

ARQ Error Control

- Two types of errors
 - Lost frames
 - Errors in frames
- Most Error Control techniques are based on
 1. Error detection scheme (e.g. parity checks, CRC), and
 2. Retransmission Scheme
- Error Control schemes that rely on error detection and retransmission of lost or corrupted frames are called **Automatic Repeat Request (ARQ)** error control

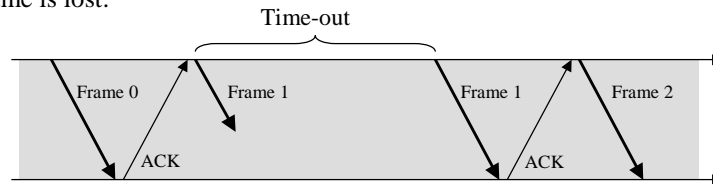
Basic Elements of ARQ

All ARQ retransmission schemes use a combination of the following components:

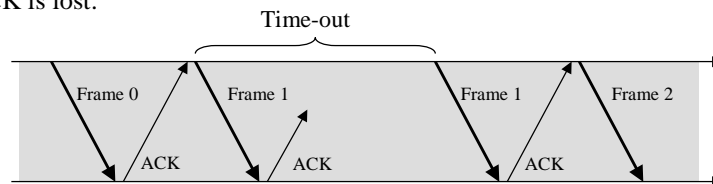
- Receiver sends an **acknowledgement (ACK)** to notify sender that frame is correctly received
- Receiver sends a **negative acknowledgement (NACK)** to notify sender that frame is incorrectly received
- Sender sends **enquiry (ENQ)** to trigger the receiver to transmit current state (in form of an ACK)
- Sender retransmits packet if ACK is not received within a **timeout** interval

Stop-and-wait ARQ

Frame is lost:

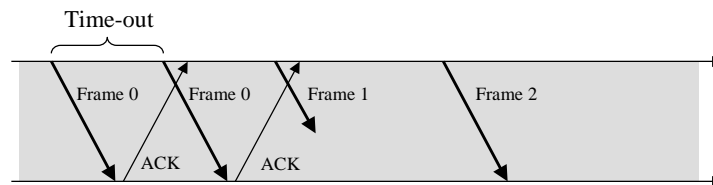


ACK is lost:



Other Ambiguities in ARQ

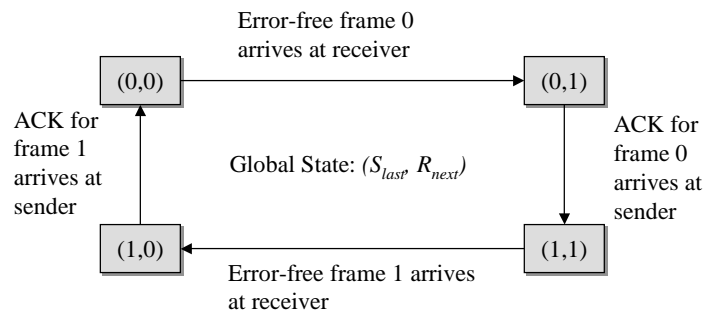
ACKs must be numbered, otherwise:



ACKs need sequence numbers in order for senders to match ACKs to frames that have been sent!

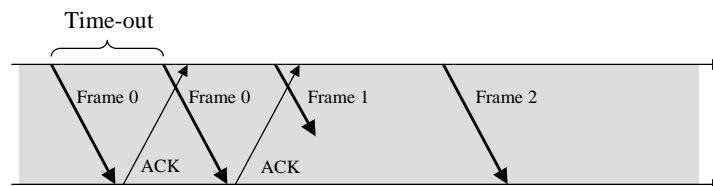
Sequence Numbers

- Sequence Numbers avoid ambiguities, but need to be limited in size (avoid overflows!)
- Example: One-bit sequence numbers in Stop-and-Wait ARQ
 - S_{last} : Sequence number of last sent frame at sender
 - R_{next} : Sequence number of next expected frame at receiver

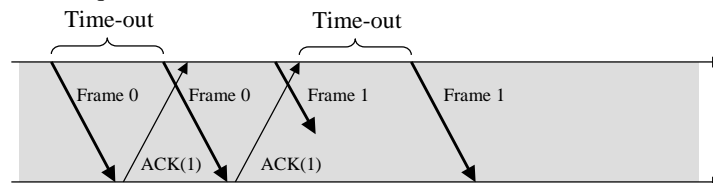


One-bit Sequence Numbers Solve Problem of Misinterpreted Duplicate ACKs

No sequence numbers:

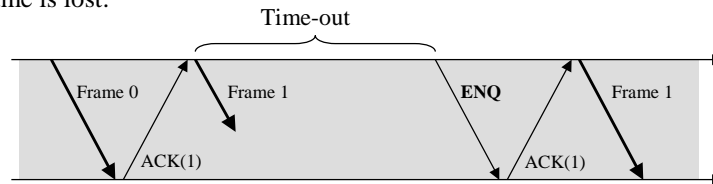


One-bit sequence numbers:

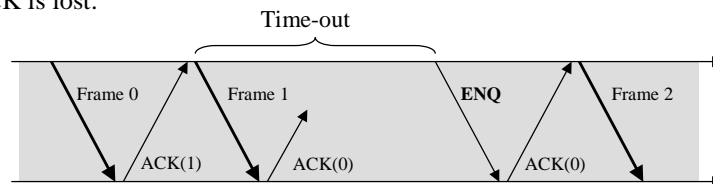


Variations of Stop-and-wait ARQ: ENQ Frames

Frame is lost:

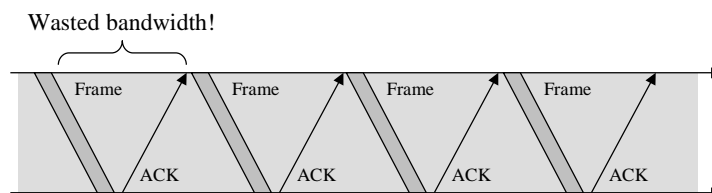


ACK is lost:



Inefficiency of Stop-and-wait ARQ

- **Efficiency** of a protocol is the maximum fraction of time when the protocol is transmitting data.

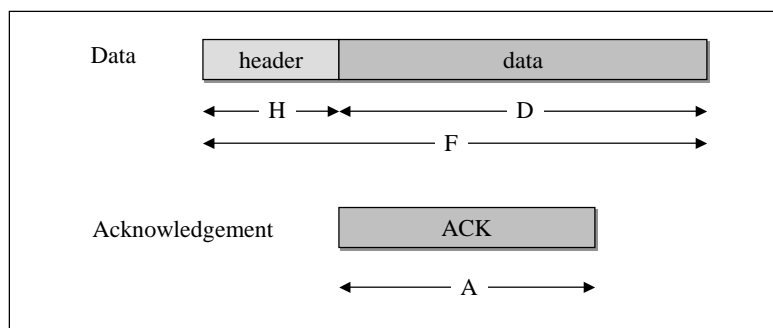


Analysis of Stop-and-wait

- Notation:

C	= Channel capacity (in bits/sec)
I	= Propagation delay
H	= Number of bits in a frame header
D	= Number of data bits in a frame
F	= Total length of a frame ($F = D + H$)
A	= Total length of an ACK frame
F/C	= Transmission delay for a frame

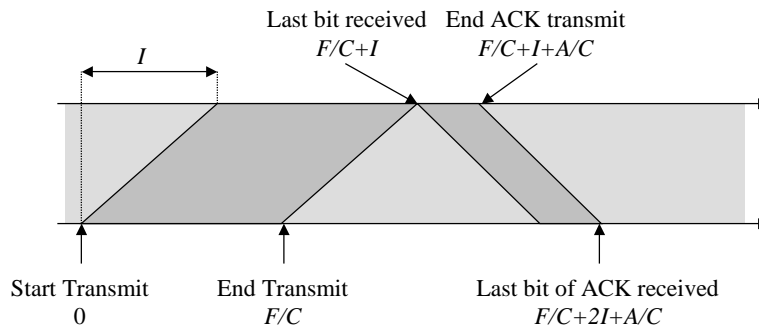
Analysis of Stop-and-wait (2)



$$a = \frac{\text{propagation_delay}}{\text{transmission_delay}} = \frac{I}{F/C}$$

Analysis of Stop-and-wait (3)

Transmission of a frame (in Stop-and-wait):



Analysis of Stop-and-wait (4)

- Efficiency of Stop-and-Wait (error-free case):

$$efficiency = \frac{D/C}{F/C + A/C + 2I} = \frac{D}{F + A + 2IC}$$

- Assuming that H and A are negligible, we obtain:

$$normalized_efficiency = \frac{D}{D + 2IC} = \frac{1}{1 + 2a}$$

Example 1: Satellite Link

Satellite link:

- Roundtrip propagation delay: 270ms
 - Data rate: 56kbps
 - Frame length : 4000bit (including header)
 - Length of ACK frames is negligible
-
- What is the value of a ?
 - What is the efficiency of the satellite link if Stop-and-Wait is used?

Example 2: LAN

Local Area Network:

- Data rate: 10 Mbps (100Mbps)
 - Propagation rate: 200,000 km/sec
 - Length of LAN: 10km
 - Frame size: 500 bit (including header)
 - Length of ACK frames is negligible
-
- What is the value for a for the LAN?
 - How efficient is the LAN?
 - What is the minimum frame size in the LAN to reach an efficiency of at least 80%?

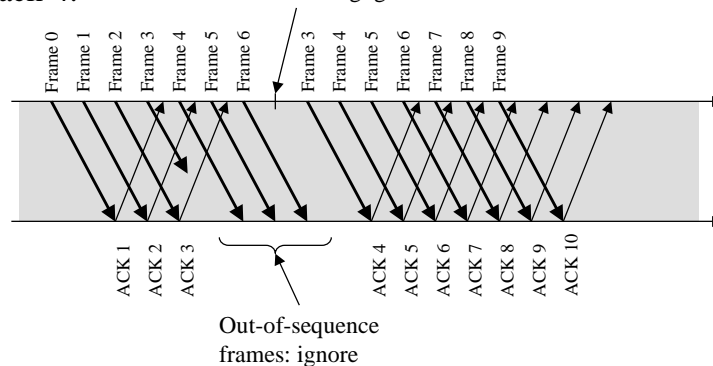
Go-back- N ARQ

- Problem with Stop-and-Wait ARQ:
 - Only one frame can be in transit at a time
 - This is inefficient when $a > 1$
- Solution:
 - Pipeline transmission by allowing multiple (W_s = window size) frames to be in transit, with ACKs outstanding
 - Choose W_s to be larger than bandwidth product, in order to keep channel busy

Basic Go-back- N ARQ

Idea of basic Go-back- N ARQ: Allow for $W_s = N$ outstanding packets at any given time. Whenever number of outstanding packets exceeds W_s , assume that something went wrong, and retransmit all of them.

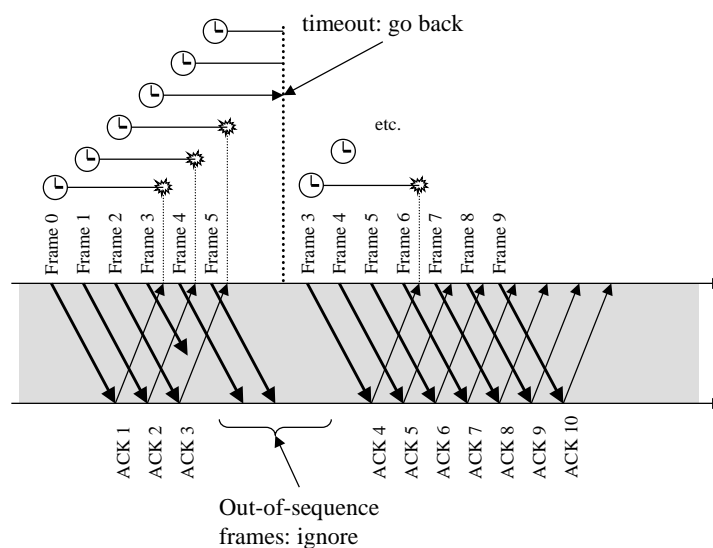
Go-back-4: 4 frames are outstanding: go back 4



Go-back- N with Timers

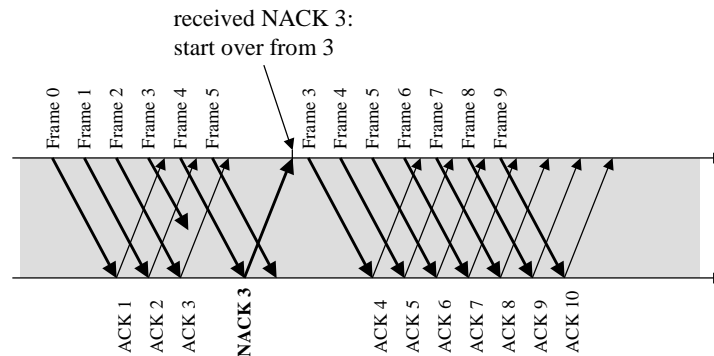
- Problem with basic Go-back- N :
 - Sender needs to keep sending in order to have outstanding frames, and so detect missing ACK.
- Alternative:
 - Associate timer with every outstanding frame.
 - Timeout triggers re-transmission from affected frame on.

Timers in Go-back- N ARQ



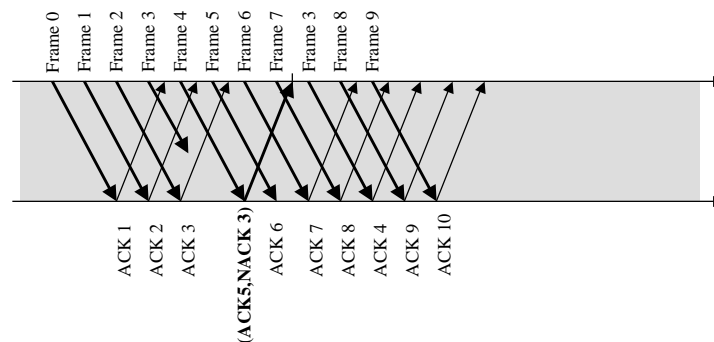
Go-back-N ARQ with NACKs

- Receiver sends NACK i if frame i is in error. After that, the receiver discards all incoming frames until it correctly receives frame i .
- If sender receives a NACK i it will retransmit frame i and all frames $i+1, i+2, \dots$ that have not been acknowledged.



Selective-Repeat ARQ

- The sender only retransmits frames for which NACK is received.
- Receiver buffers frames that come out of sequence. Receiver maintains a **receiver window**.



Analysis of ARQ

- Earlier: Analysis of Stop-and-Wait ARQ for no-error case.
- Assumptions:
 - Channel can experience frame errors.
 - Control frames (ACKs, NACKs) have no errors.
 - Sizes of control frames are negligible.

Review: Analysis of Stop-and-Wait ARQ

- Notation:
 - C = Channel capacity (in bits/sec)
 - I = Propagation delay
 - F = Total length of a frame ($F = D+H$)
 - $T = F/C$ = Transmission delay for a frame
 - P = Probability that frame is erroneous
 - U = Efficiency

- Stop-and-Wait with no error:

$$U = \frac{T}{T + 2I}$$

Stop-and-Wait ARQ: Error Case

- Probability that k transmission attempts are needed to successfully transmit a frame:

$$P[k \text{ attempts needed}] = P^{k-1} \cdot (1 - P)$$

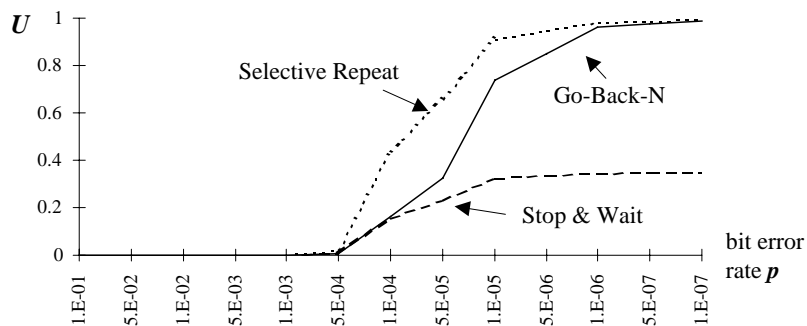
- Expected number of attempts ($= E[A]$)

$$E[A] = \sum_{i=1}^{\infty} i \cdot P^{i-1} \cdot (1 - P) = \frac{1}{1 - P}$$

- Expected efficiency with errors:

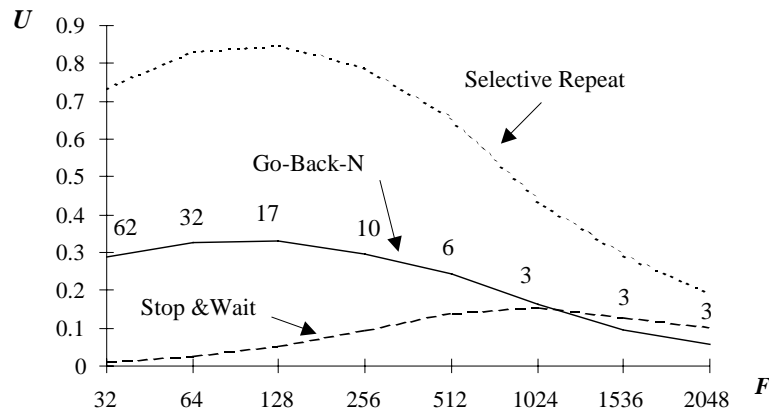
$$U = \frac{T}{E[A] \cdot (T + 2I)} = \frac{(1 - P) \cdot T}{T + 2I} = \frac{1 - P}{1 + 2a}$$

Efficiency of ARQ Protocols



1024 bit frames, 1.5 Mbps, 5msec prop delay, window size 4.

Analysis of ARQ Protocols: Optimal Frame Size

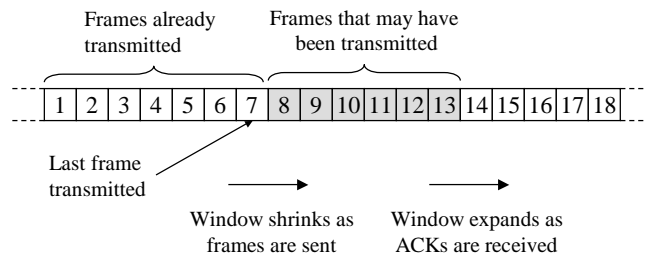


Flow Control

- Flow control is needed in order to match the speed of the sender to that of the receiver. This makes sure that data does not overflow at the receiving node.
- We assume (for simplicity) that there are no errors between sender and receiver.
- **Stop-and-Wait** Flow Control: receiver indicates readiness to receive data for each frame.
- **Sliding Window** Flow Control allows for transmission of multiple frames.

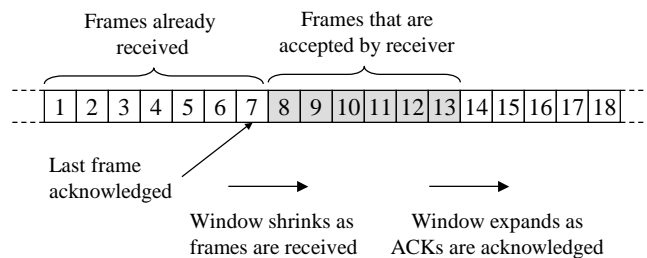
Operation of Sliding Window: Sender Window

- At any time, sender is permitted to transmit frames with sequence number in a certain range.
- This range of numbers is called the **sender window**.

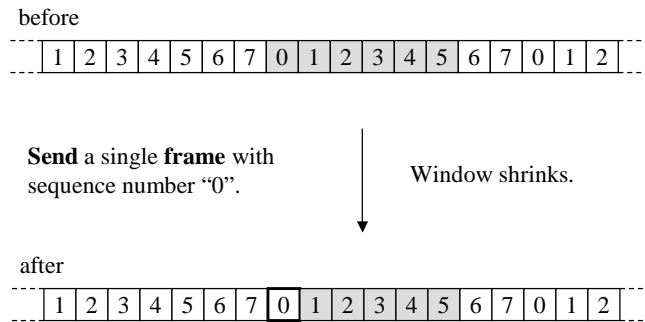


Operation of Sliding Window: Receiver Window

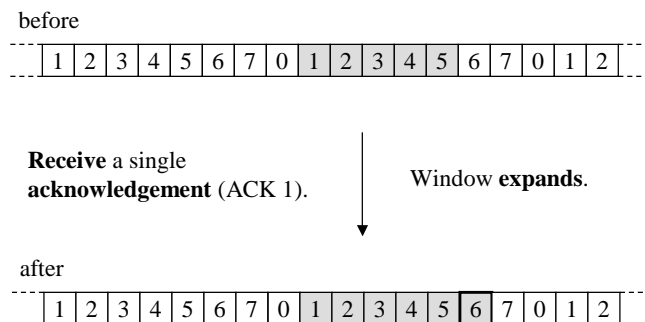
- The receiver maintains a **receiving window** of sequence numbers of frames that are accepted.



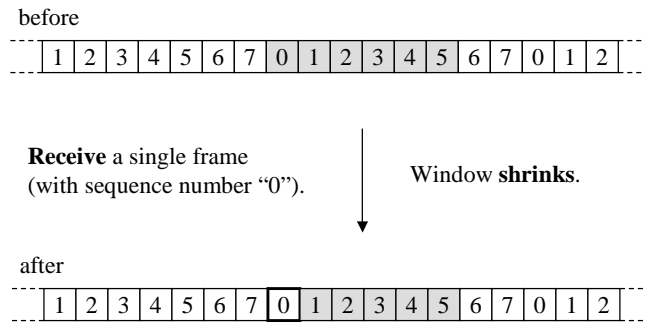
Operations at the Sender: Send Frame



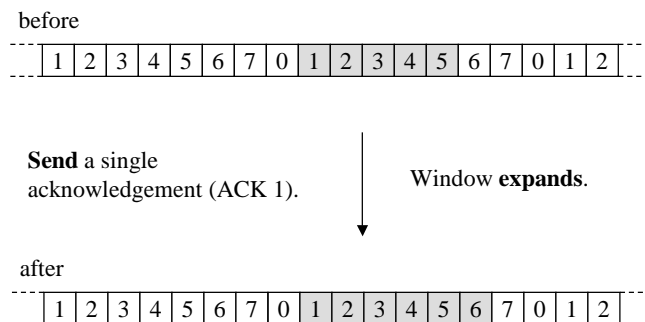
Operations at the Sender: Receive ACK



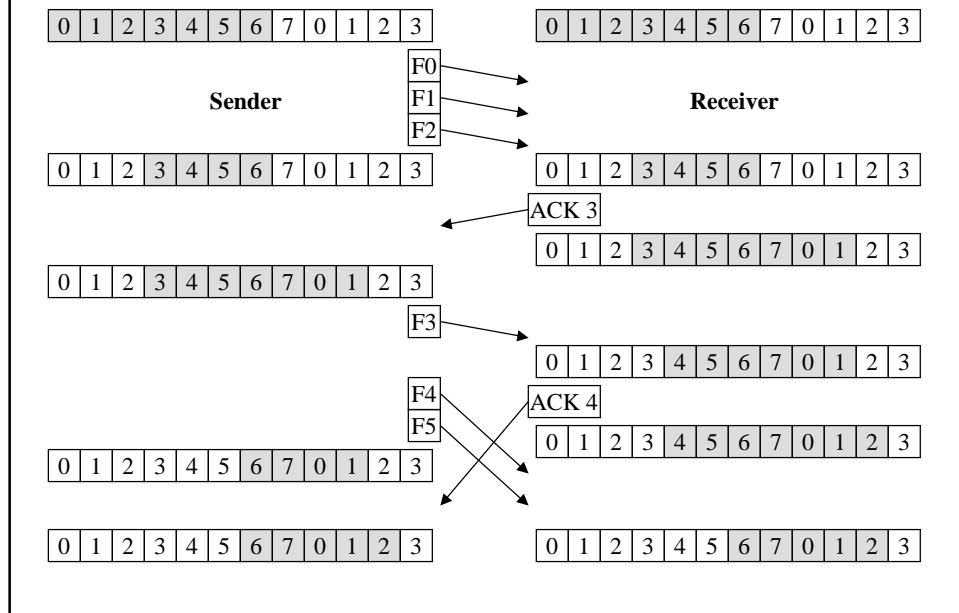
Operation at Receiver: Receive Frame



Operation at Receiver: Send ACK



Sliding Window: Example



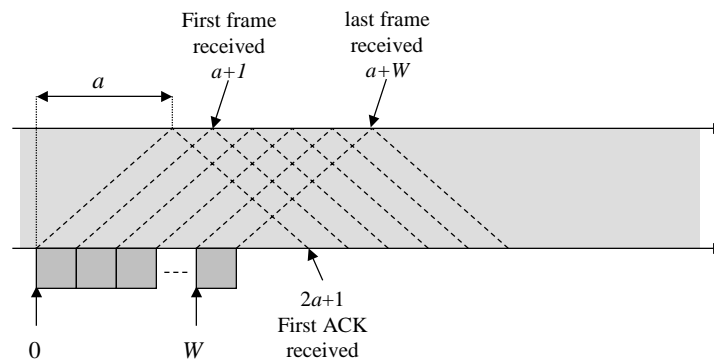
Performance of Sliding Window

- Simplify notation:

$$F/C = 1$$

$$I = a \quad (\text{Normalization})$$

W = Maximum window size (identical for sender and receiver)



Performance of Sliding Window

- Window must be sufficiently large in order for sender to send continuously.
- $W \geq 2a+1$: Sender can send continuously:

$$U = 1$$

- $W < 2a+1$: Sender can transmit W frames every $2a+1$ time units:

$$U = \frac{W}{1+2a}$$