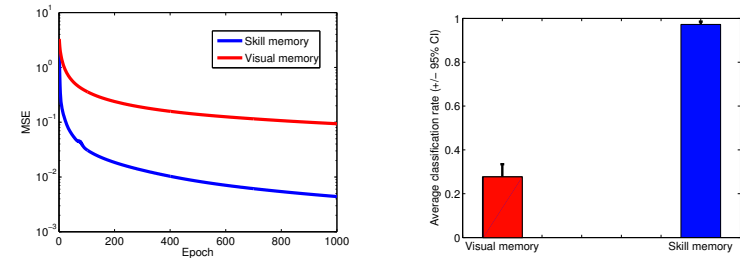


(a) Visual Memory

(b) Motor Memory

- Comparison of PCA projection of 1,000 data points in the visual and motor memory representations.
- Motor memory is clearly separable.

## Speed and Accuracy of Learning



(a) Training Speed

(b) Generalization Accuracy

- Motor-based memory resulted in faster and more accurate learning (10 trials).

## Summary

- Internal observer can learn about the properties of the external environment – through **action** maximizing **invariance** in neural activity.
- Such actions **closely reflect** the property of the stimulus that triggered the sensory neuron to fire: **Meaning** of the spike recovered (through action)!
- **Main contribution:** The **invariance criterion** for autonomously learning the **meaning** of neural states.

## Related Work (Selected)

- Piaget (1952): Sensorimotor period in child development
- Freeman (1999): Brain creates meaning through action and choices. Also see Kozma and Freeman (2003) for a KIV model of the emergence of goal-directed, intentional behavior.
- O'Regan and Noë (2001): Sensorimotor contingency theory
- Philipona et al. (2003): Inferring space through sensorimotor interaction
- Rizzolatti et al. (2001): Mirror neurons
- Gibson (1950): Direct perception of invariance and affordance
- Harnad (1990): Symbol grounding on robotic capabilities.
- Taylor (1999): Corollary discharge and awareness of attention movement prior to sensory awareness.

## Discussion

- Why is **knowing** ones own **action** any easier than **perceptual interpretation**?: Knowledge of own action may be more **immediate** than perception (cf. Moore 1996, citing Bergson).
- What gives rise to **voluntary, intentional action** and why is it special? (Freeman 1999; Kozma and Freeman 2003; Taylor 1999).
- A different view of **invariance**: Not (only) something to be detected in the environment (cf. Gibson 1950), but something that we **actively seek within**.

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## Discussion (Cont'd)

- Why not just **analyze the input directly**?: The raw input is only available at the immediate sensory surface.
- What about **other sensory modalities** (such as touch, olfaction, or audition)?
- The learning scheme **depends** on **structure** in the environment: If the environment didn't have structure, the agent can never learn.

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## Discussion (Cont'd)

- Relation to **mirror neurons** (Rizzolatti et al. 2001)?
- Role of **attention** (e.g. Rensink et al. 1997; Taylor 1999)?: Attention may be needed when ambiguities are present.
- Do **motor primitives** restrict the kind of sensory property that can be learned? What kinds of motor primitive do we have?

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## Discussion (Cont'd)

- What about meaning **other than sensorimotor-like**, such as reinforcement signals (Rolls 2001) or “feeling” (Harnad 2001)?
- **Grounding on perception alone** may not be sufficient: cf. Perceptual symbol system (Barsalou et al. 2003).
- What to make of the segregation in the **dorsal–ventral pathway**? (Goodale and Milner 1992).

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## Predictions

- Perceived orientation of a line can be altered by eye movement in the direction of incompatible orientation.
- Motor structures (cerebellum, basal ganglia) may be intimately involved in semantics.
- Geometrical understanding may be limited by the motor primitive repertoire.

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## Future Work (and Work in Progress)

- Learning receptive field structure based on SIDA.
- Lateral inhibition in sensory array.
- Crossmodal association through sensory invariance.
- Extending to more complex concepts.

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## Conclusions

- We must ask how the brain understands itself.
- Autonomous understanding of own internal state is non-trivial without direct access to the stimulus.
- Action can help solve the conundrum.
- Action that maintains invariance in internal state can recover meaning (the property of the stimulus).

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## Credits

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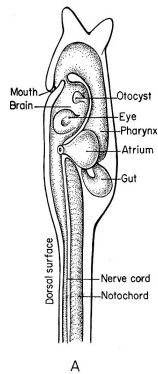
## Why Do We Have a Brain?



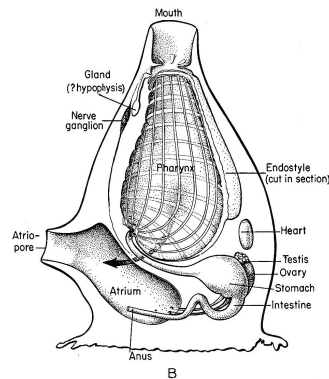
Tree  
(no Brain)

- Brain vs. no brain

Sources: <http://homepages.inf.ed.ac.uk/jbednar/> and <http://bill.srn.arizona.edu/classes/182/Lecture-9.htm>



Tunicate  
Free-floating  
(w/ Brain)



Tunicate  
Settled  
(w/o Brain)

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